

# EN2210 Continuum Mechanics

## Project

### Measuring the constitutive behavior of elastomeric sheets

#### Synopsis

You will design and construct a simple apparatus to subject an elastomeric sheet specimen to prescribed loads. You will use your equipment to determine the uniaxial and biaxial response of a sample, and fit the data with a hyperelastic constitutive equation of your choosing.

#### 1. Introduction

While most of the governing equations in continuum mechanics are invariable physical laws, the constitutive law for the solid or fluid of interest must always be determined and calibrated experimentally. Measuring the response of a material to prescribed loading is thus a standard problem in solid and fluid mechanics.

In this project, you will design and construct a simple apparatus to measure (approximately) the response of a thin elastomeric sheet to uniaxial and biaxial loading. You will use your equipment to select and calibrate a constitutive model that fits your data.

Your apparatus should be home-made and constructed from readily available materials, rather than making use of sophisticated equipment that you borrow from your lab!

You will need to devise some way to apply prescribed forces to the specimen, and measure the resulting deformation.



A few basic materials, hand-tools and supplies will be provided for you to work with. You can use other equipment and materials if you wish, but please acquire them legally... Use of facilities such as JEPIS, rapid prototyping, research engineer/technician help, or outsourcing to developing countries is not allowed!

Some questions you might try to answer include

1. Is the material incompressible (or close to it?)
2. Is the material isotropic?
3. What is its uniaxial and biaxial response?
4. Which hyperelastic potential gives the best fit to the measured data? What parameters yield the best fit?

The project should be done in groups (groups of 4 are suggested).

## 2. Project Deliverables:

Your mission is to provide:

1. An apparatus that is capable of measuring the constitutive behavior of elastomeric sheets
2. A short report (2 pages, one report per group) describing the constitutive law that you selected to model the material; giving values for relevant material properties, and comparing measured and predicted behavior (with an estimate of errors).
3. A 10 min oral presentation that demonstrates your design and reports the results of your measurements.

The due date for both is **Friday December 9**. Presentations will be given in class...

### Appendix 1: Grading Rubric

1. Design of experimental apparatus – 10 points.
  - Well built, robust and easy to use design that gives accurate and repeatable data
2. Report – 10 points
  - Clearly written description of experimental data; compared to predictions of various constitutive models
3. Presentation – 10 points
  - Articulate, well organized and correctly timed presentation that includes relevant data and results, with contributions from all group members.

### Appendix 2: Materials and tools

The catalog numbers are from McMaster-Carr (so you can find details of all the supplies on the web)

#### Tools (one of each per group)

Ultra economy plastic electronic calipers 4996A21  
Hacksaw 4077A1  
Electric drill  
Razor blades  
Flathead screwdriver

#### Instrumentation:

- Arduino Uno board  
<https://www.adafruit.com/categories/171?gclid=CJr9wbzIntACFdBMDQodd5ECVw>
- Two channel Arduino strain gauge/Load Cell/Wheatstone Bridge Shield  
<http://www.robotshop.com/en/strain-gauge-load-cell-amplifier-shield-2ch.html>
- 0.78kg micro load cell (two per group)  
<http://www.robotshop.com/en/micro-load-cell-0-78-kg.html>
- 5kg micro load cell (two per group)  
<http://www.robotshop.com/en/micro-load-cell-5-kg.html>
- IPEVO Point 2 View USB camera (one per group)  
<https://www.amazon.com/IPEVO-Point-View-USB-Camera/dp/B002UBPBTC>

## Materials

|   |             |
|---|-------------|
| Latex rubber dental dams (specimens)  |             |
| 1'x1' marine grade plywood board 1125T21  | 1 per group |
| Acrylic bars, 4' length, 1/8" thick, 1" wide 1227T119                             | 1 per group |
| Acrylic bars, 4' length, 3/16" thick 1" wide 1227T819                             | 1 per group |
| Acrylic bars, 4' length, 1/2" thick 1" wide 1227T419                              | 1 per group |
| Clear PVC unthreaded pipe, 4ft length, 0.344" ID, 1/4" OD, 49035K21               | 1 per group |
| Clear PVC unthreaded pipe, 4ft length, 0.602" ID, 3/4" OD, 49035K23               | 1 per group |
| 36" long 1/8" diameter birch dowell rod 9683K11                                   | 1 per group |
| 36" long 1/4" diameter birch dowell rod 9683K13                                   | 1 per group |
| Extra strength braided polyester twine, 0.033" dia, 50lb breaking strain, 8936T41 | 3 total     |
| Light force iron C clamp, 3" opening, 2" depth, 800lb holding cap, 5133A15        | 4 per group |
| 1/2" steel binder clips, 1/4" jaw opening, 12 per box, 12755T71                   | 2 box/group |
| Pulley blocks 3742T53   | 4 per group |
| Mounted pulleys 11/16 OD 3071T21  | 2 per group |
| Machine screw assortment 6-32 thread, 1/2", 1" 1 1/2" 2" 3"                       | In stock    |
| Machine screw 6-32 wing nuts 98671A110  | In stock    |
| 1/4" Eye bolts  | In stock    |

## Matlab commands for reading an Arduino and webcam

To read a webcam:

```
>> webcamlist;  
will list all the available cameras on your computer  
>> cam = webcam('camera name');  
Will create a webcam object  
>> preview(cam);  
will show a real-time preview of the image on the webcam  
>> img = snapshot(cam);  
will create an RGB image;  
>> imshow(img);  
will display it
```

You can find a simple code on the website that shows how to read and plot a voltage from an Arduino board