## Engineering 137, Advanced Engineering Mechanics Sem. II, '06-'07 Homework Set No. 9

**Instr: Rod Clifton** 

Due: in class Wednesday, April 12, 2006 or on 6th floor by noon on Thursday, April 13

- 1. While observing the free motion of an axially symmetric body, the following characteristics are noted:
  - (a.)  $\omega$  and H are separated by  $30^{\circ}$ ;
  - (b.) the precession rate  $\dot{\psi}$  is larger than the magnitude  $\omega$  of the angular velocity;
  - (c.) the axis of symmetry changes its direction in space by 90° during half of a precession cycle.

Solve for the ratio  $I_a/I_t$  and evaluate  $\dot{\psi}$  and the relative spin  $\dot{\phi}$  in terms of  $\omega$ .

- 2. A circular cone of mass m, base radius r, and height h=4r is rotating in free space with angular velocity components  $\omega_a=\Omega_0$  and  $\omega_t=0.5\Omega_0$ . Its center of mass has zero velocity initially.
  - (a.) What is the free precession rate  $\dot{\psi}$ ?
  - (b.) Next, the vertex of the cone is suddenly fixed, but the cone is otherwise unconstrained. What is the new precession rate?