

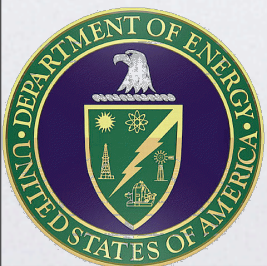


# Non-Perturbative Evidence for Technicolor

George T. Fleming  
(Yale U.)

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*Eleventh Workshop on Non-Perturbative QCD*  
l'Institut d'Astrophysique de Paris  
**06 June 2011**





# What is Technicolor?

- If EW symmetry  $SU(2)_L \times U(1)_Y$  were unbroken at GeV energies, QCD would break it via strongly-coupled Higgs mechanism.
- Pions eaten to give mass to  $W$  and  $Z$  bosons of  $O(100 \text{ MeV})$ .
- No analogue of Yukawa mechanism. Lots of very light pseudoscalar mesons due to  $N_f=6$  massless flavors.
- **Basic Idea:** Break EW symmetry at TeV scales by adding new fermions  $(\bar{Q}, Q)$  with new strong interactions. [Weinberg, Susskind 1979]
- **SM fermion mass:** New gauge interactions broken at high scale  $\Lambda_{\text{ETC}}$  couple SM fermions to techniquarks. [Dimopoulos-Susskind, Eichten-Lane 1979]

$$\text{Masses: } \frac{(\bar{Q}Q)(\bar{q}q)}{\Lambda_{\text{ETC}}^2} \quad \text{FCNC's: } \frac{(\bar{q}q)(\bar{q}q)}{\Lambda_{\text{ETC}}^2} \quad \Lambda_{\text{ETC}} \gtrsim 1000 \text{ TeV}$$

- [http://en.wikipedia.org/wiki/Technicolor\\_\(physics\)](http://en.wikipedia.org/wiki/Technicolor_(physics))



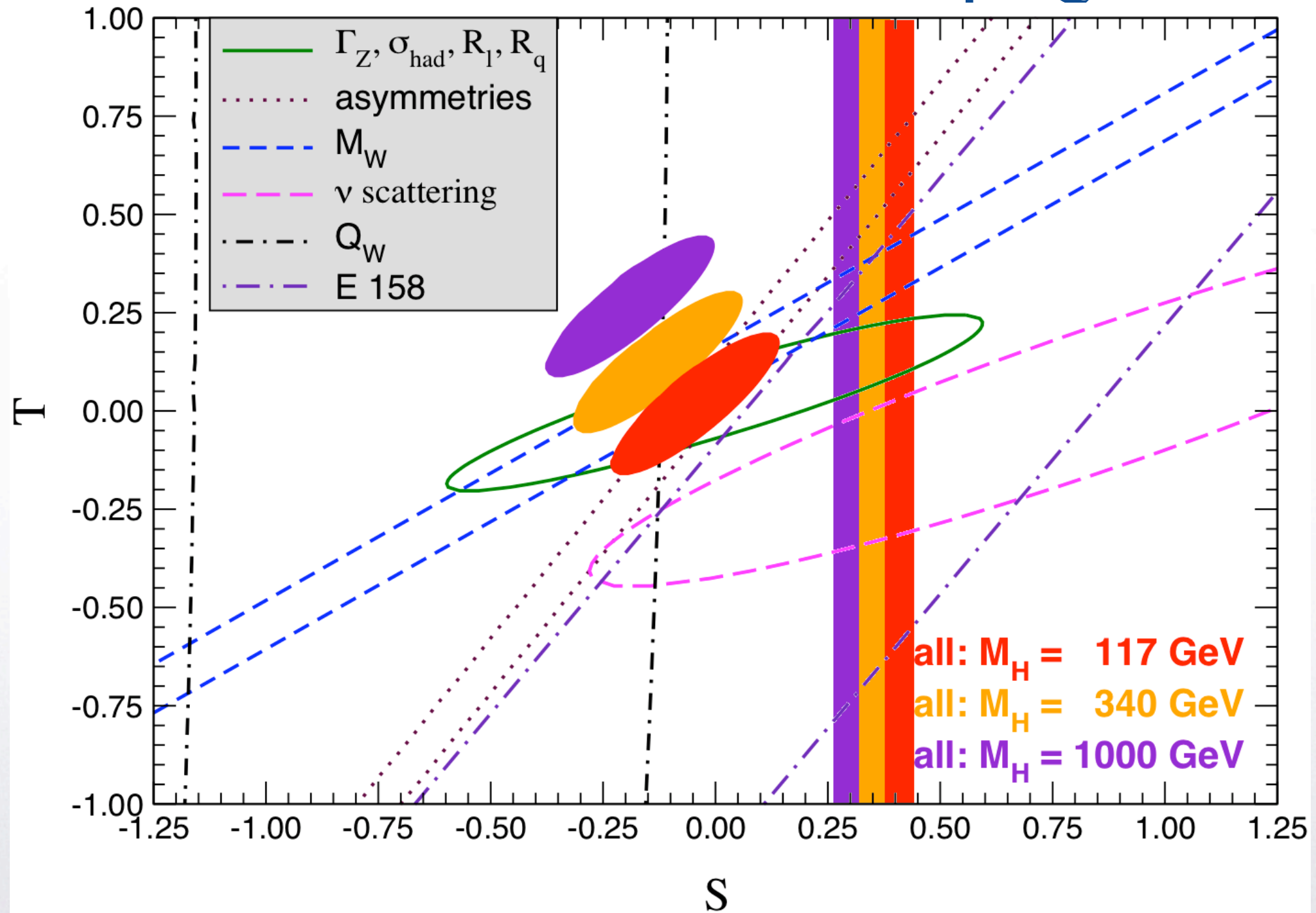


# Why did Technicolor fall out of favor?

- QCD-like strong interactions at the TeV scale can drive the Higgs mechanism, but face phenomenological challenges:
  - Either flavor changing neutral currents (FCNC) are too large or generated SM fermion masses are too small.
  - Precision EW oblique corrections (**S** parameter) in tension with experiment.
- **A resolution:** TeV strong interactions are not like QCD.
- **A problem:** How well do we really understand generic strongly interacting theories other than QCD?
- **A solution:** Lattice field theory is only now powerful enough to begin the study of strongly-coupled theories beyond QCD.



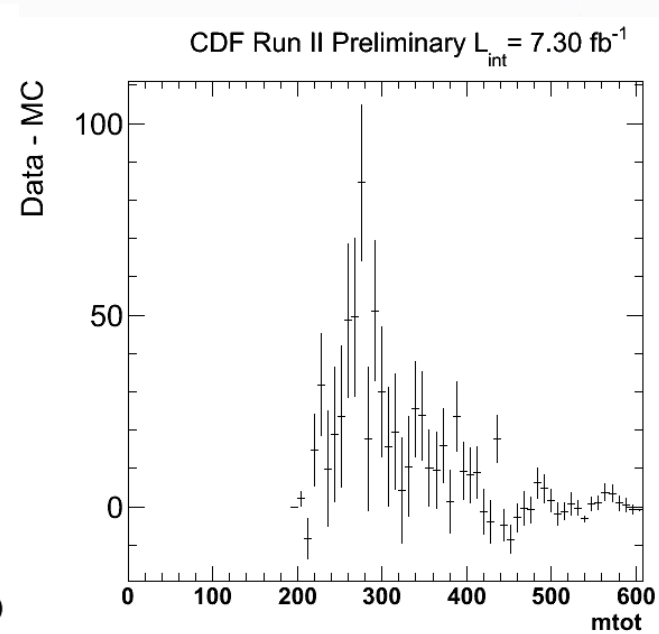
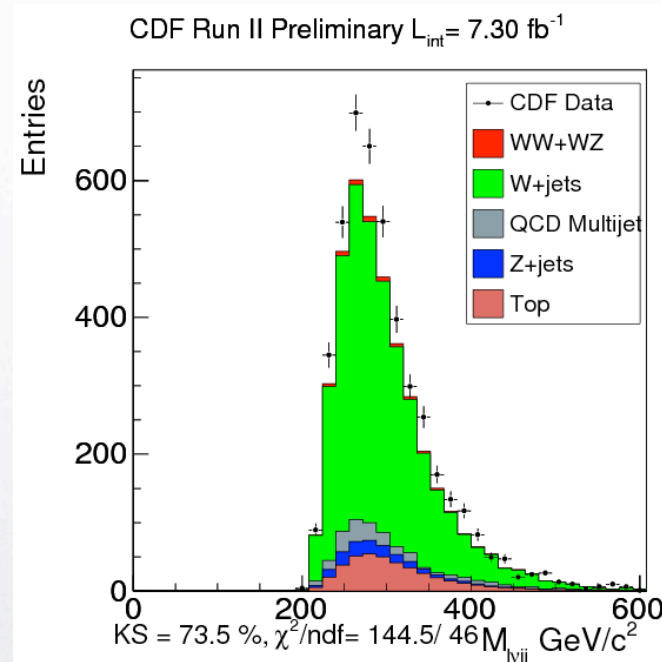
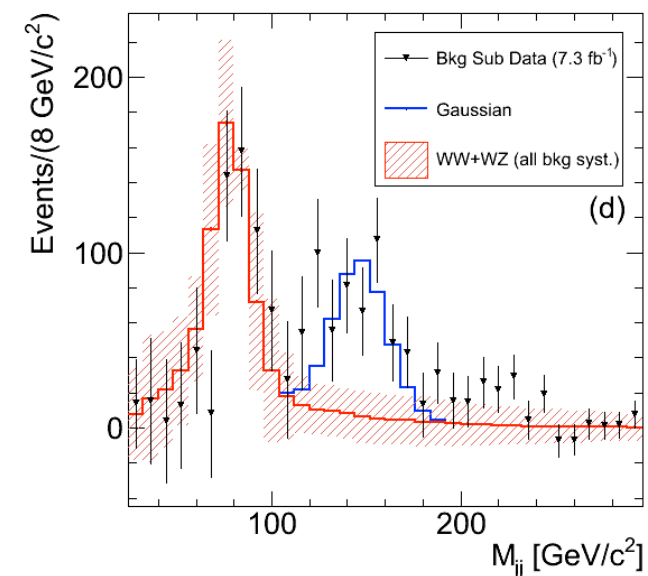
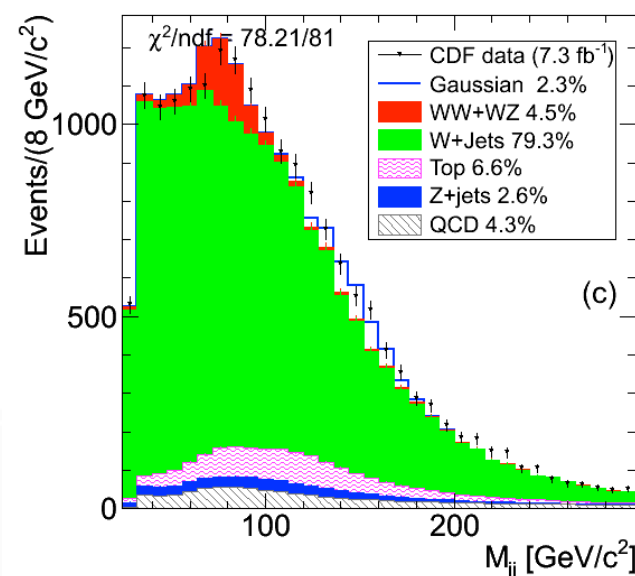
# S Parameter for Scaled-Up QCD





# Is there “evidence” for “Low-Scale Technicolor”?

- Recently, CDF found a bump in  $W+jj \rightarrow \ell \nu+jj$  in  $4.3 \text{ fb}^{-1}$  of data.  
[PRL 106, 171801 (2011)]
- Eichten, Lane, and Martin have interpreted this result in the Low Scale Technicolor model as  $\rho_T \rightarrow W+\pi_T \rightarrow W+jj$ .  
{arXiv:1104.0976 [hep-ph]}
- Last week in Blois, CDF released preliminary results of updated analysis with  $7.3 \text{ fb}^{-1}$  of data.
- [http://www-cdf.fnal.gov/physics/ewk/2011/wjj/7\\_3.html](http://www-cdf.fnal.gov/physics/ewk/2011/wjj/7_3.html)
- D0 responds by Friday. Will LHC respond this week in Perugia?





# How can the lattice address Technicolor?

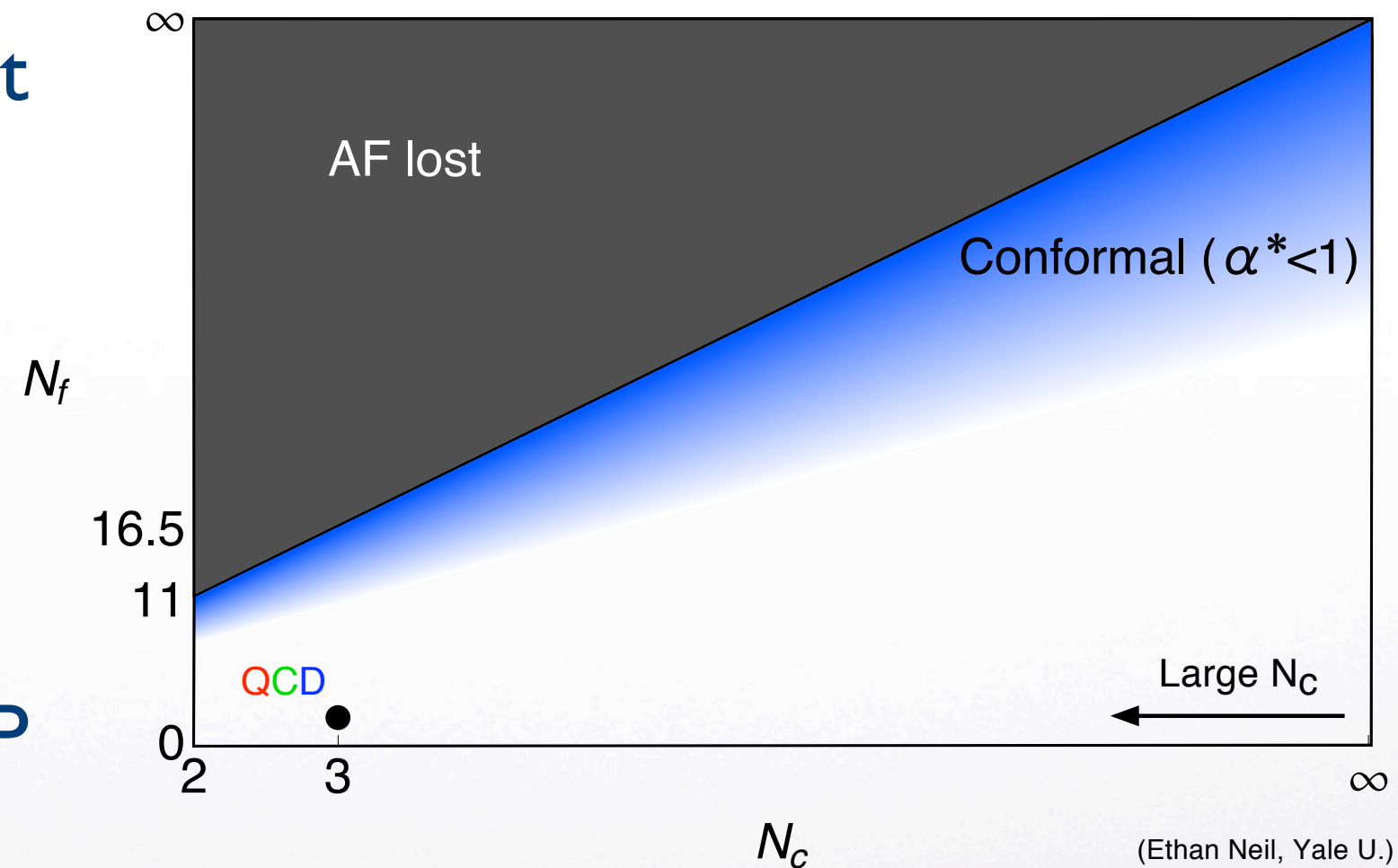
- Technicolor scenario has Higgs mechanism driven by TeV-scale strong interactions with spontaneous symmetry breaking (SSB) and Nambu-Goldstone (NG) bosons.
- QCD has these features and been studied on the lattice for decades, recently with much success.
- Other strongly-coupled gauge theories likely have these features, *i.e.* other flavors ( $N_f$ ), colors ( $N_c$ ), etc.
- Lattice studies can search for the right combination that enables Technicolor to satisfy phenomenological constraints.
- Unfortunately, other theories are usually computationally more expensive than QCD for calculation:  $\propto N_f^{3/2}, N_c^3, d(R)^3$





# Where to look for non-QCD theories?

- For  $N_f = 0-1$ , confinement but no NG bosons.
- For  $N_c = 2$ , enhanced chiral symmetry means special case: Pattern of symmetry breaking yet to be determined.
- Pert. theory indicates IRFP for  $N_f \lesssim 5.5 \cdot N_c$ .
- Phenomenological success of large  $N_c$  calculations suggest QCD-like theories for  $N_f = 2-3$  and  $N_c \geq 3$ .
- Simplest search strategy: start from QCD and increase  $N_f$ .

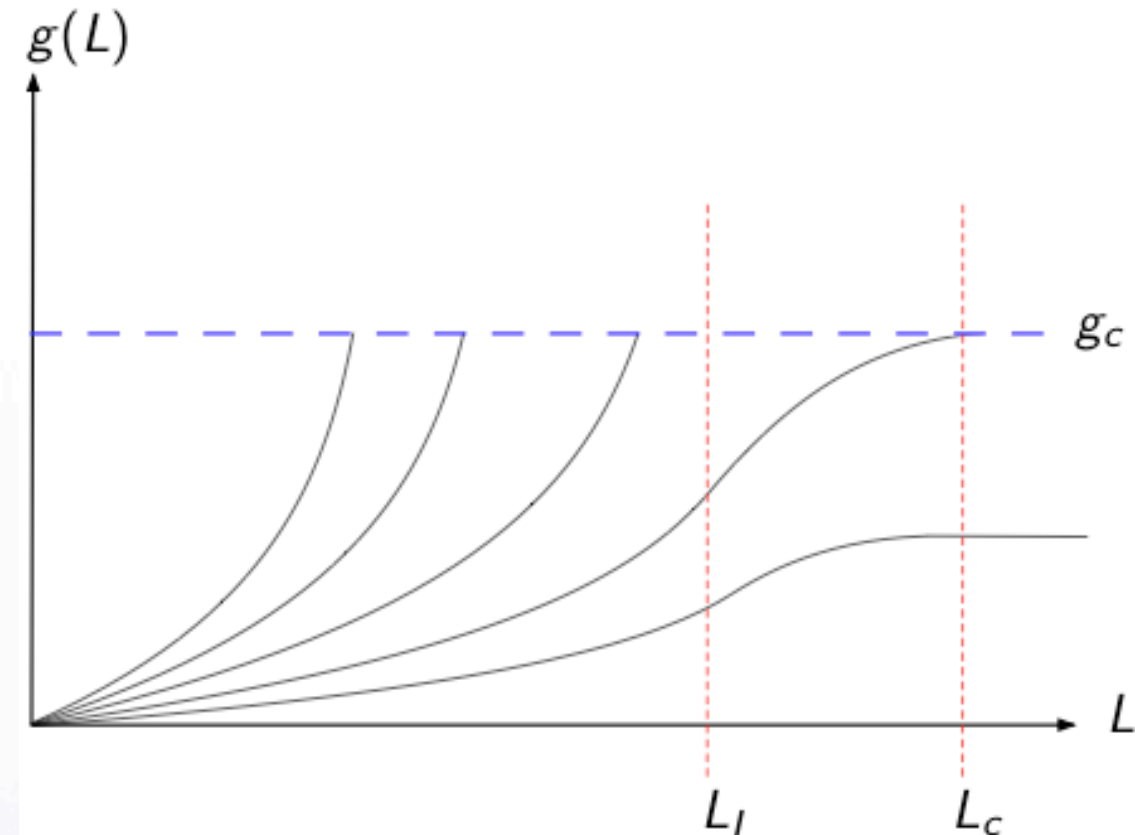


(Ethan Neil, Yale U.)



# Can the running coupling be our guide?

- In QCD,  $g(L)$  is asymptotically free and runs rapidly until SSB and confinement:  $g(L_c) = g_c$ .
- As  $N_f$  increases, the running slows down.
- For large  $N_f$ ,  $g(L)$  flows to  $g_*$  at IR fixed point (IRFP). No SSB, no Technicolor.
- Walking theories may exist nearby theories with strongly-coupled IRFP:  $g_* \simeq g_c$ .
- Unlike QCD, walking theories would have two dynamically generated scales:  $L_I$  and  $L_c$ , and in rare cases  $L_I \ll L_c$ .
- In Technicolor,  $L_I^{-1} = \Lambda_{\text{ETC}} \sim 1000 \text{ TeV}$  and  $L_c^{-1} = \Lambda_{\text{TC}} \sim 1 \text{ TeV}$ .
- How does walking help Technicolor's FCNC problem?







# Walking Dynamics

- The relevant scale for mass generation is  $\Lambda_{\text{ETC}}$ , so the relevant condensate is renormalized at that scale:  $\langle \bar{Q}Q \rangle$  at  $\Lambda_{\text{ETC}}$ .

$$\text{Masses: } \frac{(\bar{Q}Q)(\bar{q}q)}{\Lambda_{\text{ETC}}^2} \quad \text{FCNC's: } \frac{(\bar{q}q)(\bar{q}q)}{\Lambda_{\text{ETC}}^2} \quad \Lambda_{\text{ETC}} \gtrsim 1000 \text{ TeV}$$

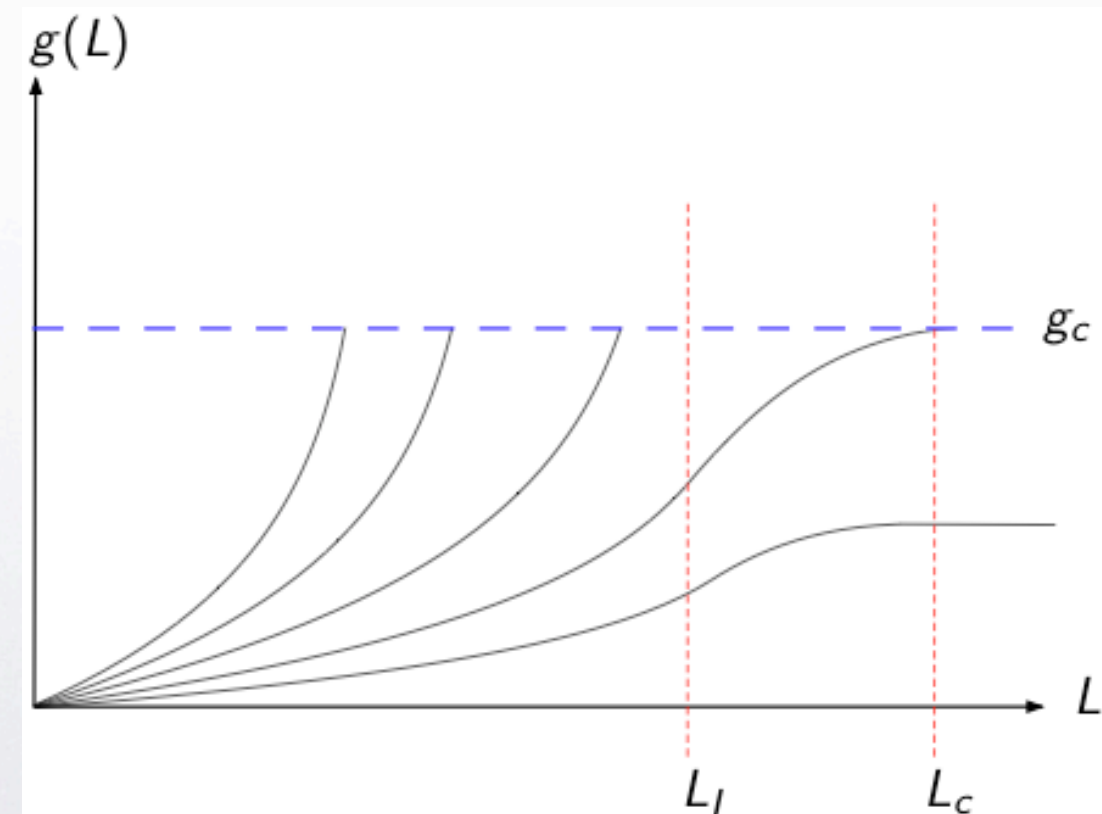
- The condensate is renormalized using the anomalous dimension  $\gamma(\mu)$ . In QCD-like theories,  $\gamma(\mu) \ll 1$  for  $\mu \gg \Lambda_{\text{TC}}$ . Leads to  $\log(\Lambda_{\text{ETC}} / \Lambda_{\text{TC}})$  enhancement.

$$\langle \bar{Q}Q \rangle_{\Lambda_{\text{ETC}}} = \langle \bar{Q}Q \rangle_{\Lambda_{\text{TC}}} \exp \left[ \int_{\Lambda_{\text{TC}}}^{\Lambda_{\text{ETC}}} \frac{\gamma(\mu)}{\mu} d\mu \right]$$

- Walking dynamics ( $\gamma \sim 1$ ) leads to power-enhanced condensates.

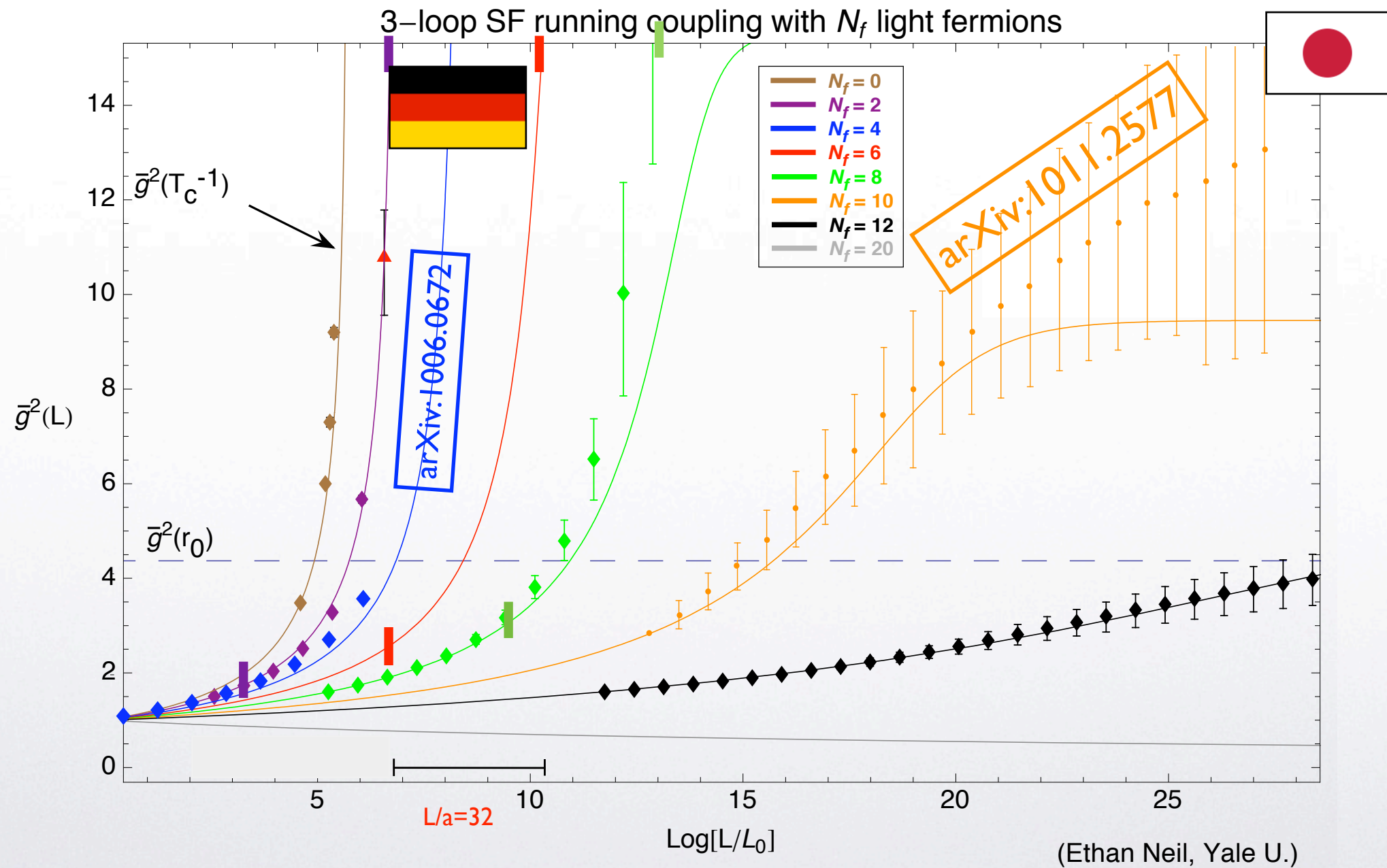
$$\frac{\langle \bar{Q}Q \rangle}{F_{\pi_T}^3} \sim \frac{\langle \bar{q}q \rangle}{f_\pi^3} \left( \frac{\Lambda_{\text{ETC}}}{\Lambda_{\text{TC}}} \right)^\gamma$$

- Now, a hierarchy of SM fermion masses can be generated while suppressing FCNC.





# Non-perturbative SF running coupling



- Results not yet confirmed in other non-pert. schemes.





# Lattice Strong Dynamics (LSD) Collaboration

*Michael Buchoff*  
*Michael Cheng*  
*Joe Wasem*  
*Pavlos Vranas*



James Osborn

*Ron Babich*  
*Rich Brower*  
*Saul Cohen*  
*Claudio Rebbi*  
*David Schaich*



Joe Kiskis

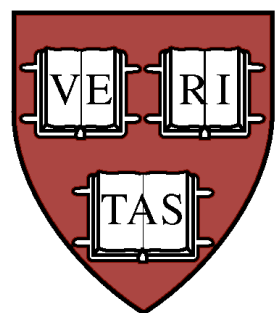
Tom Appelquist  
George Fleming  
*Meifeng Lin*  
Ethan Neil\*

Gennady Voronov



*Mike Clark*

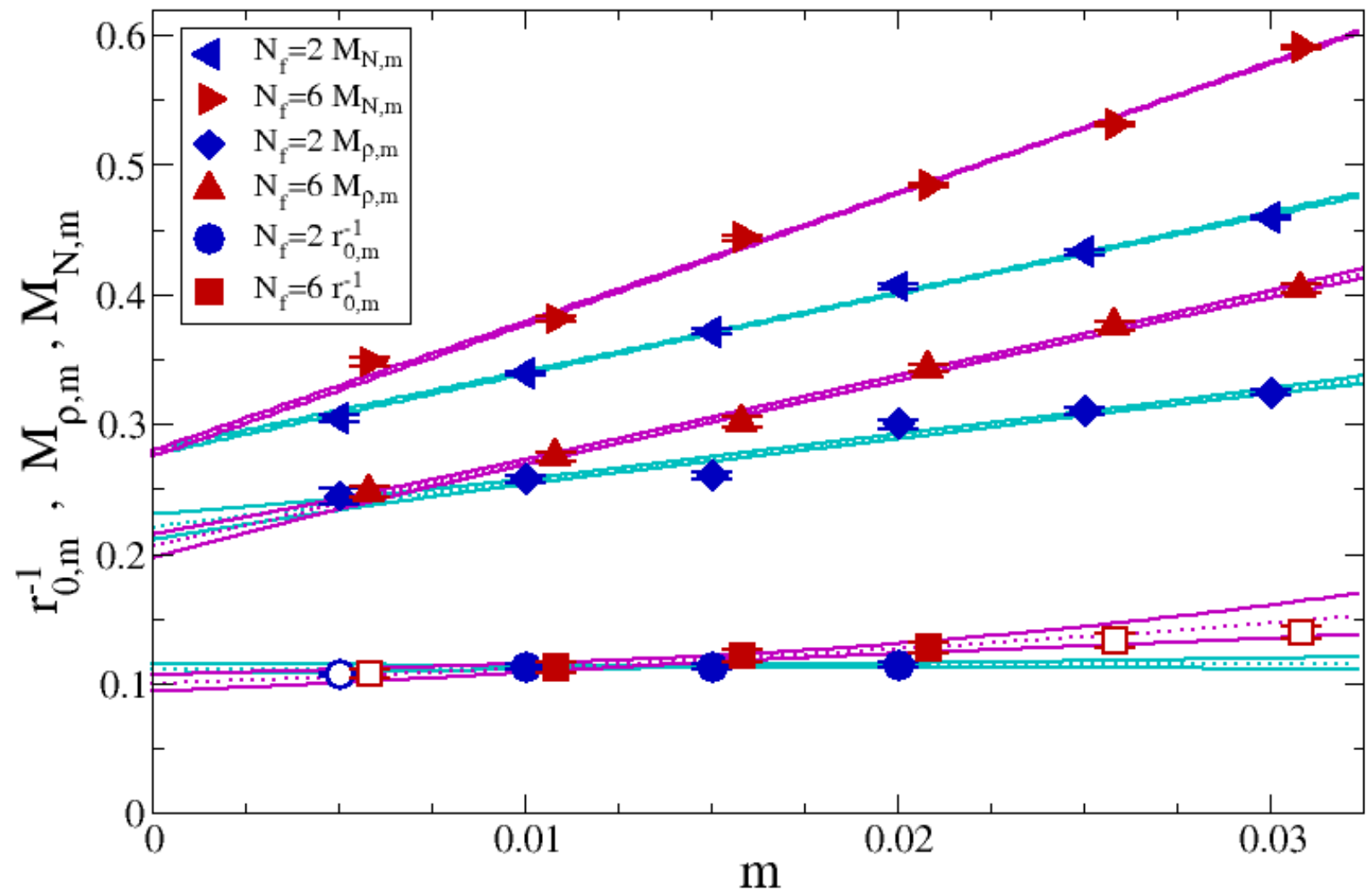
\*Recently joined Fermilab Theory Group.





## LSD: Comparing $N_f = 2$ and $N_f = 6$

- Why  $N_f = 6$ ? It's very unlikely to walk...
- On largest computers, calculations still limited to lattices where  $L/a \leq 64$ .
- A walking theory should be studied on lattices where  $L/a \sim 256-1024$ .
- Can precursors to walking be seen in slowly running theories?
- Lattice scales chosen to match confinement scale physics to  $\sim 10\%$ .







# LSD: Condensate Enhancement

- Tricky to compare scale dependent quantities in two different theories.

- Definition of Enhancement:

$$\left. \frac{\langle \bar{\psi}\psi \rangle^{(N_f)}}{\langle \bar{\psi}\psi \rangle^{(2)}} \right|_{5M_\rho} \equiv \mathcal{R}(5M_\rho) \approx \frac{\exp\left(\int_{\alpha(5M_\rho)}^{\alpha(M_\rho)} \frac{\gamma(\alpha)}{\pi\beta(\alpha)} \Big|_{N_f} d\alpha\right)}{\exp\left(\int_{\alpha(5M_\rho)}^{\alpha(M_\rho)} \frac{\gamma(\alpha)}{\pi\beta(\alpha)} \Big|_{N_f=2} d\alpha\right)}$$

- GMOR Ratios

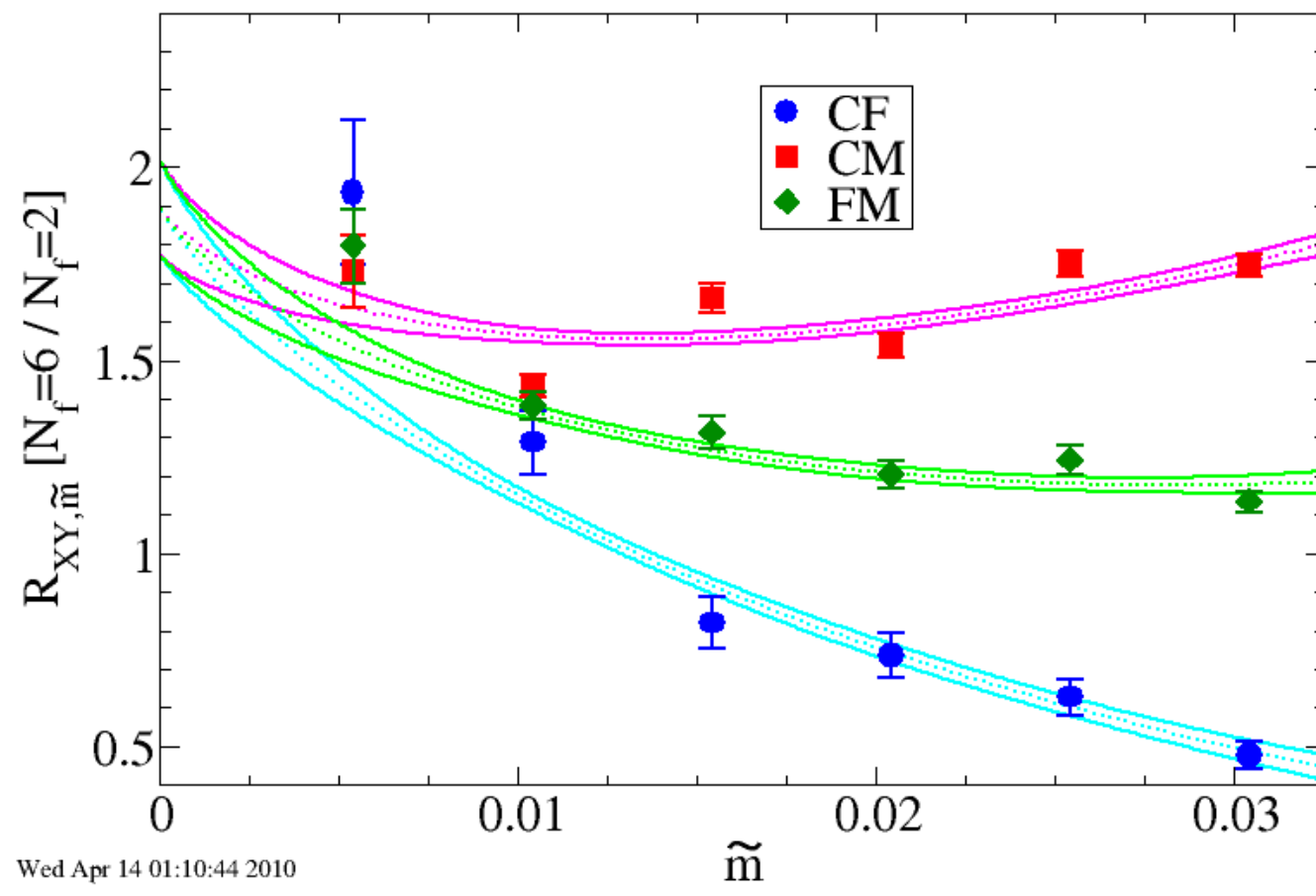
$$R = \frac{\overbrace{\langle \bar{\psi}\psi \rangle}^{\text{CF}}}{F_\pi^3} = \frac{\overbrace{M_\pi^3}^{\text{CM}}}{\sqrt{(2m)^3 \langle \bar{\psi}\psi \rangle}} = \frac{\overbrace{M_\pi^2}^{\text{FM}}}{2mF_\pi} \quad \text{as } m \rightarrow 0$$

- Chiral extrapolation

$$\mathcal{R}_{XY, \tilde{m}} = \frac{R^{(N_f)}}{R^{(2)}} [1 + \tilde{m} (\alpha_{XY10} + \alpha_{11} \log \tilde{m})], \quad \tilde{m} = \sqrt{m^{(N_f)} m^{(2)}}$$

- Perturbative estimates of enhancement:  $\mathcal{R}(5M_\rho) \sim 1.2-1.3$  (lat scheme)

- Enhancement bigger than expected. **Is this a precursor to walking?**



# LSD: Polarization Tensor for $S$ Parameter

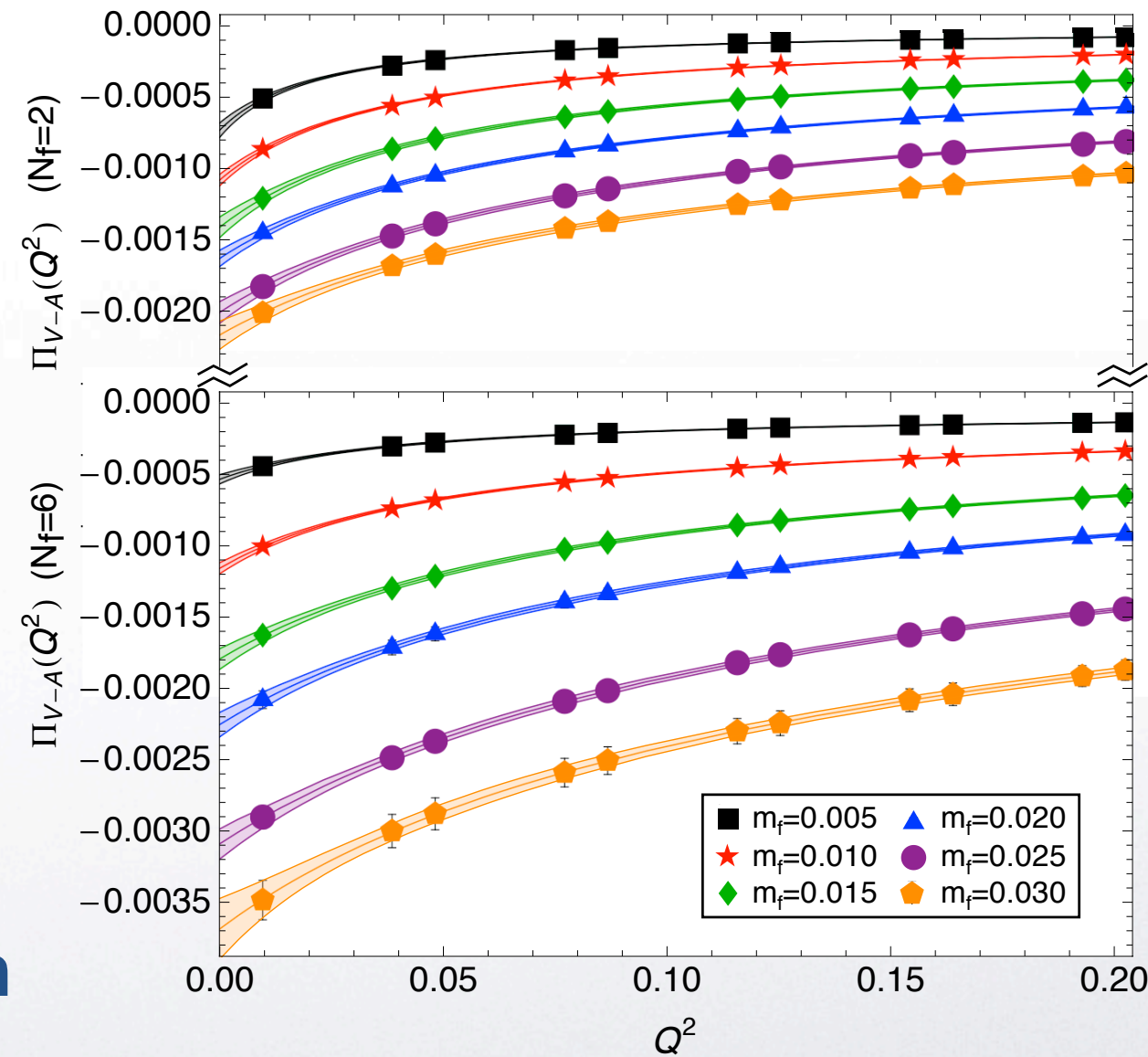
- $S$  for  $N_f / 2$  EW doublets

$$S = 4\pi \frac{N_f}{2} [\Pi'_{VV}(0) - \Pi'_{AA}(0)] + \Delta S_{SM}$$

$$= \frac{1}{3\pi} \int_0^\infty \frac{ds}{s} \left\{ \frac{N_f}{2} [R_V(s) - R_A(s)] - \frac{1}{4} \left[ 1 - \left( 1 - \frac{m_h^2}{s} \right)^3 \Theta(s - m_h^2) \right] \right\}$$

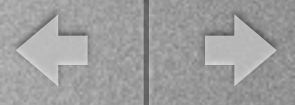
- Pade(1,2) fit of  $\Pi_{V-A}(Q^2)$  assumes  $Q^{-2}$  scaling as  $Q^2 \rightarrow \infty$  [1<sup>st</sup> WSR].

- Slope shows decreasing trend with decreasing mass for  $N_f = 6$ .



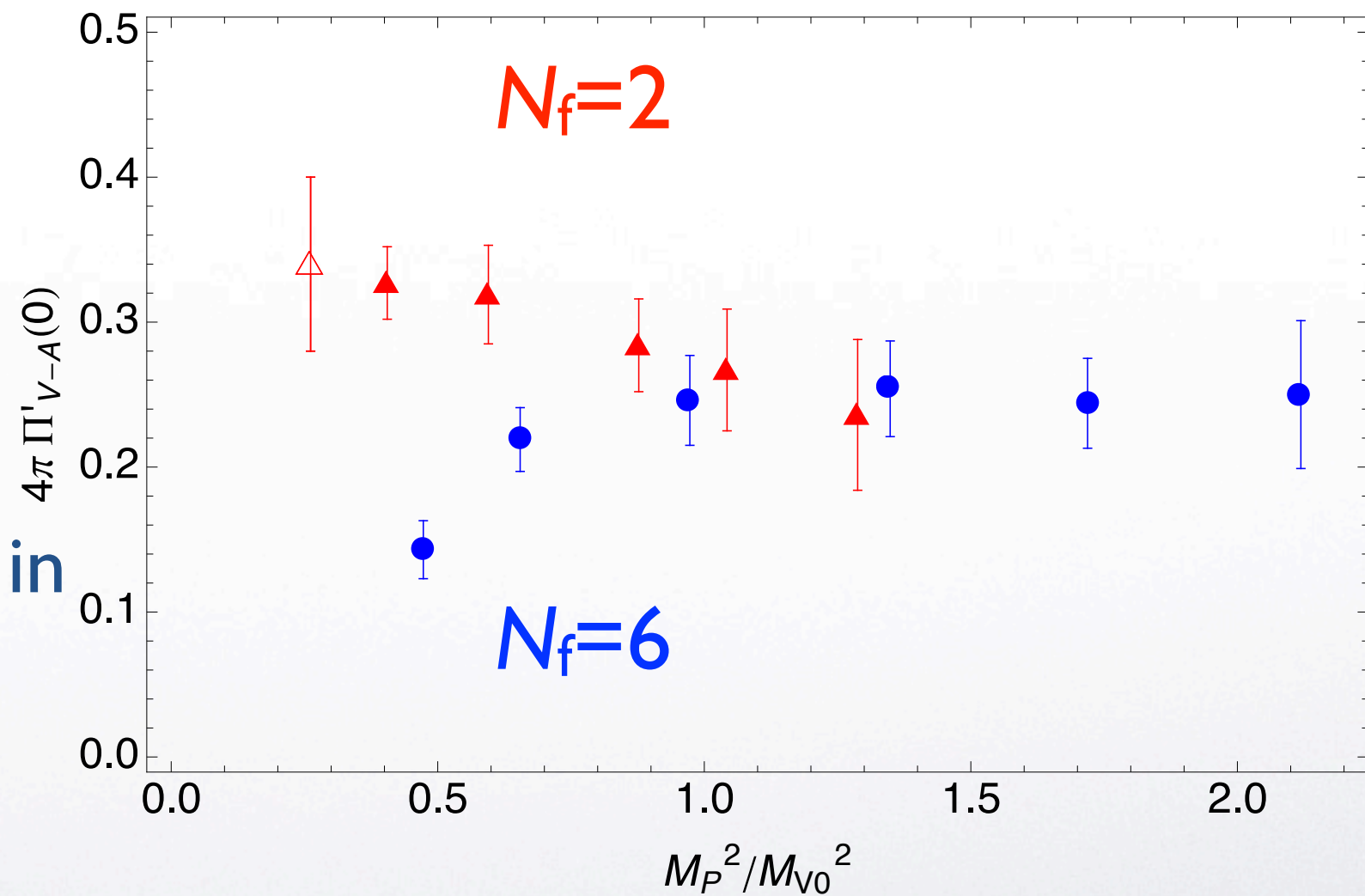
D. Schaich & E. Neil





# **LSD**: Flavor dependence of $\Pi'_{V-A}(0)$

- Polarization tensor computed for one EW doublet.
- Filled symbols  $M_P \cdot L \geq 4$ .
- Plot vs.  $M_P^2$  instead of  $m$ , in units of  $M_{V0}$ .
- $\Pi' \sim \log M_P^2$  as  $M_P^2 \rightarrow 0$ .
- Free field value for  $\Pi' = 1/2\pi = 0.159\dots$





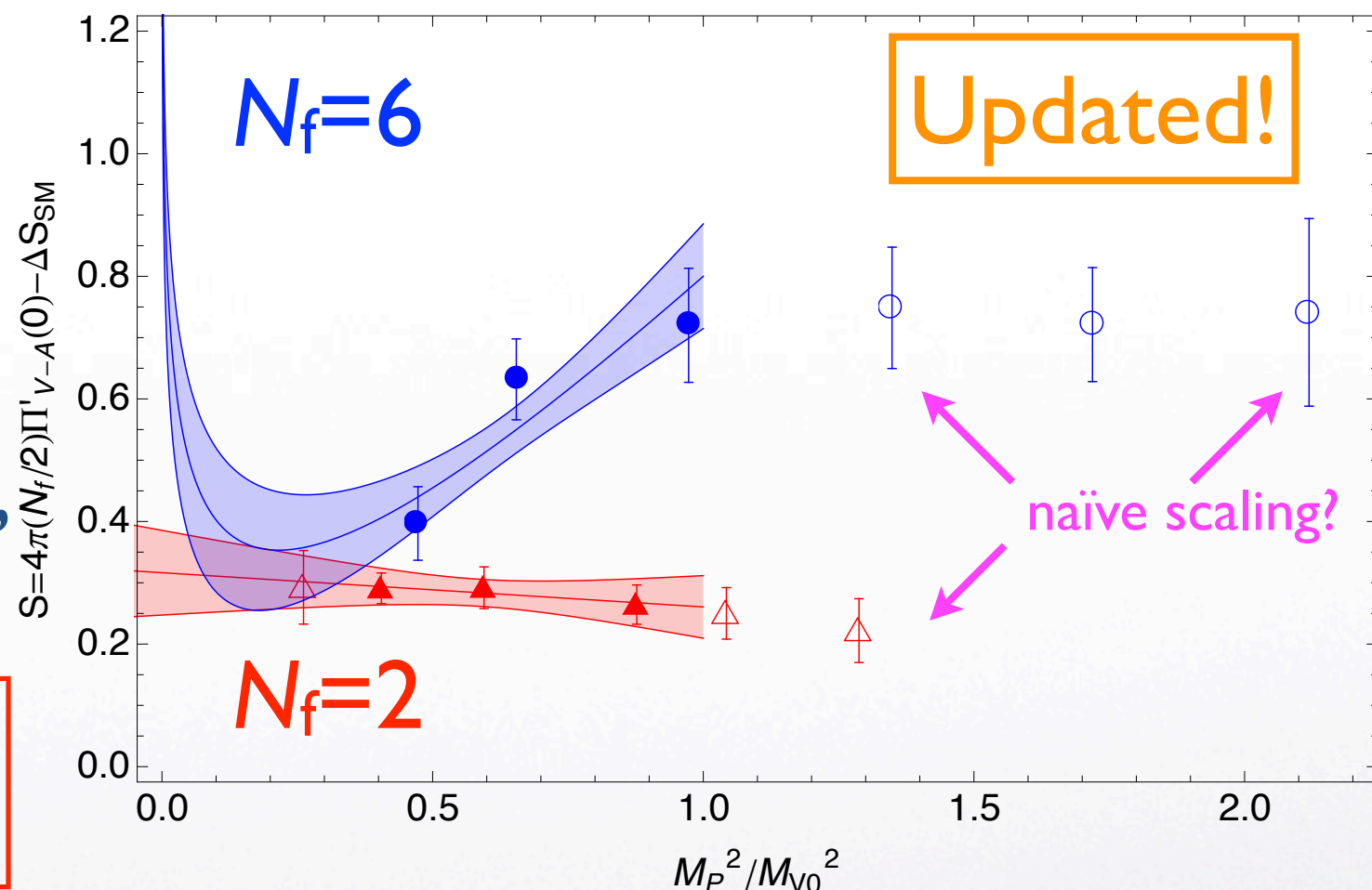
# Flavor dependence of $S$ Parameter

- Very naïve scaling for  $S$

$$S \propto \frac{N_f}{2} \frac{N_c}{3}$$

- Walking conjectured to reduce  $S$  by parity doubling, e.g. single-pole dominance:

$$S \sim 4\pi \left( \frac{N_f}{2} \right) \left[ \frac{F_V^2}{M_V^2} - \frac{F_A^2}{M_A^2} \right]$$

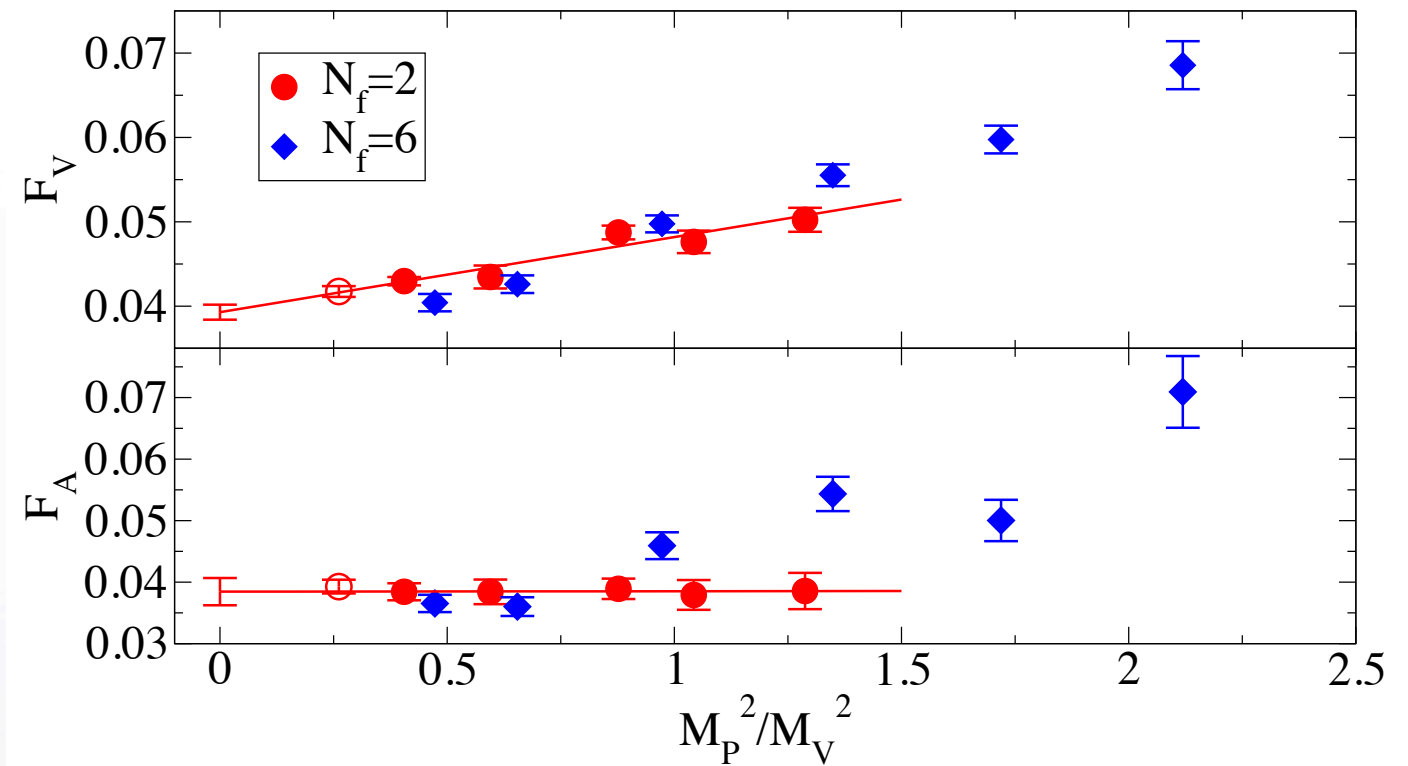
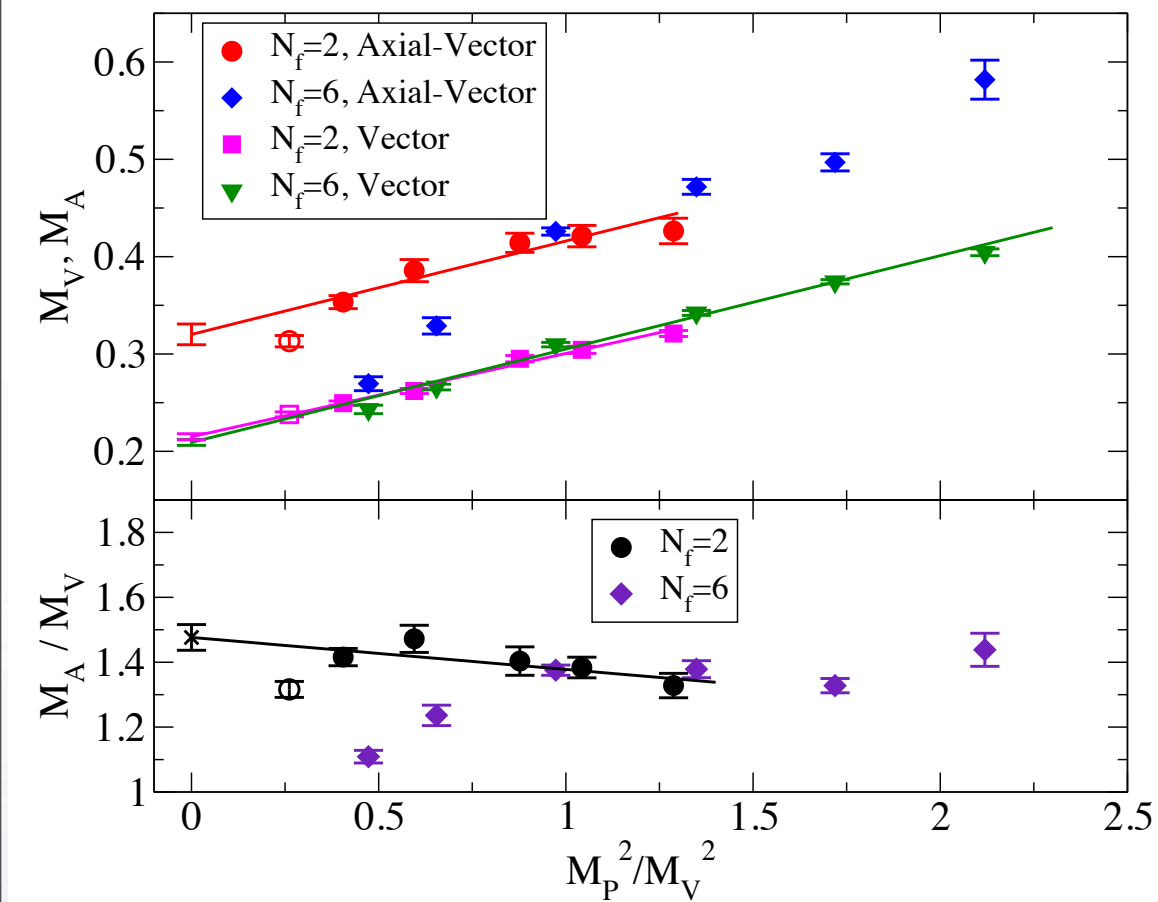


- After  $\Delta S_{SM}$  subtraction,  $S$  reduced relative to naïve scaling for  $N_f=6$ . **Is it a precursor of walking behavior?**

- n.b.  $S$  for  $N_f=6$  still log divergent until spectrum of PNCB's fixed.



# Flavor dependence of parity partners



- Note slope of  $M_V$  vs.  $M_P^2$  roughly independent of  $N_f$ , not true for  $M_V$  vs.  $m$ .

arXiv:1009.5967 [hep-ph]



# Conclusions

- For  $SU(3)$  running coupling studies for various  $N_f$  suggest a walking theory may exist for  $8 < N_f < 12$  flavors.
- Direct study of walking theories beyond the current capabilities of current computers, algorithms, ...
- Searches for precursors of walking behavior as the running slows with increasing  $N_f$  supports the vision that a walking theory can solve Technicolor's phenomenological problems.
- For  $N_f = 6$ , non-perturbative condensates are enhanced and  $S$  parameter reduced relative to perturbative expectations.
- Technicolor remains a viable option for physics at the TeV scale.

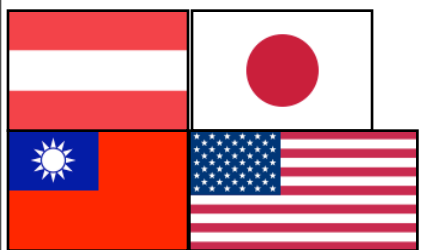




# Backup Slides



# A Dozen Lattice BSM Efforts Worldwide



Aoyama et al.



DeGrand et al.



Del Debbio et al.



Deuzeman et al.



Catteral et al.



**LSD**



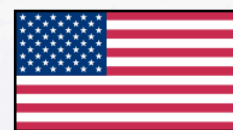
Hietanen et al.



A. Hasenfratz



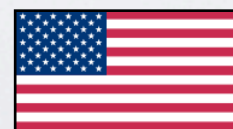
**LHC**



Jin-Mawhinney



Yamada et al.



Kogut-Sinclair







## Technicolor on the Lattice (II)

- Tools developed for study of Lattice QCD:
  - Non-perturbative Running Coupling
  - Non-perturbative Renormalization of Operators
  - Light Hadron and Glueball Spectrum
  - Chiral Observables (condensate, Dirac eigenvalues)
  - Thermodynamic Observables ( $T_c$ , EoS)
- Are tools optimized for QCD useful for non-QCD studies?
  - Exception: Monte Carlo methods using Wilsonian RG?
  - Can finite-size scaling methods be adapted from stat. mech.?



# Traveling Road Show

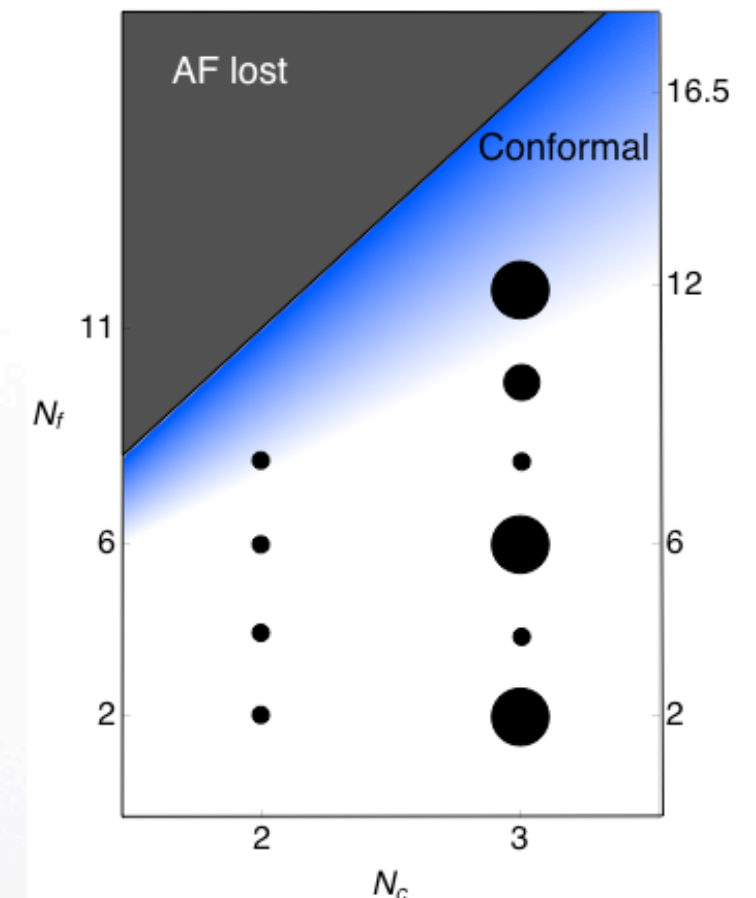
1. Lattice Gauge Theory for LHC Physics, Livermore, CA, May 2–3, 2008. <http://www.yale.edu/LSD/workshop08/>
2. XXVI International Symposium on Lattice Field Theory, Williamsburg, VA, July 14–19, 2008. <http://conferences.jlab.org/lattice2008/>
3. Workshop on Dynamical Electroweak Symmetry Breaking, Odense, Denmark, September 9–13, 2008. <http://hep.sdu.dk/dewsb/>
4. New frontiers in large N gauge theories, Seattle, WA, February 3–6, 2009. <http://www.int.washington.edu/PROGRAMS/09-4lw.html>
5. Large N@Swansea, Swansea, Wales UK, July 7–10, 2009. <http://www.ippp.dur.ac.uk/Workshops/09/largeN/>
6. XXVII International Symposium on Lattice Field Theory, Beijing, China, July 25–31, 2009. <http://rc hep.pku.edu.cn/workshop/lattice09/index.xml>
7. Les Houches Summer School, Session XCIII: Modern perspectives in lattice QCD: Quantum field theory and high performance computing, August 3–28, 2009. <http://giulio.tau.ac.il/~bqs/Houches2009/Houches0809.html>
8. Universe in a Box: LHC, Cosmology and Lattice Field Theory, Leiden, The Netherlands, August 24–28, 2009. <http://www.lorentzcenter.nl/lc/web/2009/366/info.php3?wsid=366>
9. 2nd Workshop on Lattice Gauge Theory for LHC Physics, November 6–7, 2009, Boston, MA. <http://www.yale.edu/LSD/workshop/>
10. Origin of Mass 2010, CP<sup>3</sup>-Origins, Odense, Denmark, May 3–7, 2010. <http://cp3-origins.dk/events/meetings/mass-2010>
11. Aspen Center for Physics, Aspen, CO, May 24 – Jun 11, 2010. <http://www.aspenphys.org/documents/program/summer2010.html>
12. XXVIII International Symposium on Lattice Field Theory, Sardinia, Italy, Jun 14–19, 2010. <http://www.infn.it/Lattice2010/>
13. Future Directions in Lattice Gauge Theory, CERN, Jul 19 – Aug 13, 2010. <http://indico.cern.ch/conferenceDisplay.py?confId=64133>
14. Workshop on Strongly-Interacting Field Theories, Jena, Germany, Sep 29 – Oct 1, 2010. <http://www.tpi.uni-jena.de/workshop2010>
15. Lattice Simulations for Physics Beyond the Standard Model, Hsinchu, Taiwan, Nov 12, 2010. <http://phys.cts.ntu.edu.tw/workshop/2010/991112LHC/?fclass=1>





# LSD Program Overview

- $SU(2)$  and  $SU(3)$  gauge theories with  $N_f$  domain wall fundamental fermions.
- Initial focus on  $SU(3)$ : code readiness and QCD experience.
- Preparing  $SU(2)$  code for production.
- Majority of flops so far spent on  $SU(3)$  with  $N_f=2,6,10$ .
- Exploration of IR: QCD-like, conformal or “walking”.
- Phenomenology:  $S$  parameter, condensate enhancement.
- One PRL, recent preprint: [arXiv:1009.5967 \[hep-ph\]](https://arxiv.org/abs/1009.5967)





# Flavor dependence of NLO ChiPT

$$M_\pi^2 = 2mB \left\{ 1 + \frac{2mB}{(4\pi F)^2} \left[ 2\alpha_8 - \alpha_5 + N_f (2\alpha_6 - \alpha_4) + \frac{1}{N_f} \log \frac{2mB}{(4\pi F)^2} \right] \right\}$$

$$F_\pi = F \left\{ 1 + \frac{2mB}{(4\pi F)^2} \left[ \frac{1}{2} (\alpha_5 + N_f \alpha_4) - \frac{N_f}{2} \log \frac{2mB}{(4\pi F)^2} \right] \right\}$$

$$\langle \bar{q}q \rangle = F^2 B \left\{ 1 + \frac{2mB}{(4\pi F)^2} \left[ \frac{1}{2} (2\alpha_8 + \eta_2) + 2N_f \alpha_6 - \frac{N_f^2 - 1}{N_f} \log \frac{2mB}{(4\pi F)^2} \right] \right\}$$

- The leading non-analytic terms are enhanced in the condensate and  $f_\pi$  but suppressed in  $(M_\pi)^2$ .
- The  $\alpha_i \sim \mathcal{O}(1)$  low energy constants.
- $\eta_2 \sim \mathcal{O}(a^{-2})$  contact term: UV-sensitive slope for condensate.





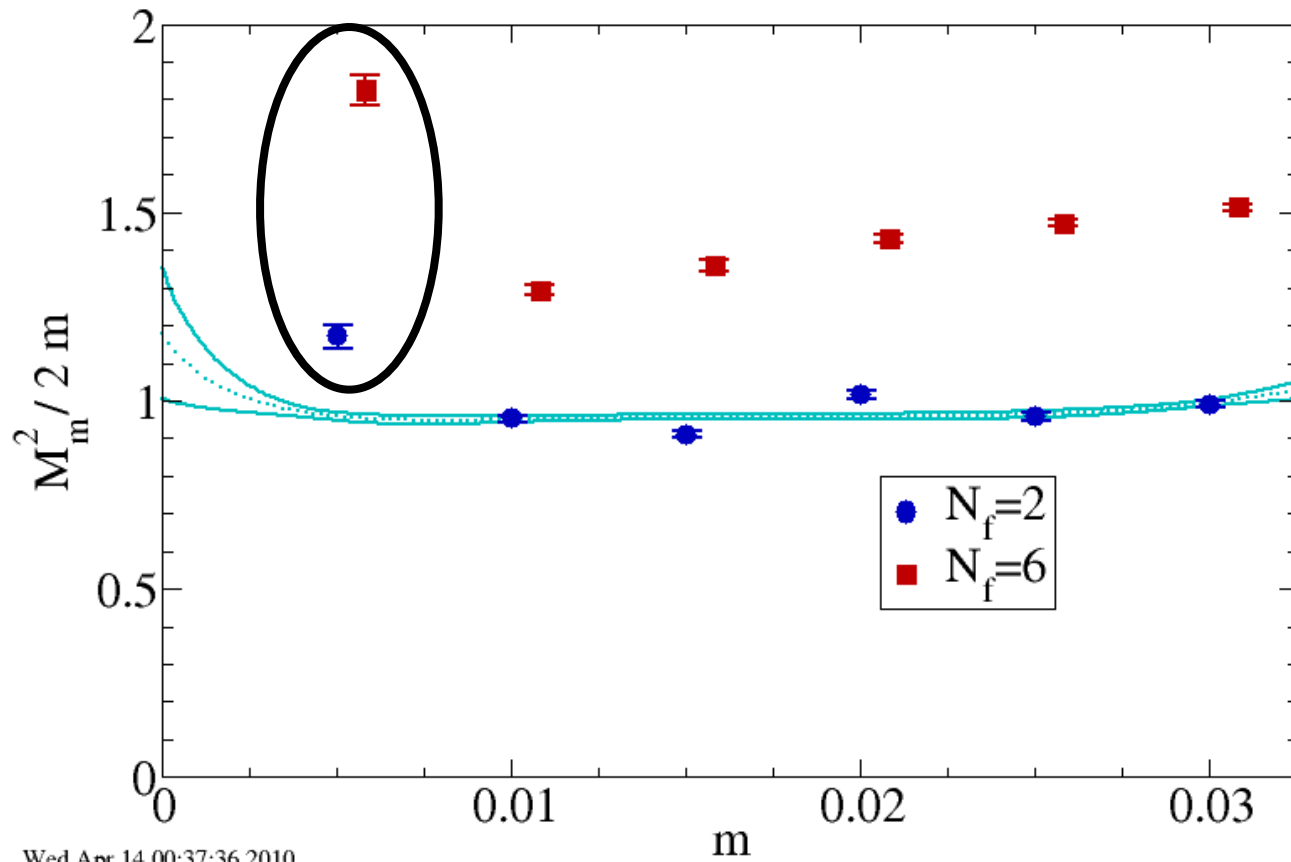
# Non-analytic flavor factors in NNLO ChiPT

	$m \log(m)$	$m^2 \log^2(m)$
$M_{\pi^2}$	$N_f^{-1}$	$-3/8 N_f^2 + 1/2 - 9/2 N_f^{-2}$
$F_{\pi}$	$-1/2 N_f$	$3/16 N_f^2 + 1/2$
$\langle qq \rangle$	$-N_f + N_f^{-1}$	$3/2 - 3/2 N_f^{-2}$

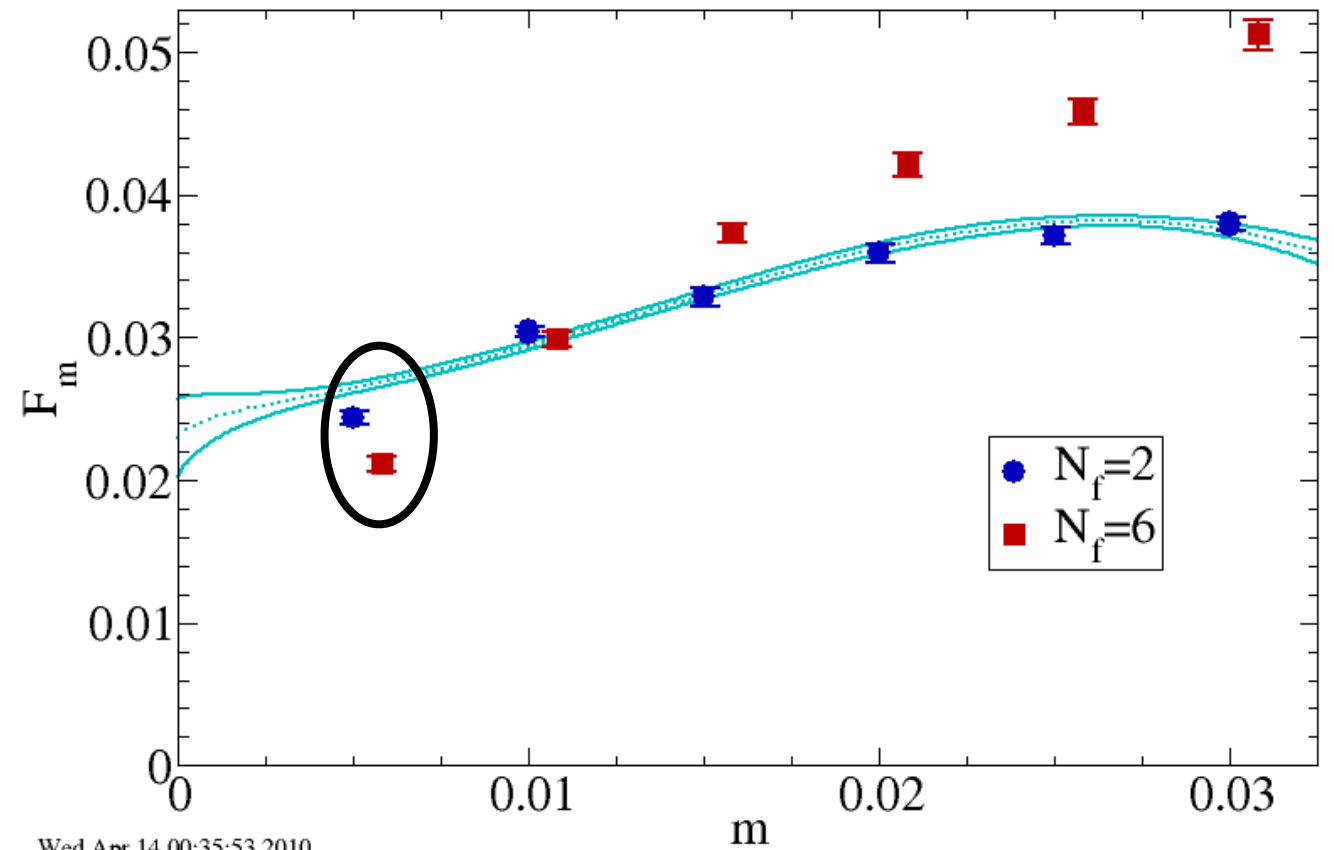
- J. Bijnens and J. Lu, JHEP11(2009)116 [arXiv:0910.5424]
- Small NLO coeff for  $M_{\pi^2}$  is not generic and doesn't persist to higher orders.
- Can NNLO formulae help us extrapolate  $N_f \gg 2$  results?



# Preliminary: Basic Chiral Observables



Wed Apr 14 00:37:36 2010



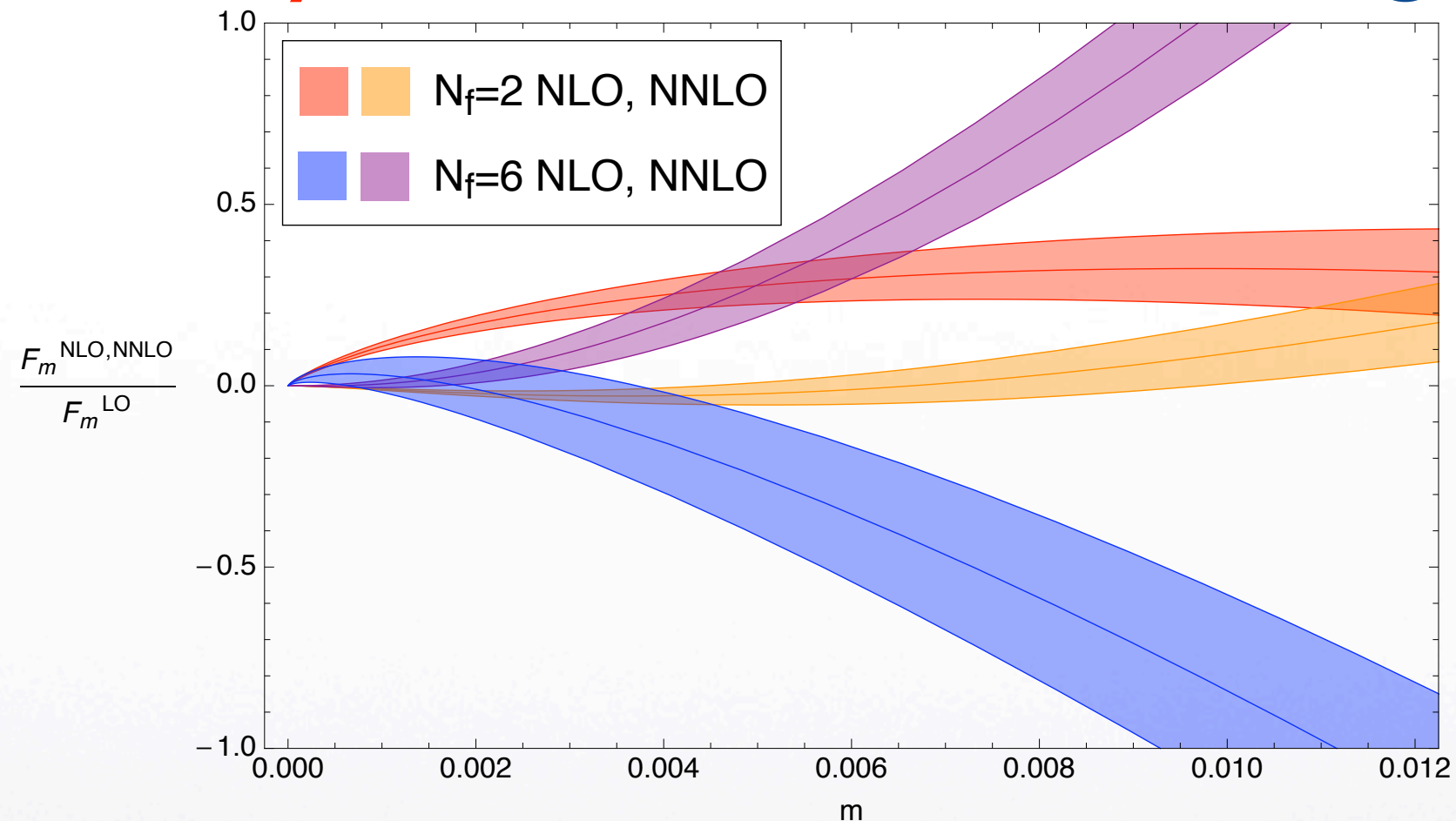
Wed Apr 14 00:35:53 2010

- NNLO ChiPT fits work fine for  $N_f=2$ .
- NNLO expression for general  $N_f$  recently derived by Bijmans and Lu [[JHEP11\(2009\)116](#)].





# Preliminary: $\chi$ PT Radius of Convergence



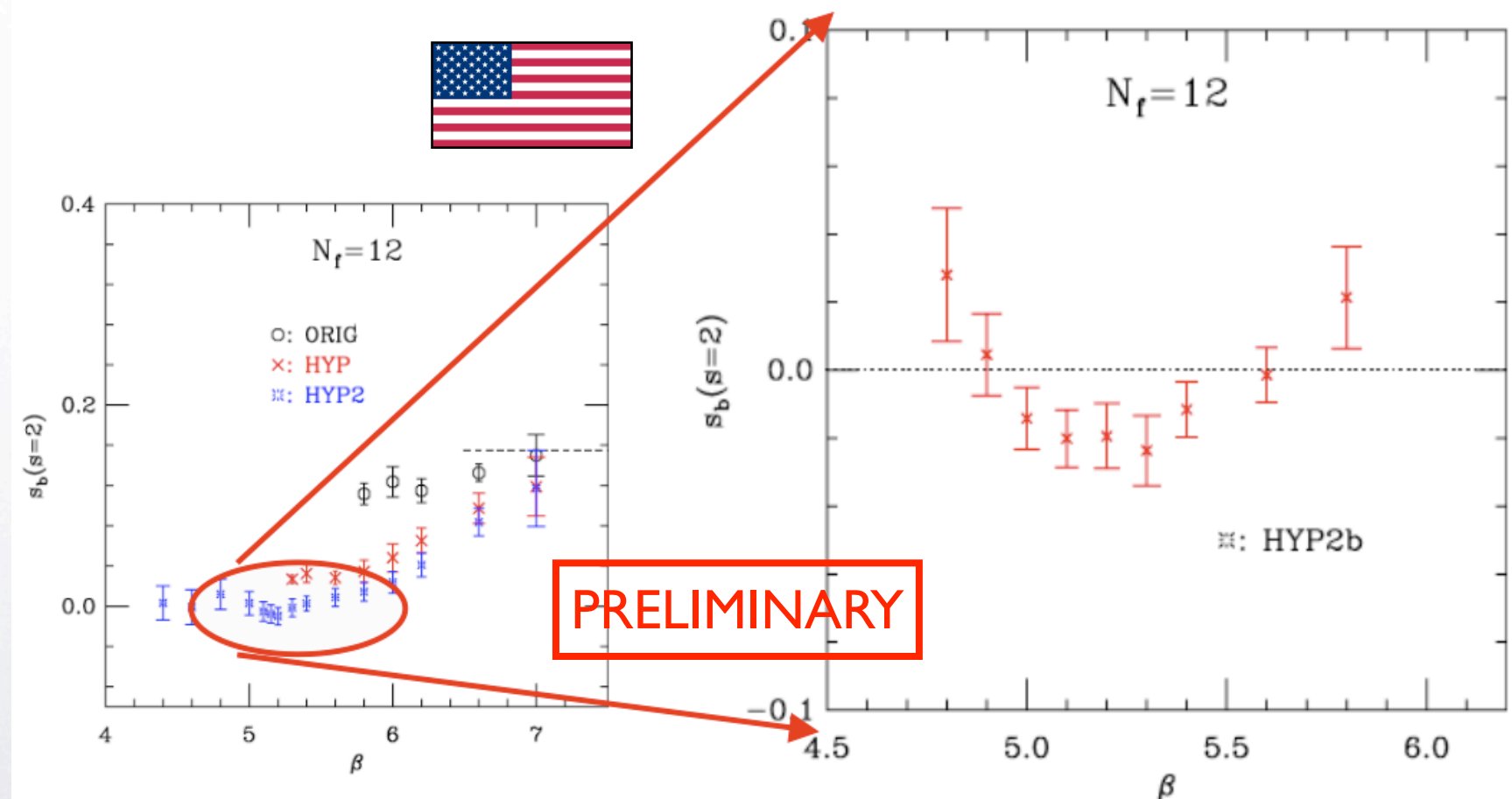
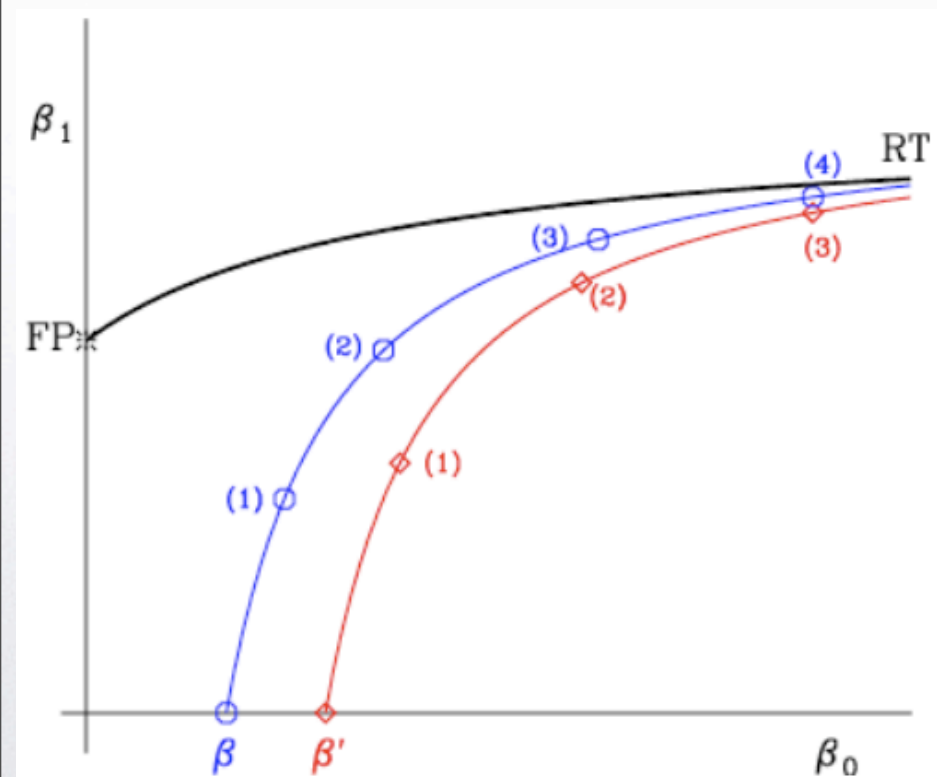
- Smaller quark masses needed for reliable NNLO extrapolation for  $N_f > 2$  [E.T. Neil *et al.*, PoS(CD09)088].
- On  $32^3 \times 64$ ,  $m \cong 0.01$ :  $M_\pi \cdot L \sim 4$  and  $F_\pi \cdot L \sim 1$ .  $48^3 \times 64$  lattices needed to reach smaller quark masses.



# Running Couplings in Other NP Schemes

- Monte Carlo Renormalization Group (MCRG) 2-Lattice Method  
Anna Hasenfratz

$$s_b(\beta) = \beta - \beta' , \quad s_b(\beta^*) = 0$$







# Twisted Polyakov Loop Scheme

SU(3) Nf=12 case in Twisted Polyakov loop scheme

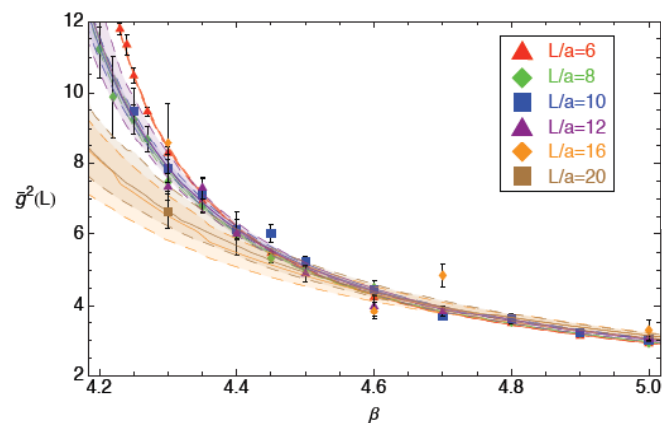
Lattice size

$s = 1 : L = 4, 6, 8, 10$   
 $s = 1.5 : L = 6, 9, 12, 15$

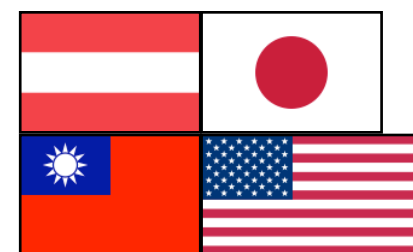
parameter  $4.0 < \beta < 20$

statistics (2% error)  
100,000 trj.

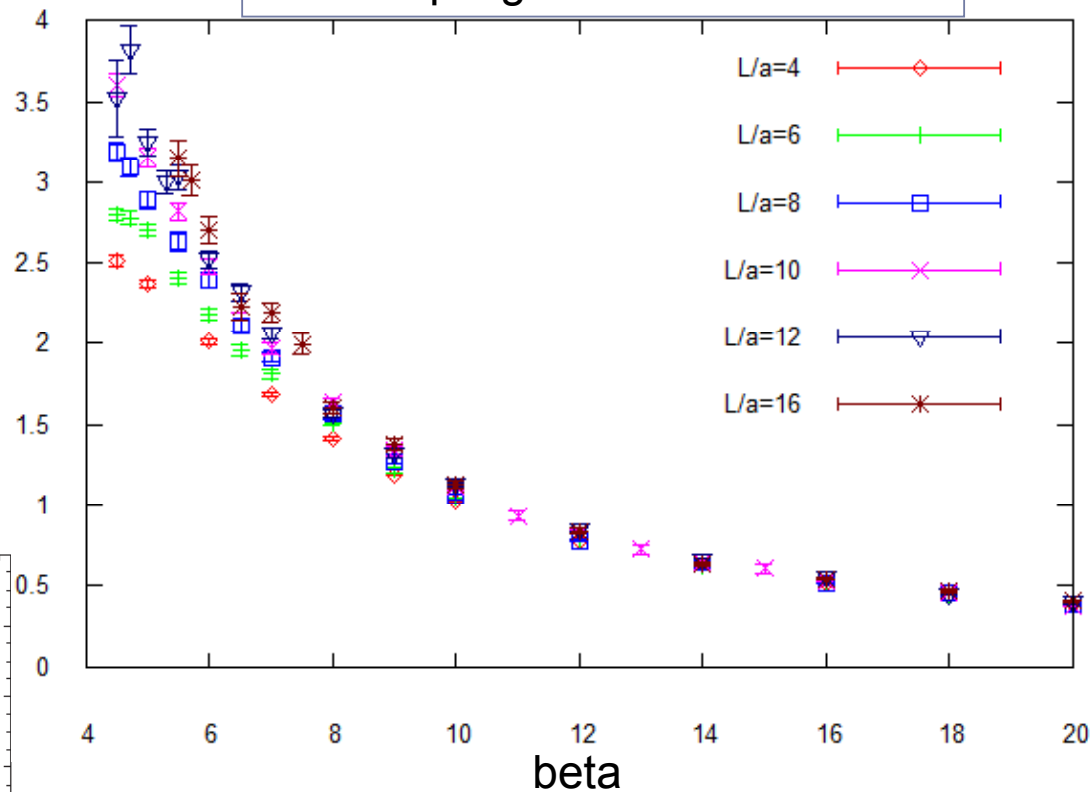
cf: Appelquist et.al.



- Hybrid Monte Carlo algorithm (exact algorithm)
- staggered fermion (massless 4N flavor)



TPL coupling for each lattice size



Different behavior with SF scheme

➔ Continuum extrapolation is important

Talk by E. Itou  
Hsinchu, Taiwan  
Nov. 12, 2010