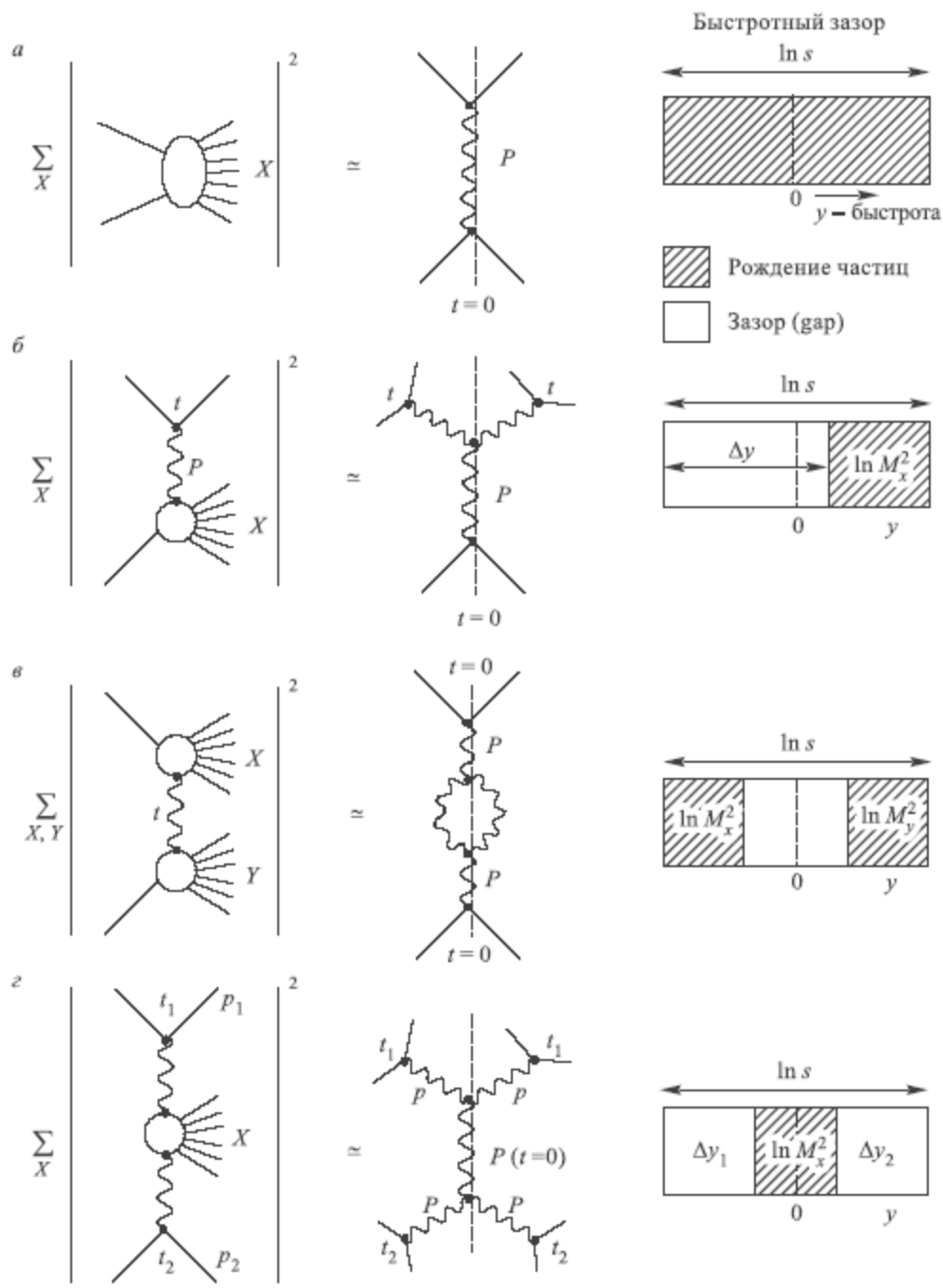


“Blois” in Vietnam:

**Lessons from the first measurements
of elastic and total cross sections at
the LHC by TOTEM**

L. Jenkovszky and D. Lontkovskiy
(Kiev: jenk@bitp.kiev.ua)

EDS, Quy Nhon, Dec. 2011



$$\sigma_t(s) = \frac{4\pi}{s} \text{Im}A(s, t=0); \quad \frac{d\sigma}{dt} = \frac{\pi}{s^2} |A(s, t)|^2; \quad n(s);$$

$$\sigma_{el} = \int_{t_{min} \approx -s/2 \approx \infty}^{t_{thr.} \approx 0} \frac{d\sigma}{dt}; \quad \sigma_{in} = \sigma_t - \sigma_{el}; \quad B(s, t) = \frac{d}{dt} \ln\left(\frac{d\sigma}{dt}\right);$$

(and ratios: $\sigma/B, \dots$).

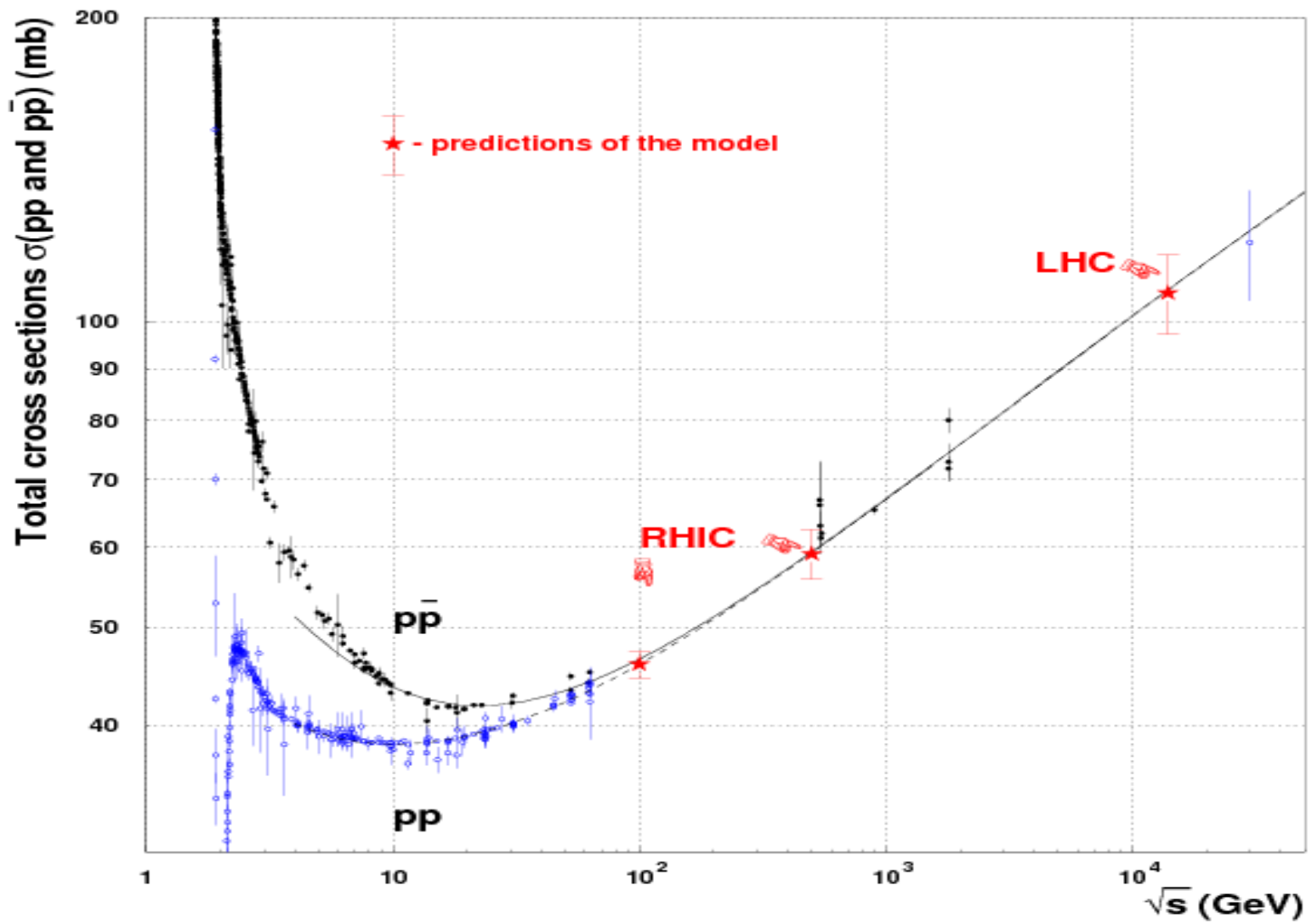
$$A_{pp}^{p\bar{p}}(s, t) = P(s, t) \pm O(s, t) + f(s, t) \pm \omega(s, t) \rightarrow_{LHC} \approx P(s, t) \pm O(s, t),$$

where P, O, f, ω are the Pomeron, odderon and non-leading Reggeon contributions.

The variety of languages results in a Babylonian confusion

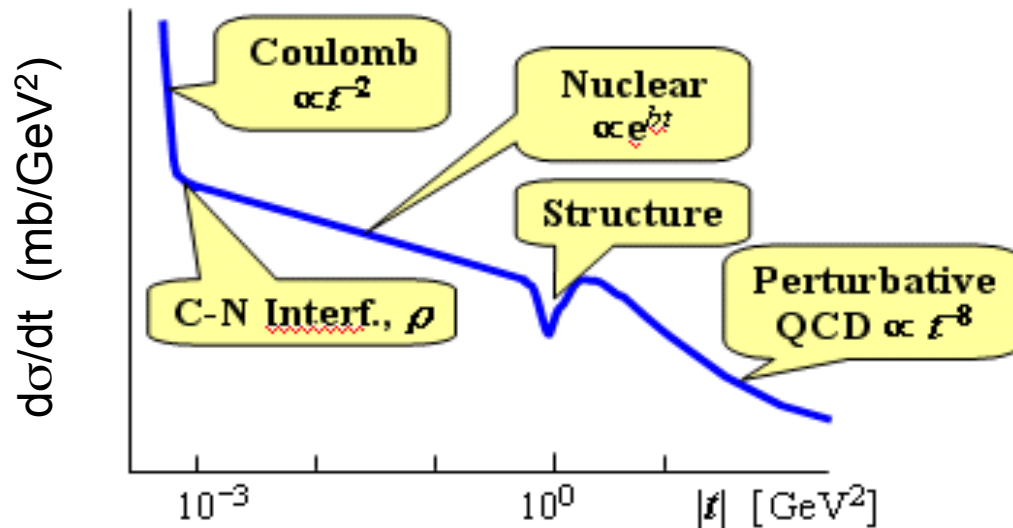
| $\alpha(0) \setminus C$ | + | - |
|-------------------------|----------|----------------------------|
| 1 | P | O |
| 1/2 | f | ω |

Pomeron exchange is synonym of Diffraction!



Elastic Scattering (generalities & details)

$\sqrt{s} = 14$ TeV prediction of BSW model



momentum transfer $-t \sim (p\theta)^2$
 θ = beam scattering angle
 p = beam momentum

$$\rho = \frac{\text{Re}(f_{el}(t))}{\text{Im}(f_{el}(t))}\bigg|_{t \rightarrow 0}$$

$$\left. \frac{dN}{dt} \right|_{t=CNI} = L\pi |f_C + f_N|^2 \approx L\pi \left| -\frac{2\alpha_{EM}}{|t|} + \frac{\sigma_{tot}}{4\pi} (i + \rho) e^{-\frac{b|t|}{2}} \right|^2$$

L , σ_{tot} , b , and ρ
 from FIT in CNI
 region (UA4)

CNI region: $|f_C| \sim |f_N| \rightarrow$ @ LHC: $-t \sim 6.5 \cdot 10^{-4} \text{ GeV}^2$; $\theta_{min} \sim 3.4 \text{ } \mu\text{rad}$
 ($\theta_{min} \sim 120 \text{ } \mu\text{rad}$ @ SPS)

Basic ingredients in any model-building; no theory:

1. **Undisputable:** the Pomeron is supercritical, $\alpha(0) > 1$.

Question: do we need also a “hard” component in the (universal) Pomeron?

2. Input (“Born term) and unitarization (e.g. “Regge-eikonal). Problems:

a) $B_2 = B_1/2$? b) More dips, at higher $|t|$ are not seen.

2. Where (e.g. in t) is the transition between “soft” (exponential) and “hard” power behaviour of the differential cross section (with TOTEM’s rich?)

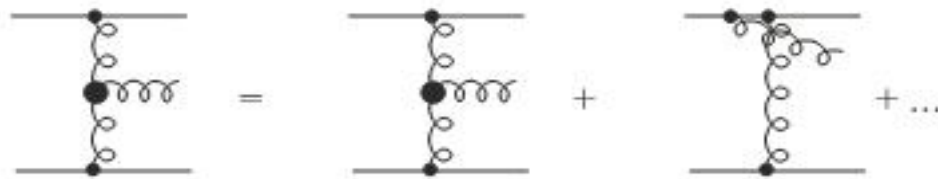
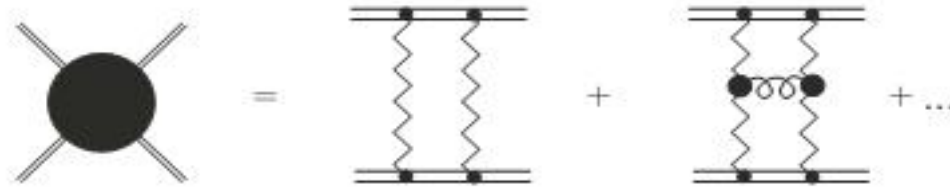
4. Geometrical models of the matter distribution (black disc or ring, Chou-Yang);

4. Is an odd-C (asymptotic!) contribution inevitable? I think so! Is the odderon part of diffraction (this is a lexical problem);

5. Spin in high-energy pp scattering

“THEORY”:

R. Fiore, L.L. Jenkovszky, E.A. Kuraev, A.I. Lengyel, *Predictions for high-energy pp and $\bar{p}p$ scattering from a finite sum of gluon ladders*, Phys. Rev. D81, #5 (2010) 056005; arXiv0911.2094/hep-ph



$$\sigma_t^{(P)}(s) = \sum_{i=0}^N f_i \theta(s - s_0^i) \theta(s_0^{i+1} - s), \quad (1)$$

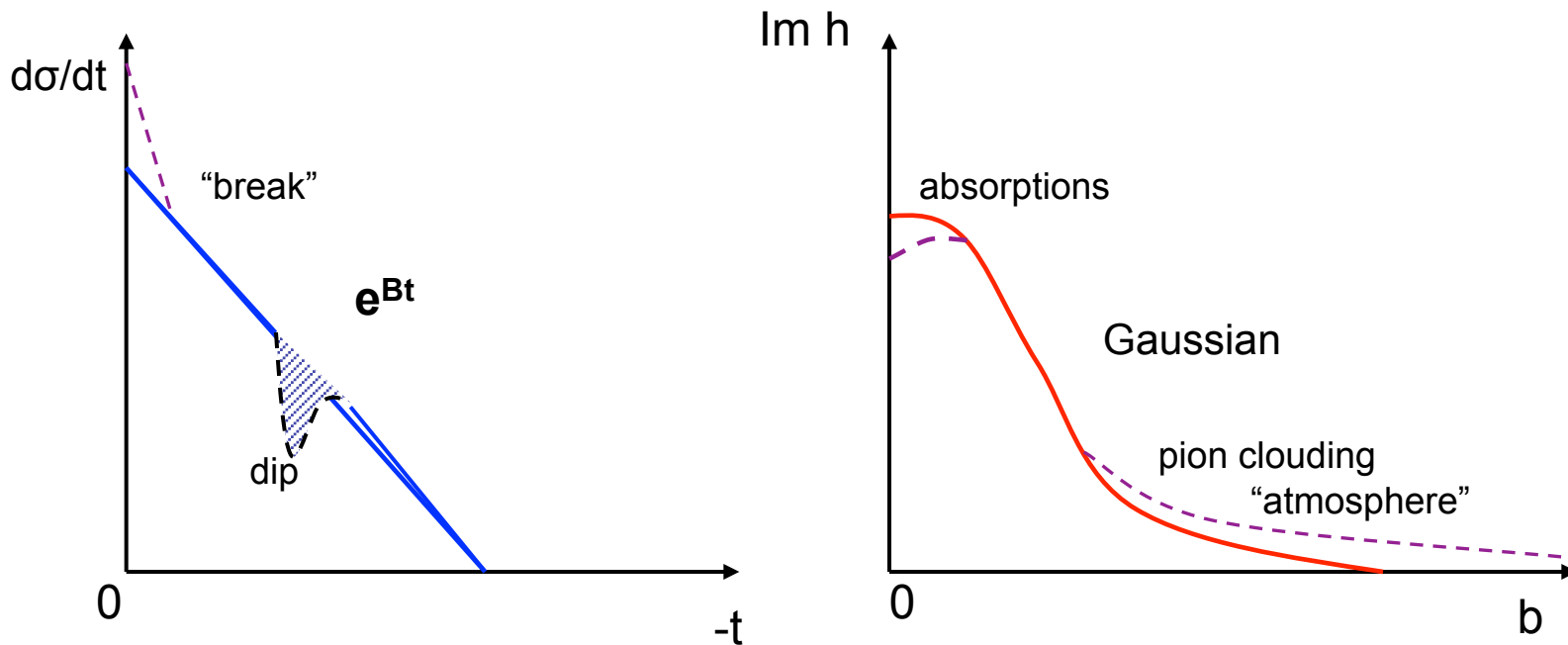
where

$$f_i = \sum_{j=0}^i a_{ij} L^j, \quad (2)$$

Geometrical scaling (GS), saturation and unitarity

1. On-shell (hadronic) reactions ($s, t, Q^2=m^2$);

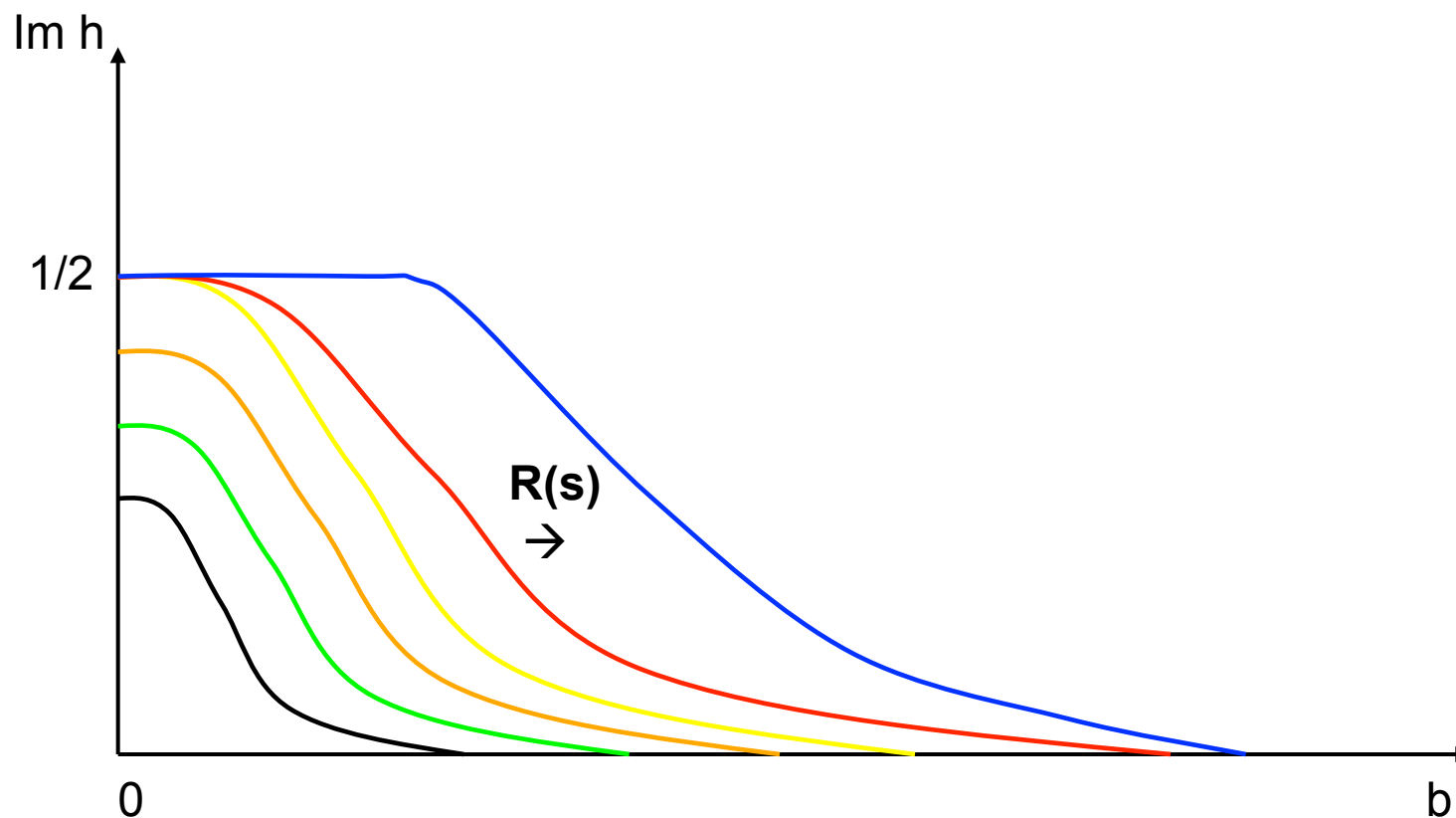
$t \leftrightarrow b$ transformation: $h(s, b) = \int_0^\infty d\sqrt{-t}\sqrt{-t}A(s, t)$
and dictionary:



Предел черного диска, $\text{Im } h=1/2$? Нет угрозы!

П. Дегрола, Л.Л. Енковский, Б.В. Струминский, ЯФ, EPJ (1999).

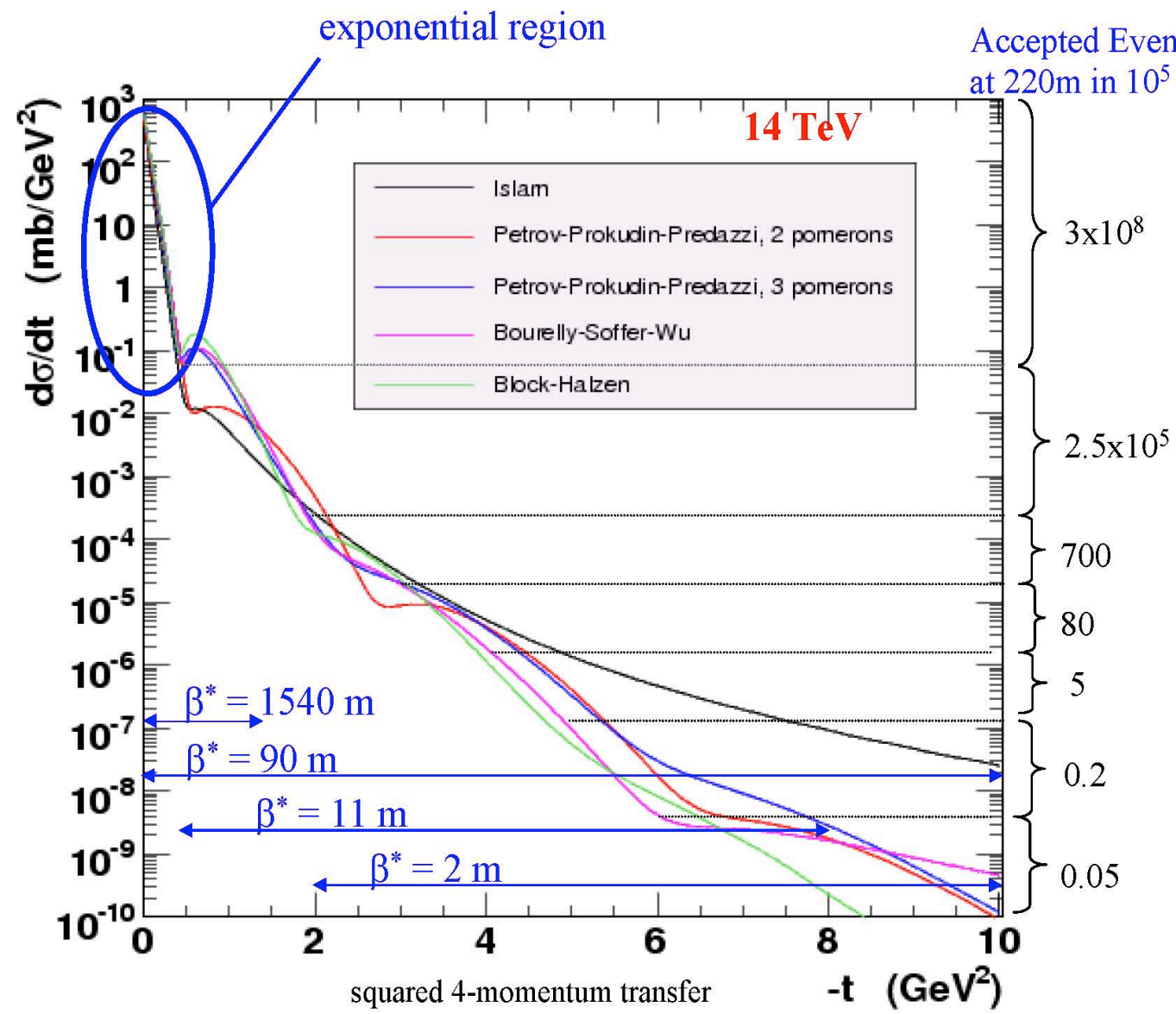
См. также спор Трошина и Тюриня с Влоком и Halzenom (arXiv: 21.11.2011)



Saturation of the Black Disc Limit?

$ImH(s, b) = |h(s, b)|^2 + G_{in}(s, b)$, (h is associated with the "opacity), Here from: $0 \leq |h(s, b)|^2 \leq \Im h(s, b) \leq 1$. The Black Disc Limit (BDL) corresponds to $\Im h(s, b) = 1/2$, provided $h(s, b) = i(1 - \exp[i\omega(s, b)])/2$, with an imaginary eikonal $\omega(s, b) = i\Omega(s, b)$.

There is an alternative solution, that with the "minus" sign in $h(s, b) = [1 \pm \sqrt{1 - 4G_{in}(s, b)}]/2$, giving (S. Troshin and N. Tyurin (Protvino)): $h(s, b) = \Im u(s, b) / [1 - iu(s, b)]$,





TOTEM 2011-01
22 June 2011

CERN-PH-EP-2011-101
26 June 2011

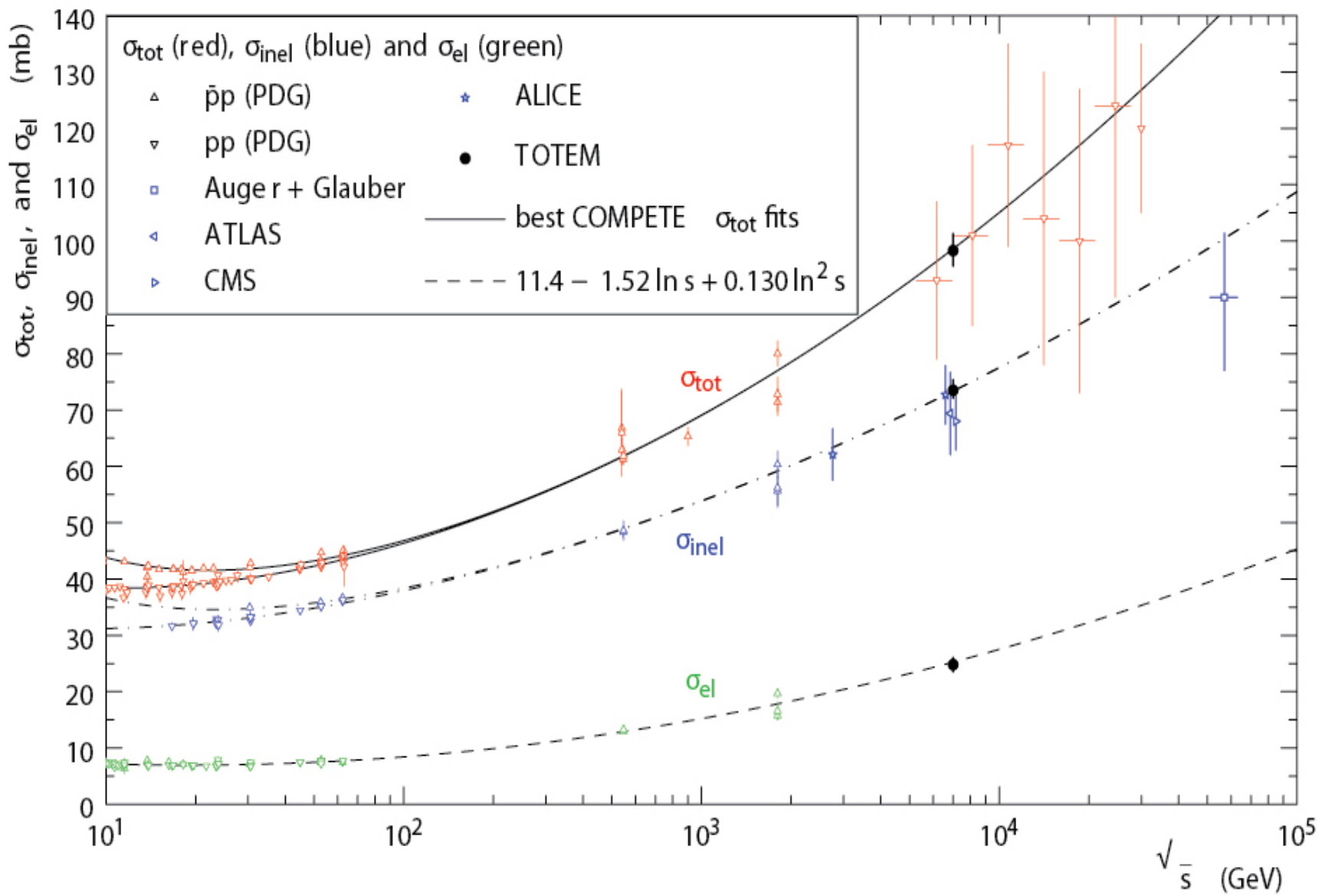
Elastic pp Scattering at the LHC at $\sqrt{s} = 7$ TeV.

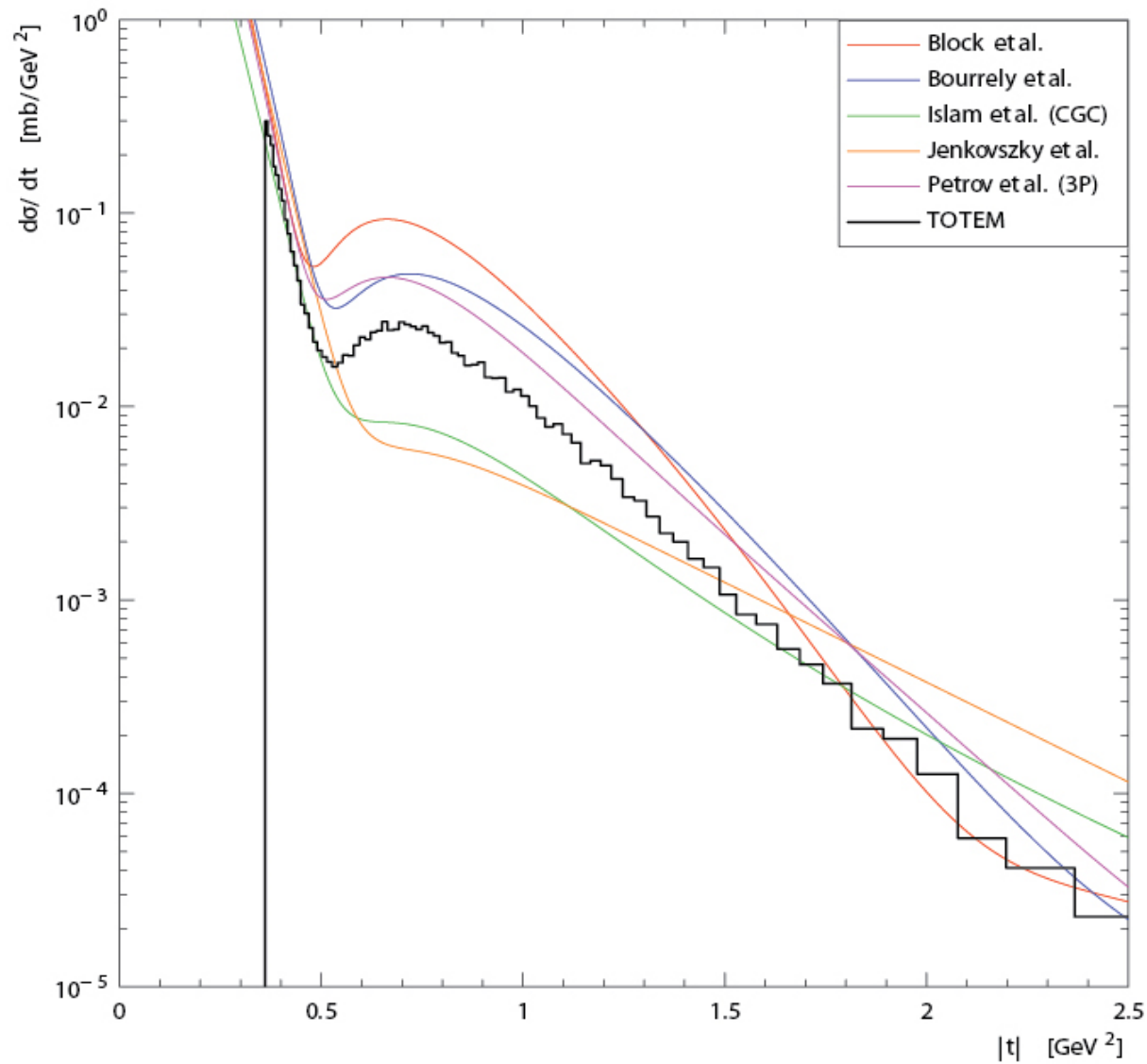
The TOTEM Collaboration

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J. Petäjäjärvi^{3a}, J. Procházka^{1a}, M. Quinto^{5a}, E. Radermacher⁸, E. Radicioni^{5a}, F. Ravotti⁸,
E. Robutti^{6a}, L. Ropelewski⁸, G. Ruggiero⁸, H. Saarikko^{3a,3b}, A. Santroni^{6b,6a}, A. Scribano^{7b},
G. Sette^{6b,6a}, W. Snoeys⁸, F. Spinella^{7a}, J. Sziklai⁴, C. Taylor⁹, N. Turini^{7b}, V. Vacek^{1b}, J. Welti^{3a,b},
M. Vítek^{1b}, J. Whitmore¹⁰.

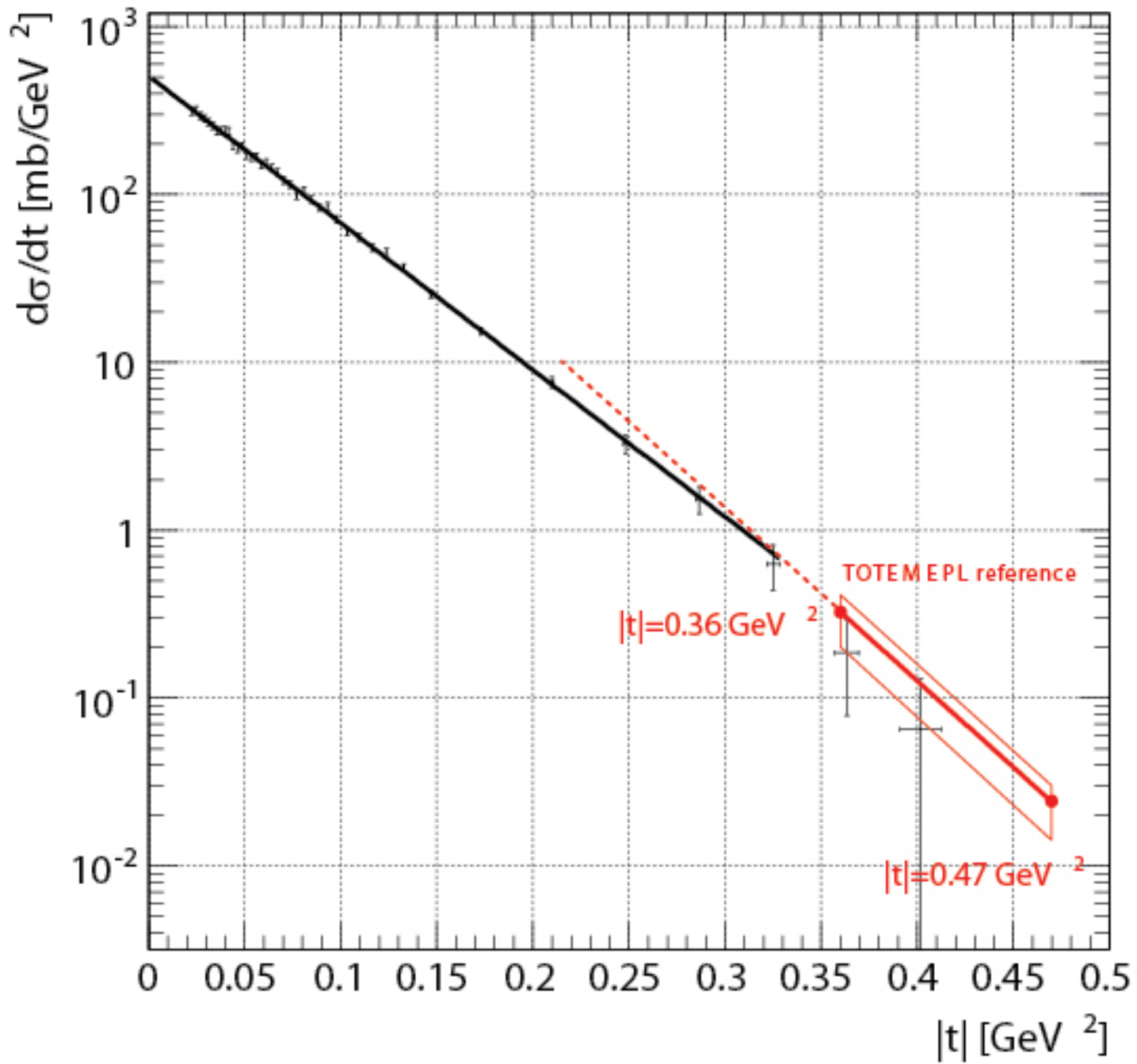
P. Aspell et. al. (TOTEM Collaboration), *Proton-proton elastic scattering at the LHC energy 7 TeV*, Europhys. Lett. **{bf 95}** (2011) 41001; arXiv:1110.1385.

G. Antchev et al. (TOTEM Collab.), *First measurement of the total proton-proton cross section at the LHC energy of 7 TeV*, to be publ in EPL; arXiv:1110.1395.





L. Jenkovszky, A. Lengyel, D. Lontkovskyi, The Pomeron and Odderon in elastic, inelastic and total cross sections at the LHC, *Int. J. Mod. Phys. A* 26, # 26 & 27 (2011) 4755-4771, arXiv:1105.1202



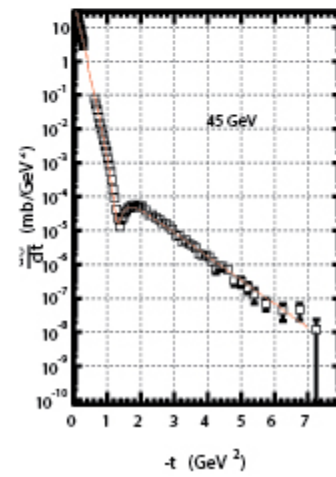
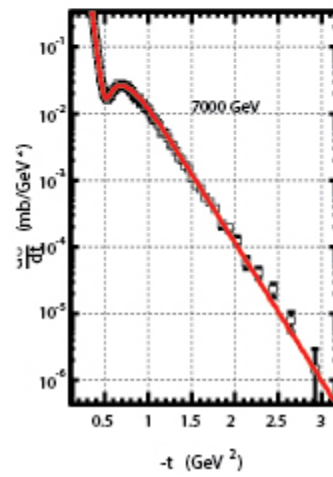
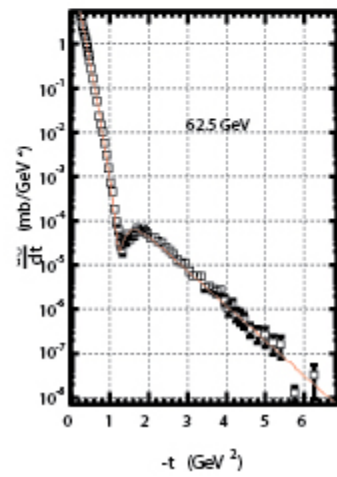
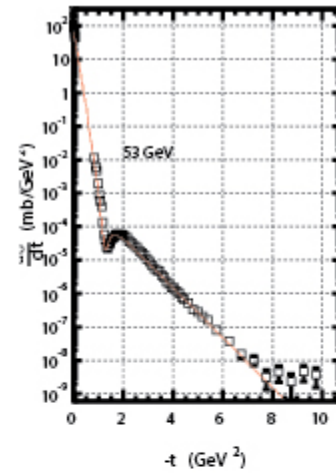
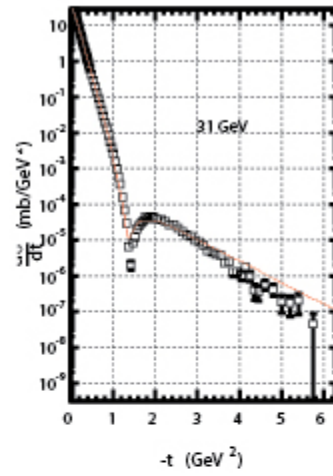
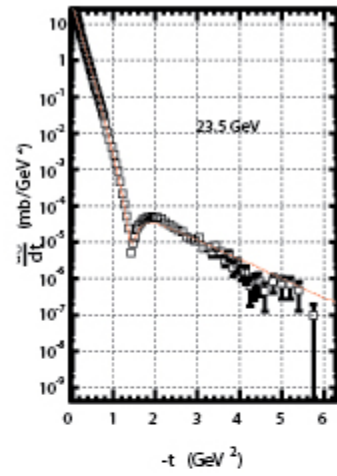
Phenomenology

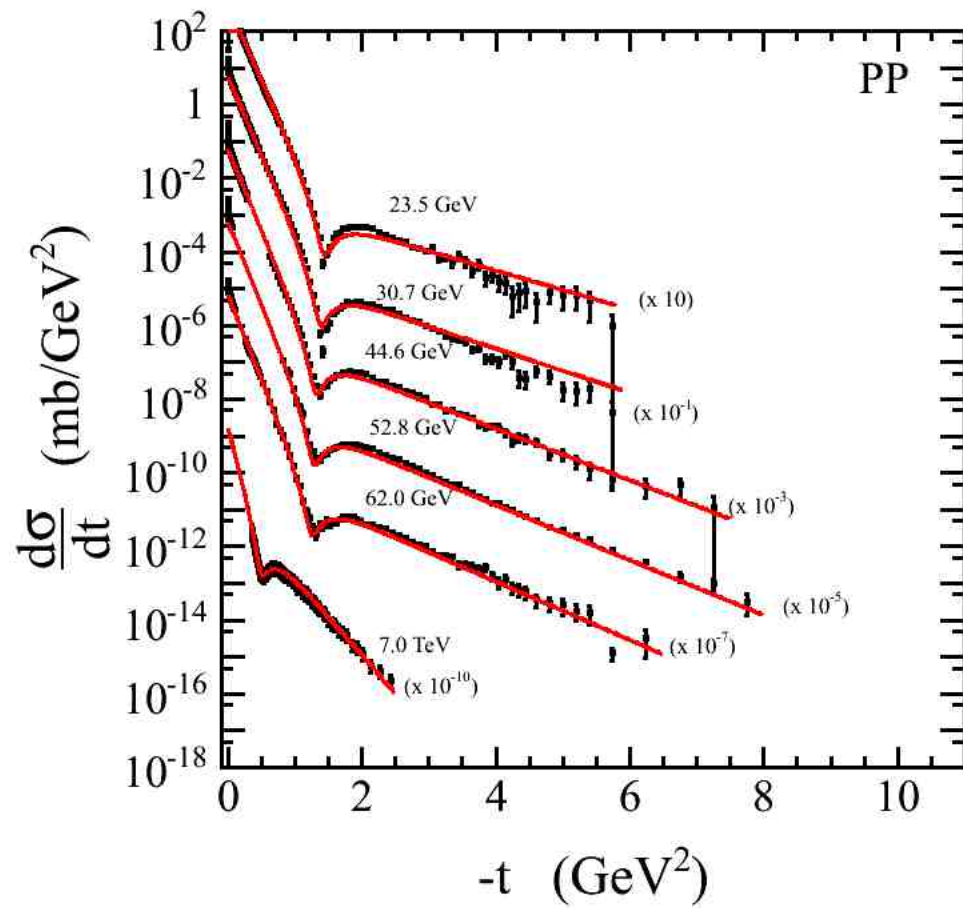
R.J.J. Phillips and V. Barger, *Model independent analysis of the structure in pp scattering*, Phys. Lett. B 46 (1973) 412.

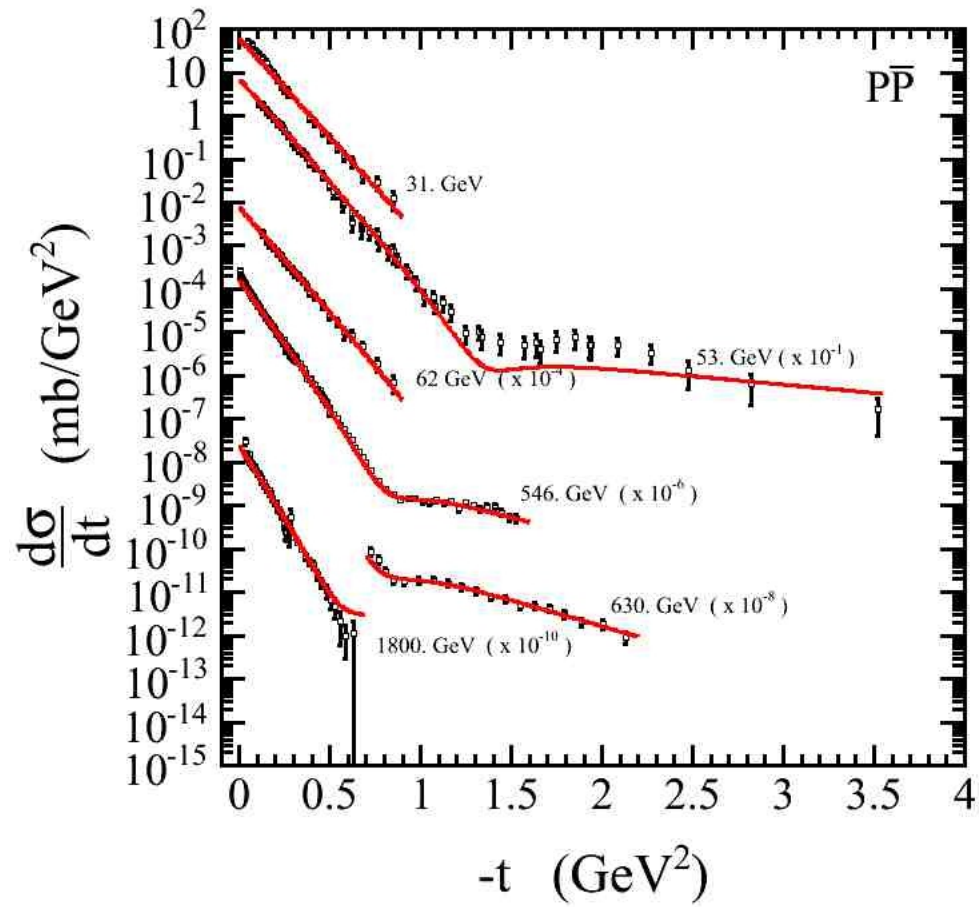
Phillips and Barger in 1973 [], right after its first observation at the ISR.
Their formula reads

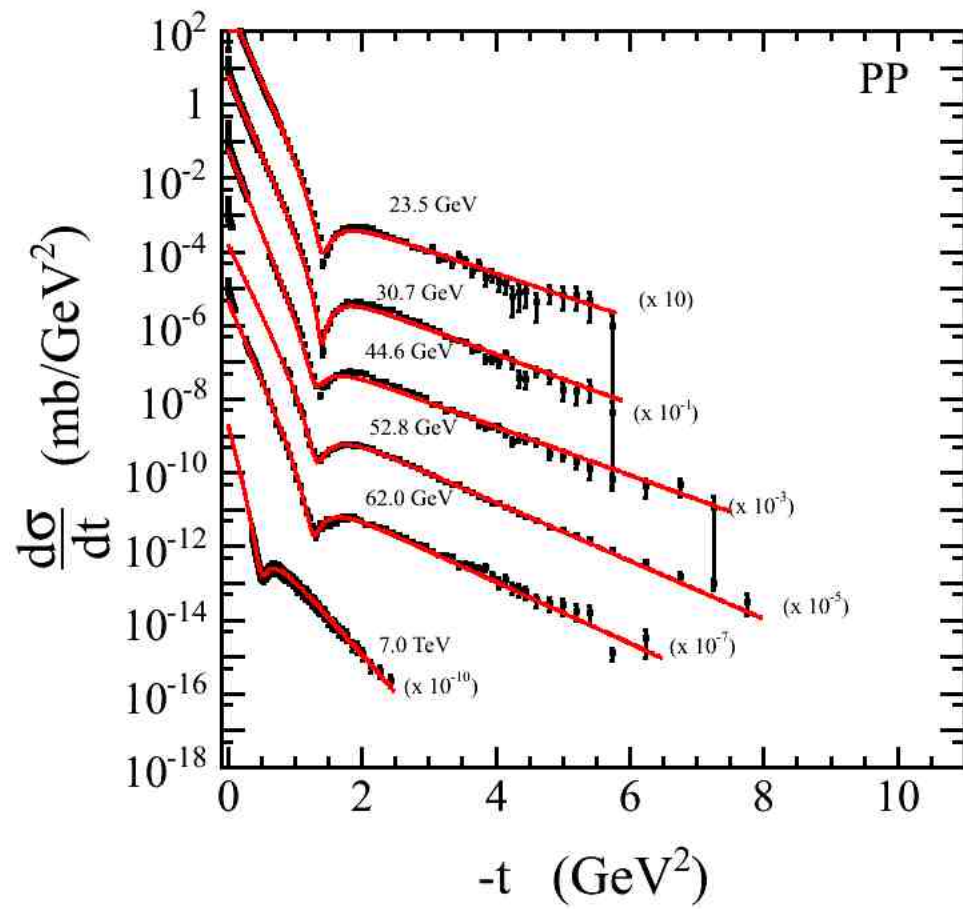
$$\frac{d\sigma}{dt} = |\sqrt{A} \exp(Bt/2) + \sqrt{C} \exp(Dt/2 + i\phi)|^2, \quad (1)$$

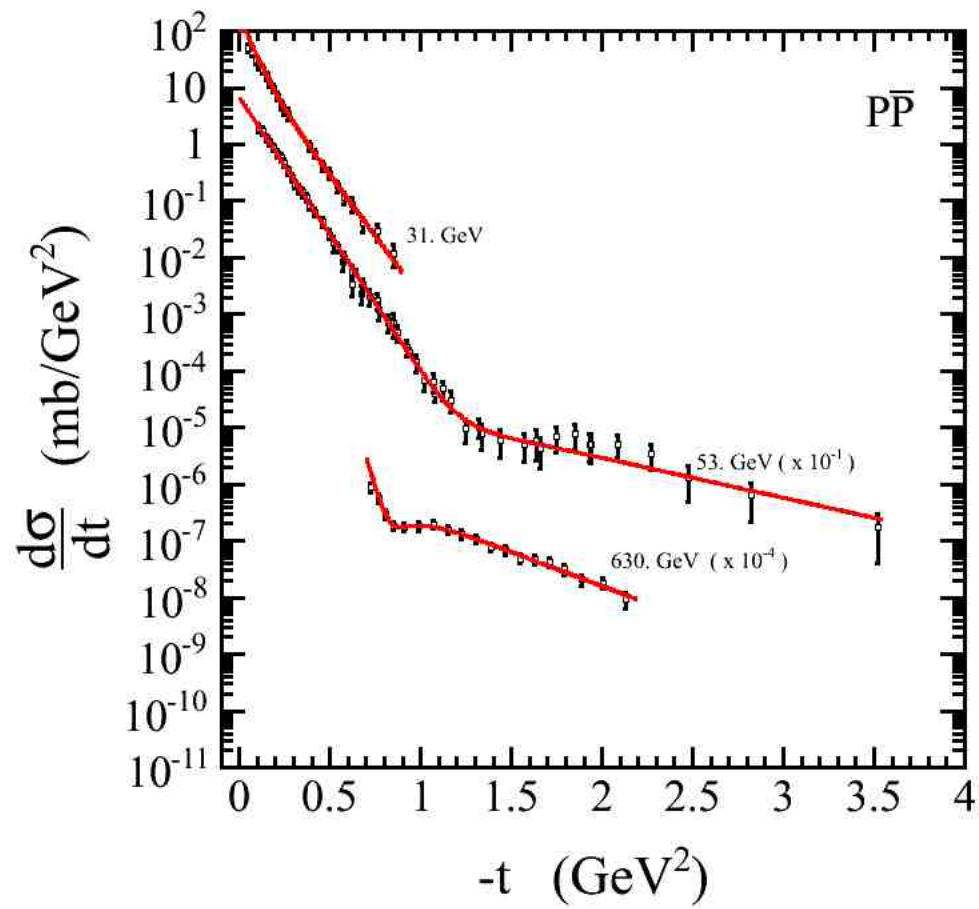
where A , B , C , D and ϕ are determined independently at each energy.

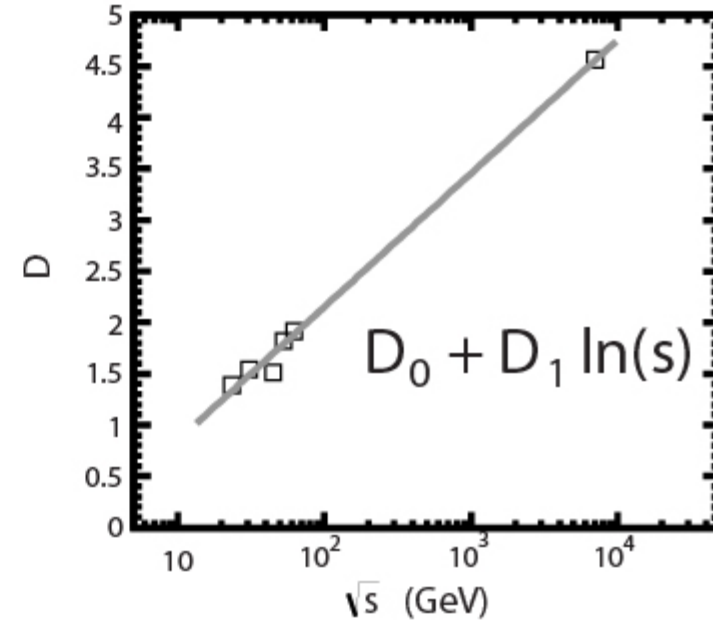
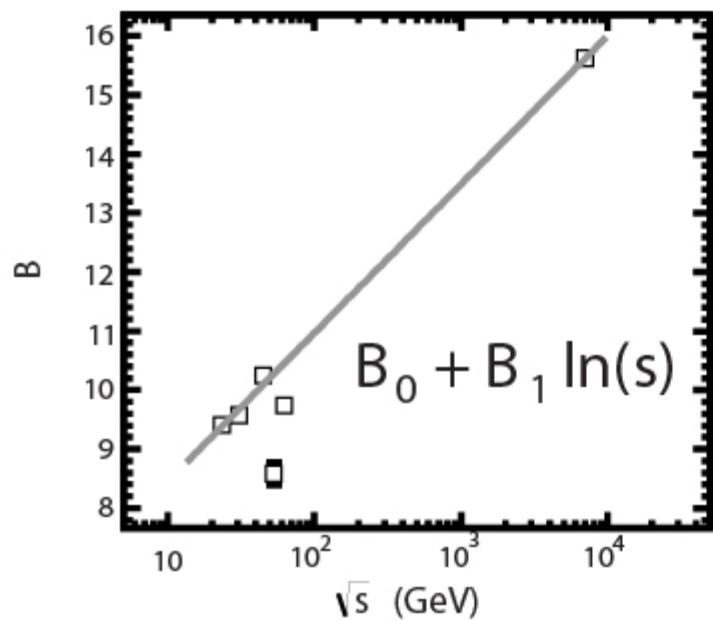
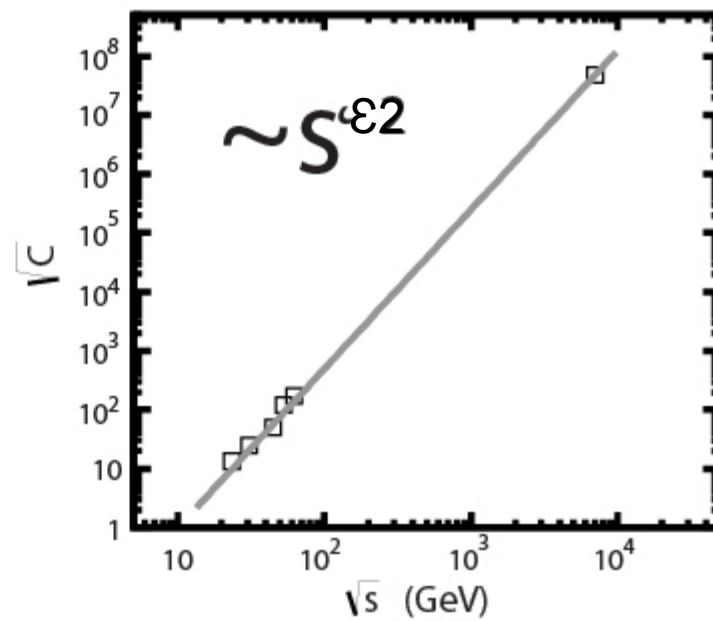
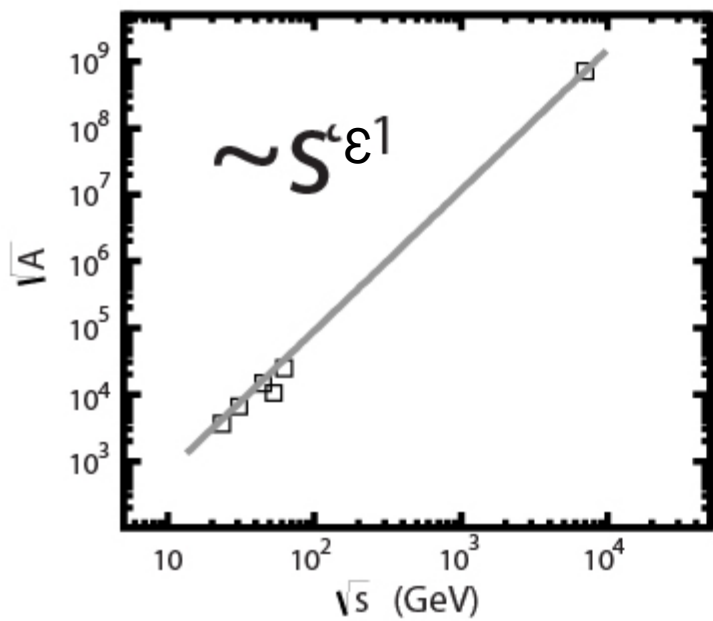












L. Jenkovszky and D. Lontkovskiy: In the Proc. of the Crimean (2011) Conference; also presented at the Russian-Spanish Dual Meeting in Barcelona, November, 2011:

| Parameter name | Value | Uncertainty |
|----------------|-----------------------|----------------|
| | χ^2/\mathbf{NDF} | 4.60434 |
| \sqrt{A} | +2.214549e+001 | +2.344779e-001 |
| B_0 | +1.391529e+000 | +7.408365e-003 |
| B_1 | +3.032435e-001 | +1.525472e-003 |
| \sqrt{C} | +6.952456e+003 | +1.596950e+001 |
| D_0 | +9.766352e+000 | +1.234181e-002 |
| D_1 | +4.648188e-001 | +9.965043e-003 |
| ϵ_1 | +1.358585e+000 | +1.243930e-003 |
| ϵ_2 | +1.057306e+000 | +1.830864e-003 |
| ϕ | +3.511842e+000 | +3.713867e-003 |

T a b l e 2: Parameters obtained from the fit to the pp data

Model building (input + unitarization)

(analyticity, Regge behaviour (factorization), unitarity, GS)

$$A_{pp}^{p\bar{p}}(s, t) = P(s, t) \pm O(s, t) + f(s, t) \pm \omega(s, t) \xrightarrow{LHC} P(s, t) \pm O(s, t),$$

where P is the Pomeron contribution and O is that of the Odderon.

$$P(s, t) = i \frac{as}{bs_0} (r_1^2(s) e^{r_1^2(s)[\alpha_P(t)-1]} - \epsilon r_2^2(s) e^{r_2^2(s)[\alpha_P(t)-1]}),$$

where $r_1^2(s) = b + L - \frac{i\pi}{2}$, $r_2^2(s) = L - \frac{i\pi}{2}$ with $L \equiv \ln \frac{s}{s_0}$; $\alpha_P(t)$ is the Pomeron trajectory and a, b, s_0 and ϵ are free parameters.

Is $A(s,t)$ factorizable? **No, it is not!** (Regge poles, 60-ies)
The inclusion of the virtuality, Q^2 , or the external mass is much more tricky.

$$A_P(s,t) = \frac{d}{d\alpha_P} \left[e^{-i\pi\alpha_P/2} G(\alpha_P) \left(s/s_0 \right)^{\alpha_P} \right] = \quad (1)$$
$$e^{-i\pi\alpha_P(t)/2} \left(s/s_0 \right)^{\alpha_P(t)} \left[G'(\alpha_P) + \left(L - i\pi/2 \right) G(\alpha_P) \right].$$

$$\alpha = \alpha(t)$$

The Pomeron is a dipole in the j -plane

$$A_P(s, t) = \frac{d}{d\alpha_P} \left[e^{-i\pi\alpha_P/2} G(\alpha_P) \left(s/s_0 \right)^{\alpha_P} \right] = \quad (1)$$

$$e^{-i\pi\alpha_P(t)/2} \left(s/s_0 \right)^{\alpha_P(t)} \left[G'(\alpha_P) + \left(L - i\pi/2 \right) G(\alpha_P) \right].$$

Since the first term in squared brackets determines the shape of the cone, one fixes

$$G'(\alpha_P) = -a_P e^{b_P[\alpha_P-1]}, \quad (2)$$

where $G(\alpha_P)$ is recovered by integration, and, as a consequence, the Pomeron amplitude can be rewritten in the following “geometrical” form

$$A_P(s, t) = i \frac{a_P s}{b_P s_0} \left[r_1^2(s) e^{r_1(s)[\alpha_P-1]} - \varepsilon_P r_2^2(s) e^{r_2(s)[\alpha_P-1]} \right], \quad (3)$$

where $r_1^2(s) = b_P + L - i\pi/2$, $r_2^2(s) = L - i\pi/2$, $L \equiv \ln(s/s_0)$.

By factoring out the term from the square brackets, we get:

$$A_P(s, t) = i \frac{a_P}{b_P} \frac{s}{s_0} \sqrt{R_1^4 + \varepsilon_P^2 R_2^4} \left[\frac{R_1^2}{\sqrt{R_1^4 + \varepsilon_P^2 R_2^4}} e^{R_1^2 \cdot [\alpha_P - 1]} - \frac{\varepsilon_P^2 R_2^2}{\sqrt{R_1^4 + \varepsilon_P^2 R_2^4}} e^{R_2^2 \cdot [\alpha_P - 1]} \right]. \quad (1)$$

One can define

$$\cos \theta \equiv \frac{R_1^2}{\sqrt{R_1^4 + \varepsilon_P^2 R_2^4}} = \frac{e^{i\theta} + e^{-i\theta}}{2}, \quad \sin \theta \equiv -\frac{\varepsilon_P^2 R_2^2}{\sqrt{R_1^4 + \varepsilon_P^2 R_2^4}} = \frac{e^{i\theta} - e^{-i\theta}}{2i}. \quad (2)$$

$$A_P(s, t) = i \frac{a_P}{b_P} \frac{s}{s_0} \sqrt{R_1^4 + \varepsilon_P^2 R_2^4} e^{-i\theta} \left[(e^{i2\theta} + 1) e^{R_1^2 \cdot [\alpha_P - 1]} + (e^{i2\theta} - 1) e^{-i\frac{\pi}{2}} e^{R_2^2 \cdot [\alpha_P - 1]} \right]. \quad (3)$$

Or equivalently for the case of linear trajectory with unit intercept $\alpha_P(t) = 1 + \alpha'_P t$

$$A_P(s, t) = i e^{-i\theta} \left[\sqrt{A} e^{\frac{1}{2} B_1 t} + \sqrt{A} e^{\frac{1}{2} B_1 t + i\varphi_1} + i \left(\sqrt{A} e^{\frac{1}{2} B_2 t} + \sqrt{A} e^{\frac{1}{2} B_2 t + i\varphi_2} \right) \right]. \quad (4)$$

Where

$$\sqrt{A}(s) = \sqrt{\left(\frac{1}{2} \frac{a_P}{b_P} \frac{s}{s_0} \right)^2 (R_1^4 + \varepsilon_P^2 R_2^4)}, \quad (5a)$$

$$B_1(s) = 2R_1^2(s) \alpha'_P, \quad B_2(s) = 2R_2^2(s) \alpha'_P, \quad (5b)$$

$$\varphi_1 = -2\theta, \quad \varphi_2 = 2\theta + \pi. \quad (5c)$$

Such an amplitude can be considered as a sum of two PB-type amplitudes.

The Pomeron trajectory

The Pomeron trajectory has threshold singularities, the lowest one being due to the two-pion exchange, required by the t -channel unitarity. There is a constrain (Barut, Zwanziger; Gribov) from the t -channel unitarity, by which

$$\Im\alpha(t) \sim (t - t_0)^{\Re\alpha(t_0)+1/2}, \quad t \rightarrow t_0,$$

where t_0 is the lightest threshold. For the Pomeron trajectory it is $t_0 = 4m_\pi^2$, and near the threshold:

$$\alpha(t) \sim \sqrt{4m_\pi^2 - t}. \quad (1)$$

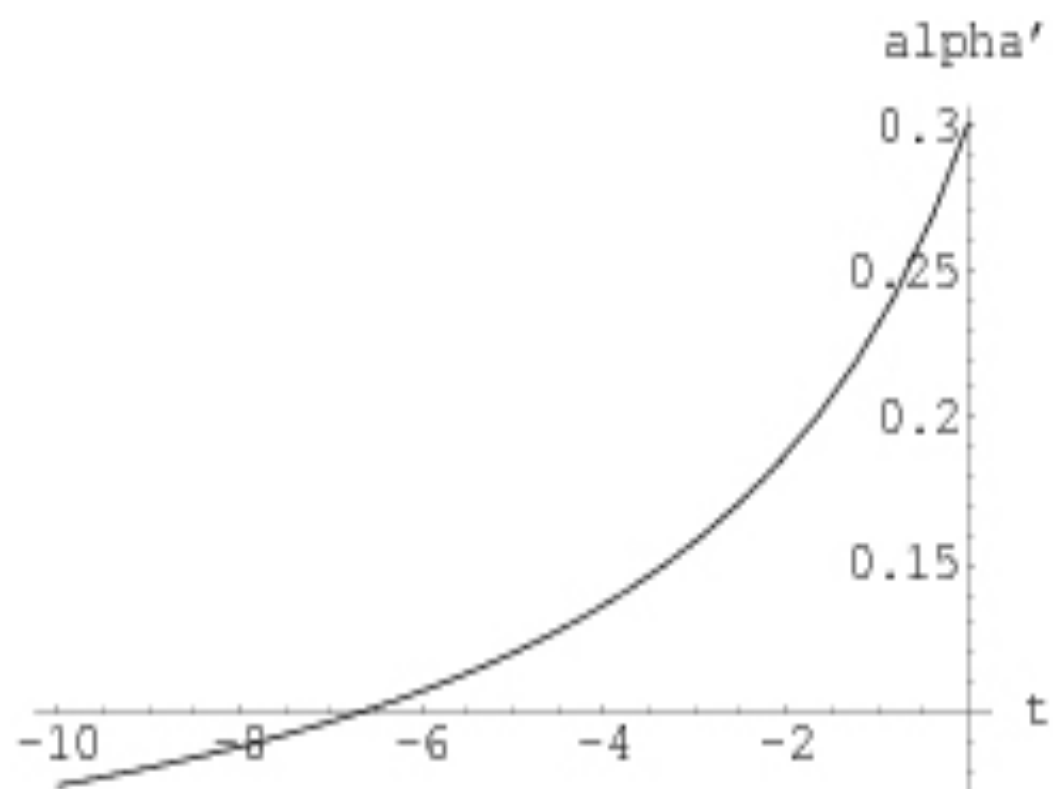
The observed nearly linear behaviour of the trajectory is promoted by higher, additive thresholds.

Asymptotically, the trajectories are logarithmic. This follows from the compatibility of the Regge behavior with the quark counting rules (Brodsky, Farrar; MMT), as well as from the solution of the BFKL equation. A simple parametrization combining the linear behaviour at small $|t|$ with its logarithmic asymptotic is:

$$\alpha(t) = \alpha_0 - \gamma \ln(1 - \beta_1 t).$$

Nearly linear at small $|t|$, it reproduces the forward cone of the differential cross section, while its logarithmic asymptotic provides for the wide-angle scaling behavior. A combined form is:

$$\alpha(t) = \alpha_0 - \gamma \ln(1 + \beta_2 \sqrt{t_0 - t}).$$

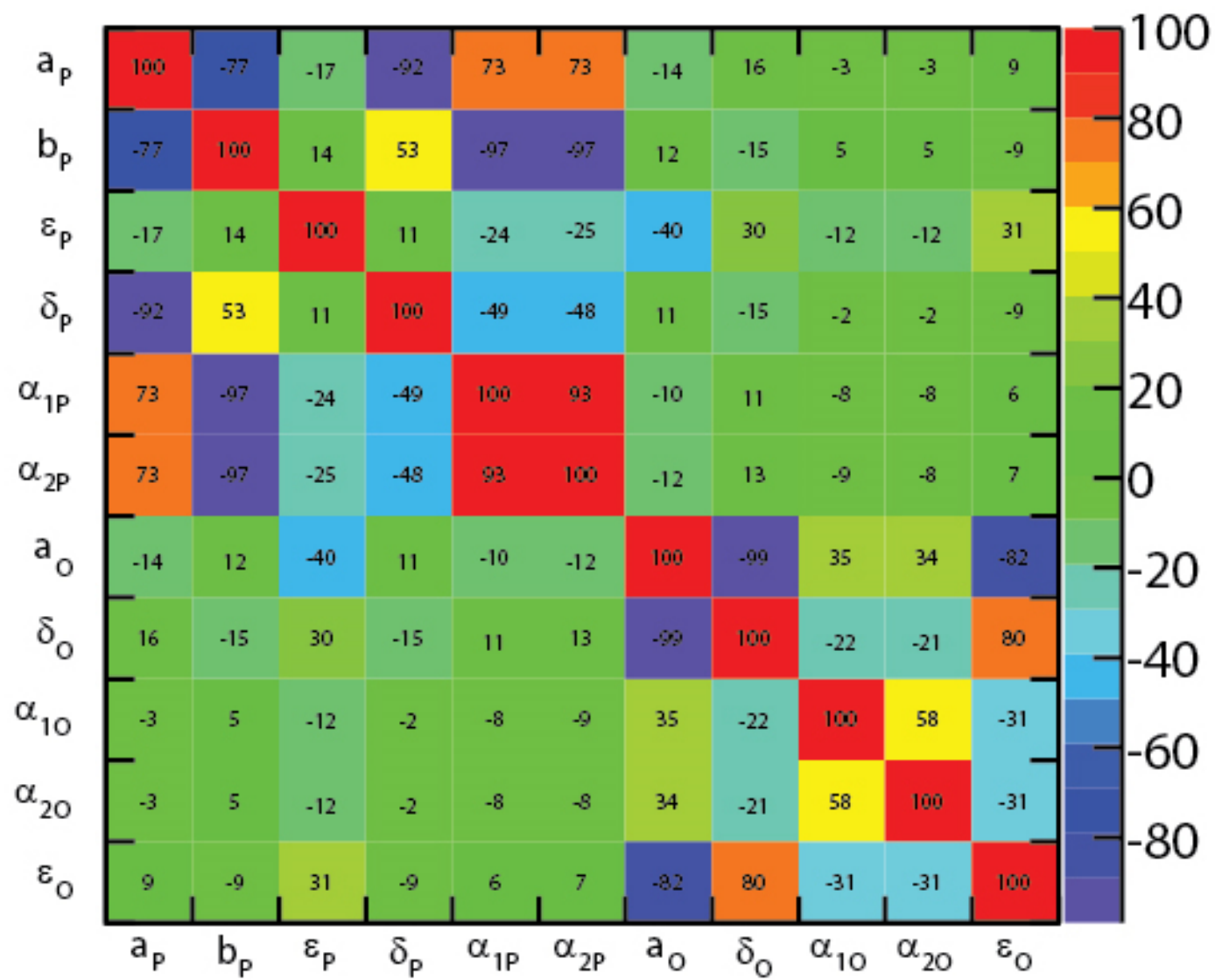


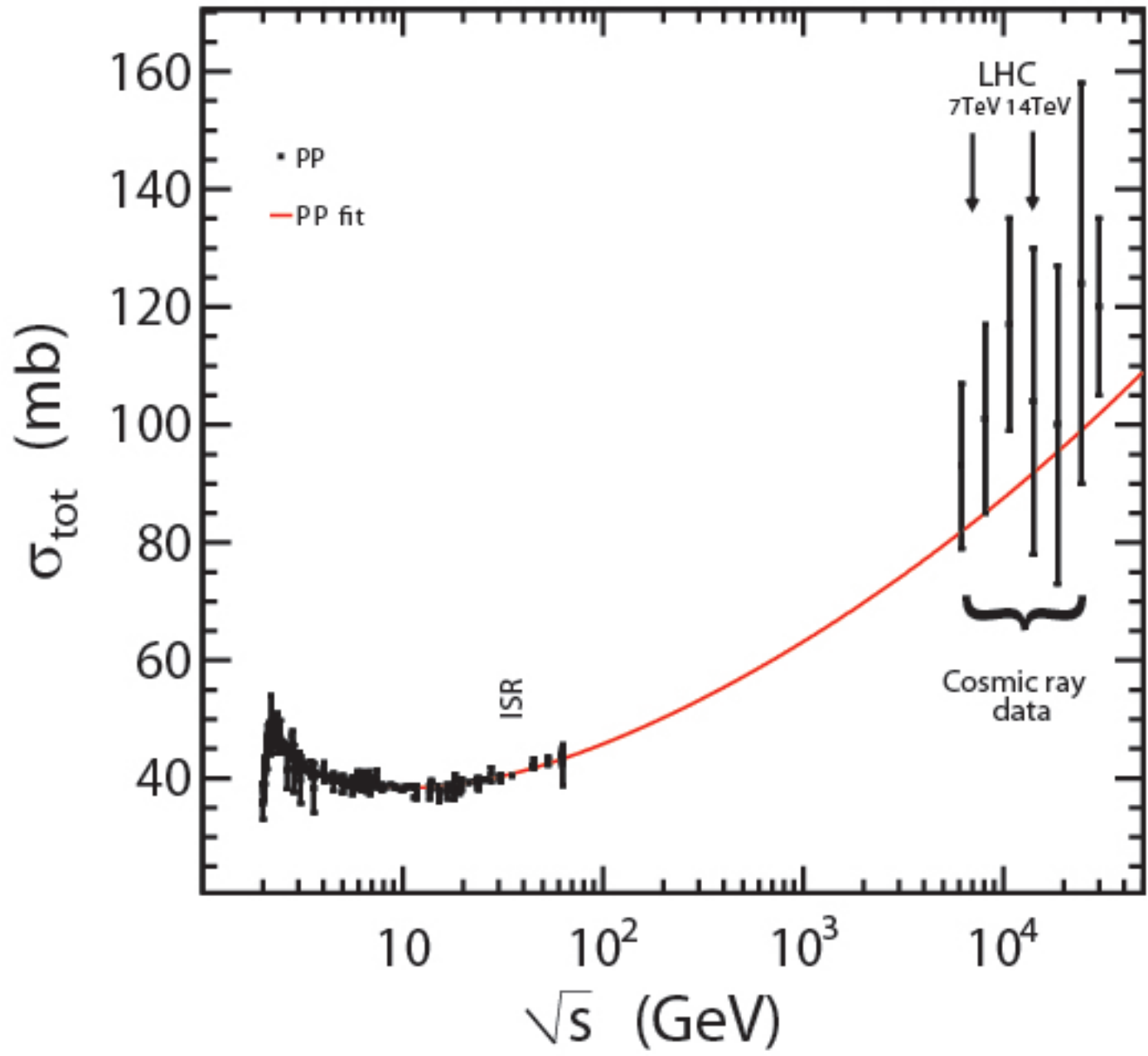
Representative examples of the Pomeron trajectories: 1) Linear; 2) With a square-root threshold, required by t -channel unitarity and accounting for the small- t “break” as well as the possible “Orear”, $e^{\sqrt{-t}}$ behavior in the second cone; and 3) A logarithmic one, anticipating possible “hard effects” at large $|t|$ $|t| < 8 \text{ GeV}^2$.

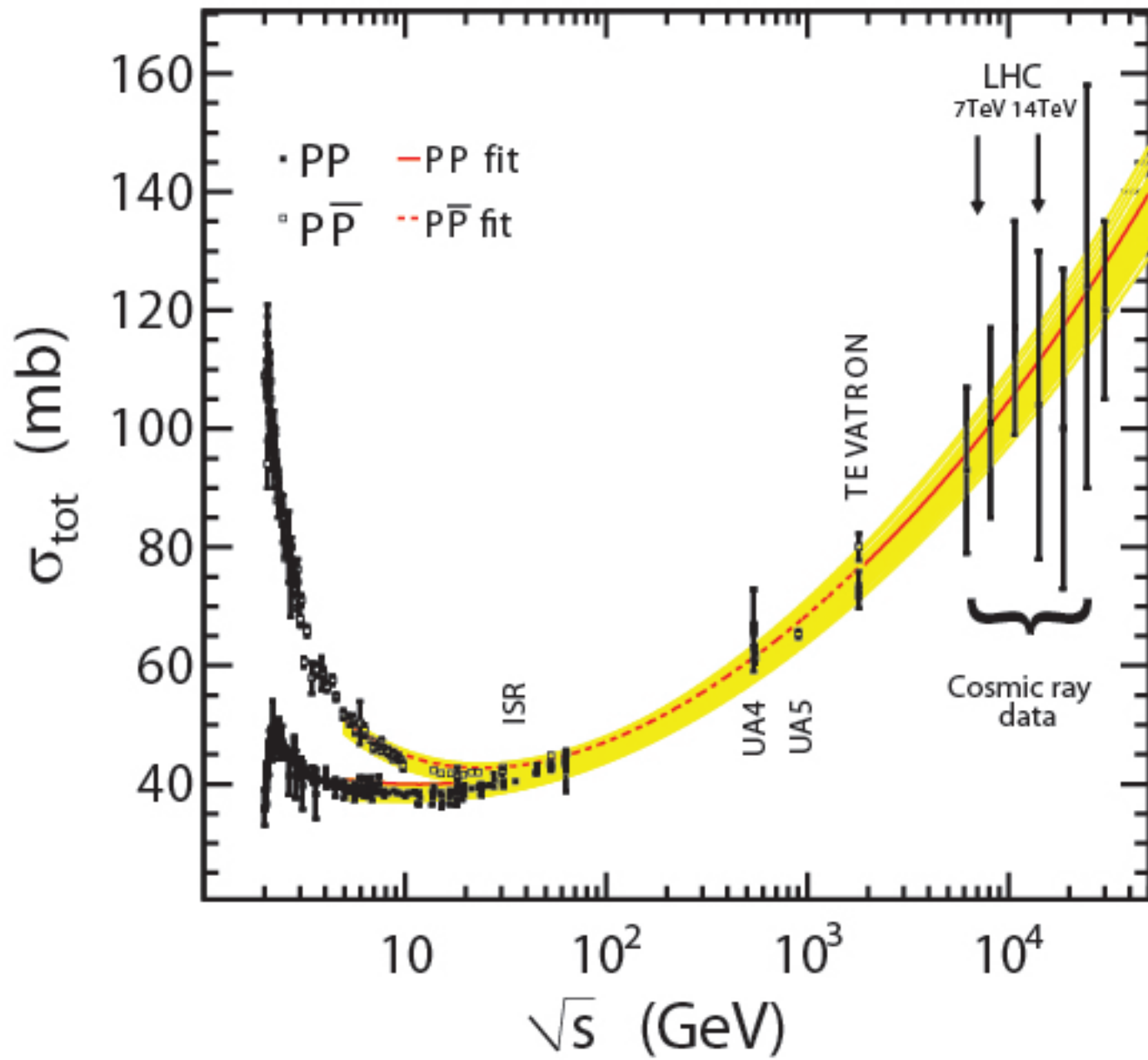
$$\alpha_P \equiv \alpha_P(t) = 1 + \delta_P + \alpha_{1P}t, \quad (\text{TR.1})$$

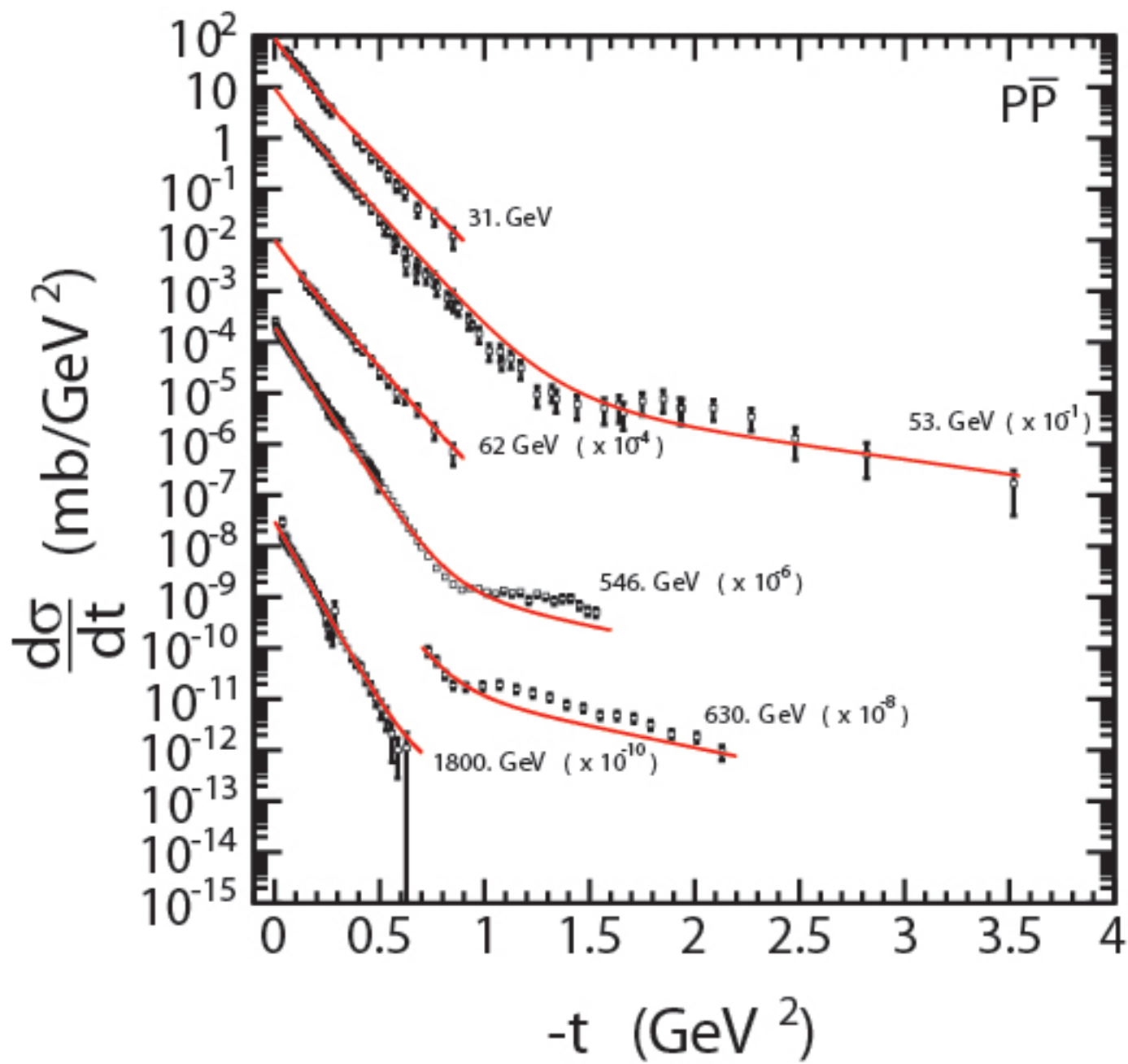
$$\alpha_P \equiv \alpha_P(t) = 1 + \delta_P + \alpha_{1P}t - \alpha_{2P} \left(\sqrt{4\alpha_{3P}^2 - t} - 2\alpha_{3P} \right), \quad (\text{TR.2})$$

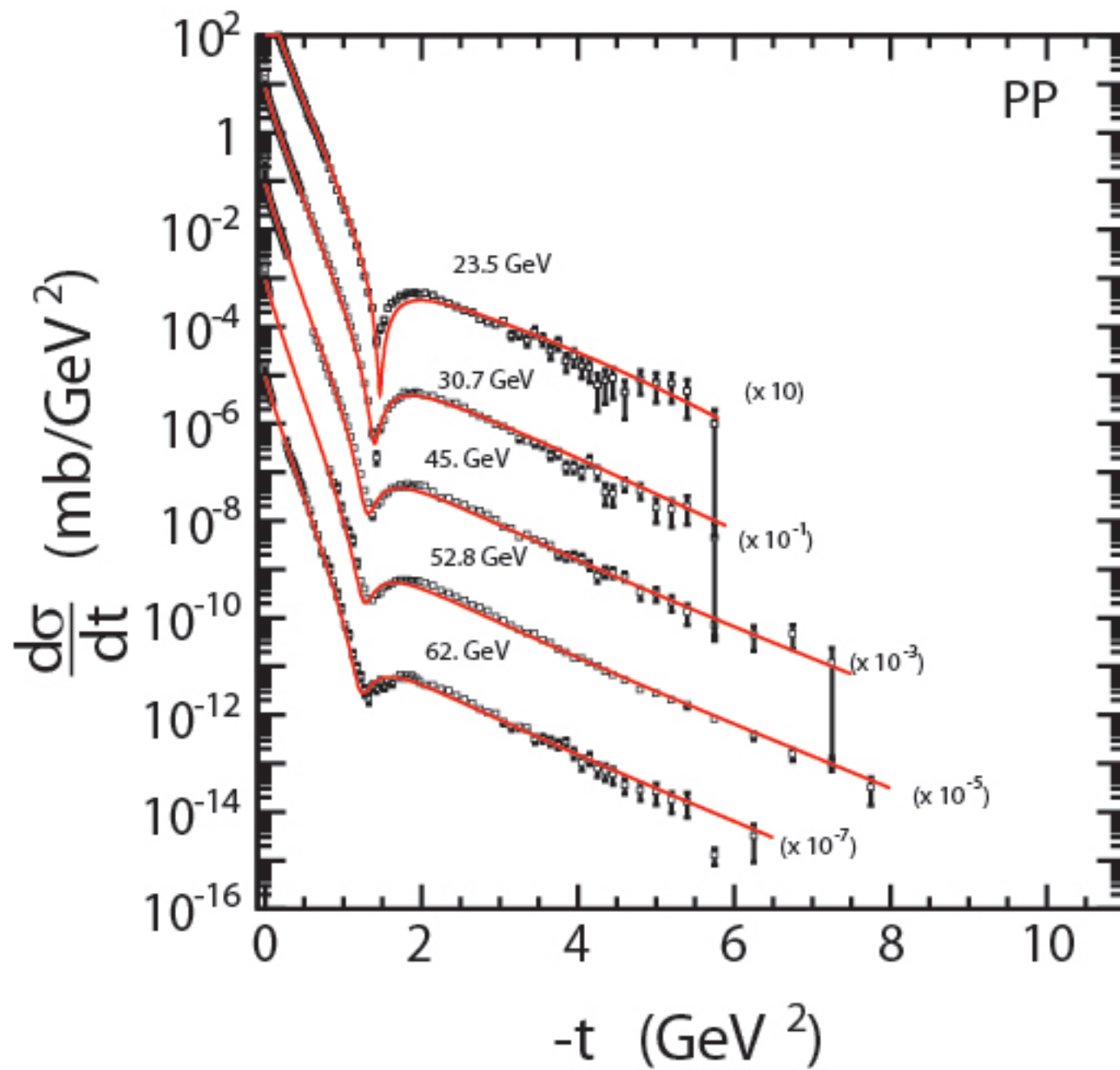
$$\alpha_P \equiv \alpha_P(t) = 1 + \delta_P - \alpha_{1P} \ln(1 - \alpha_{2P}t). \quad (\text{TR.3})$$

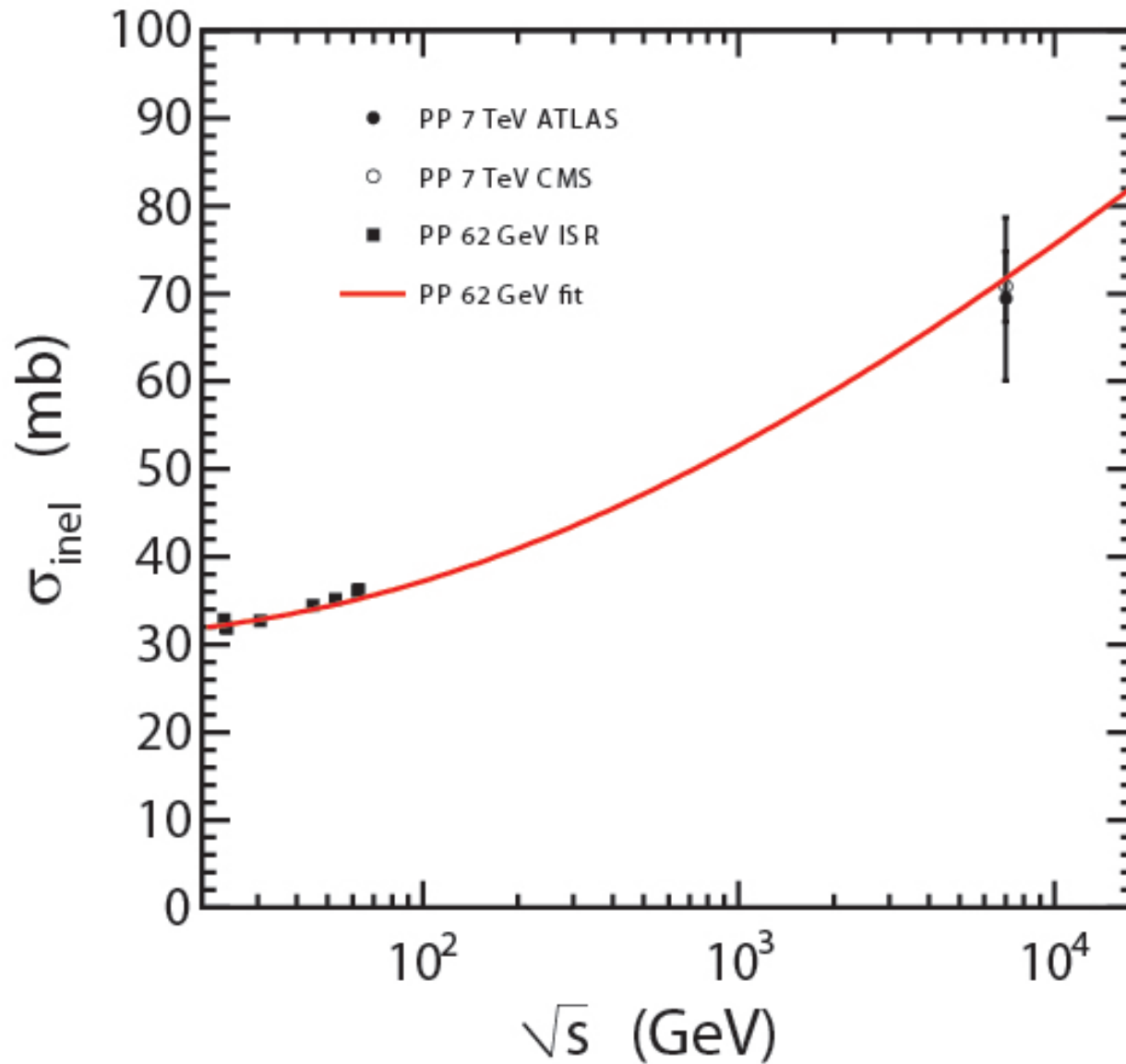




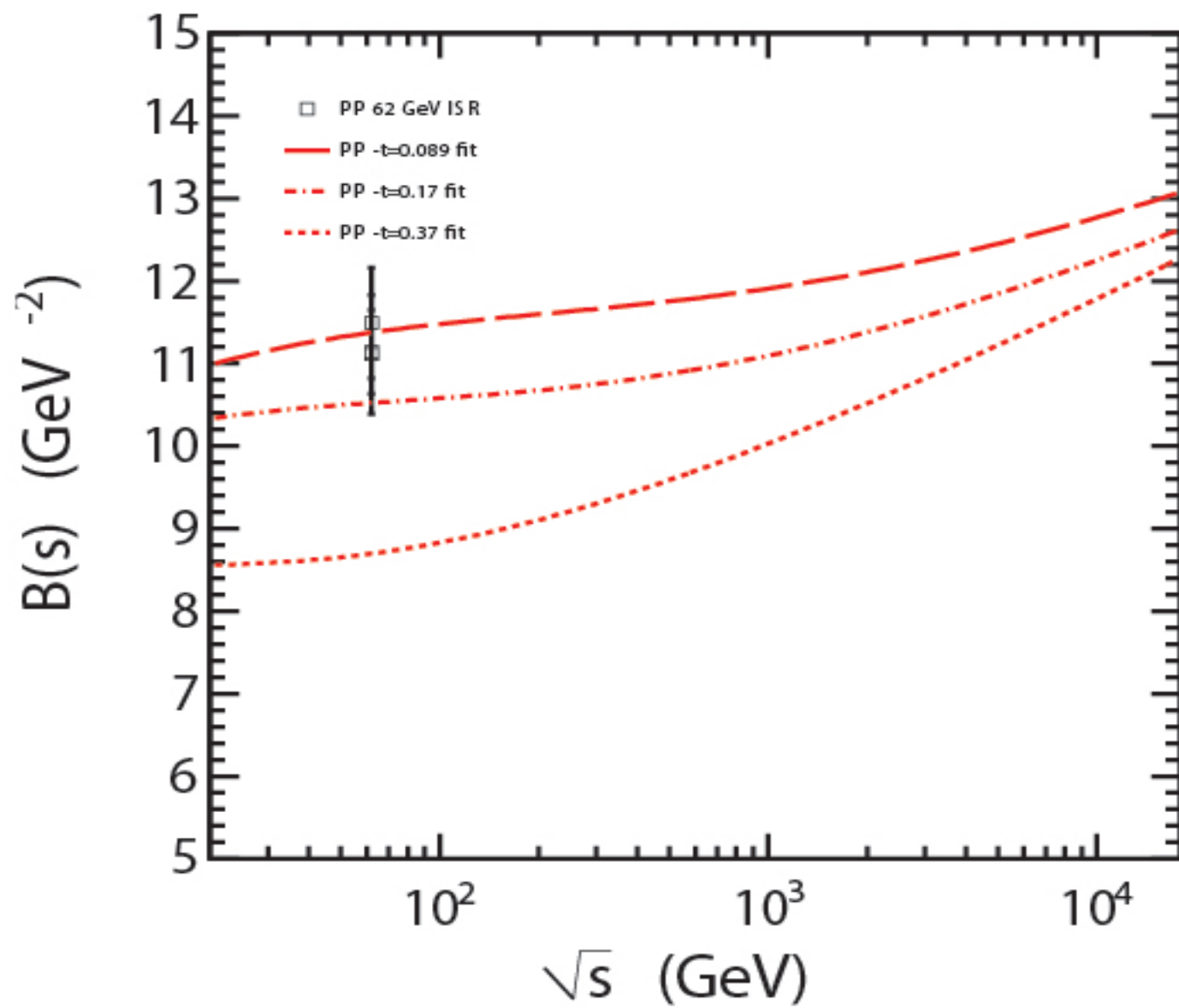


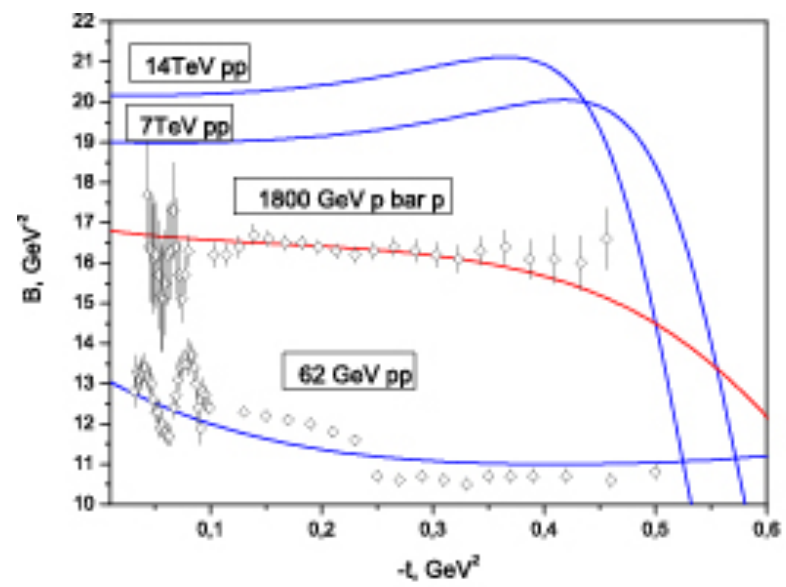


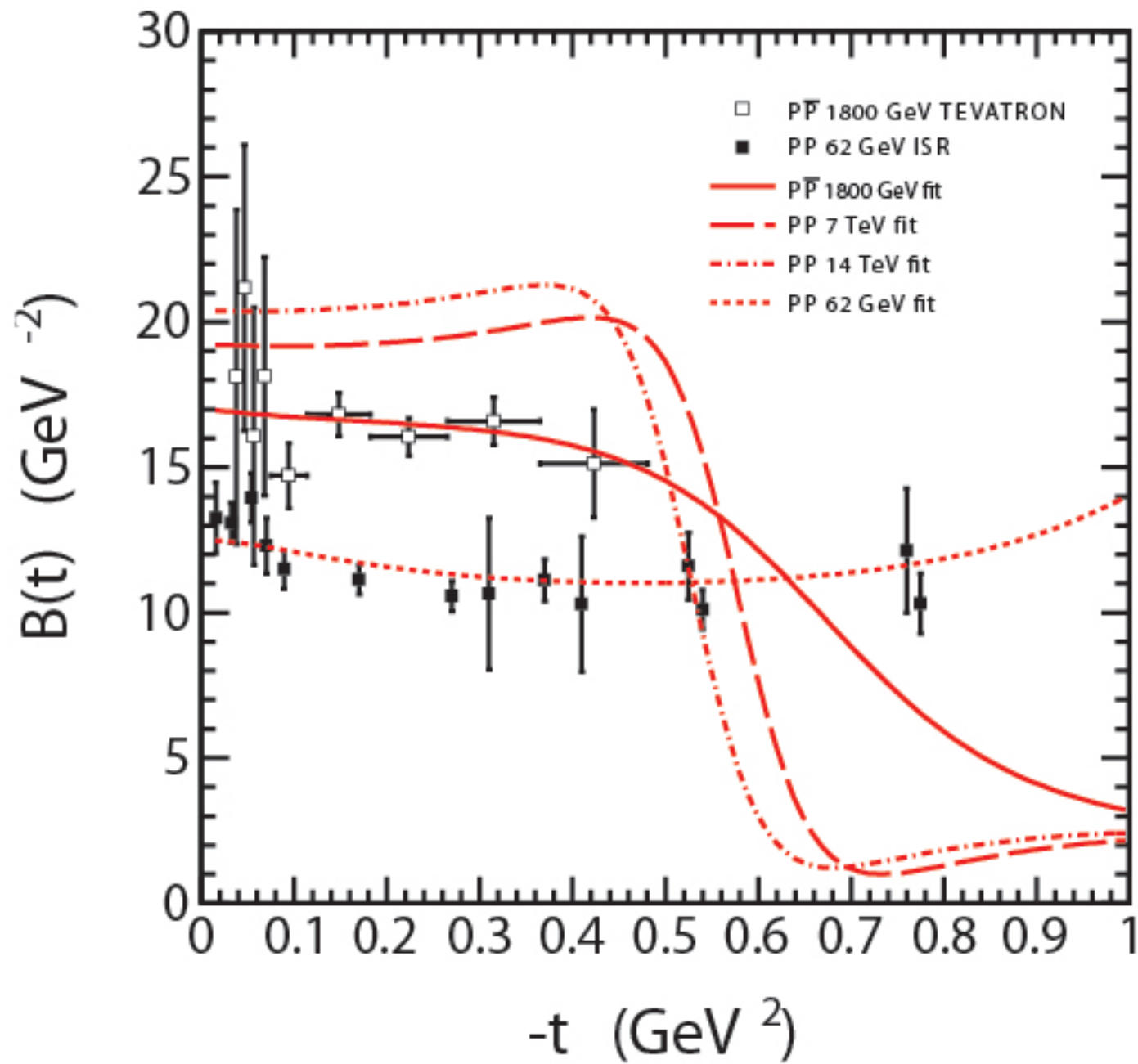




ATLAS At DIS11 [http://www-atlas.lbl.gov/\\$\sim\\$stompkins/parallel.SxDNVM.tompkins.talk.pdf](http://www-atlas.lbl.gov/\simstompkins/parallel.SxDNVM.tompkins.talk.pdf);
CMS at DIS11 <https://wiki.bnl.gov/conferences/images/8/8c/Parallel.SxDNVM.Marone.13April.talk.pdf>







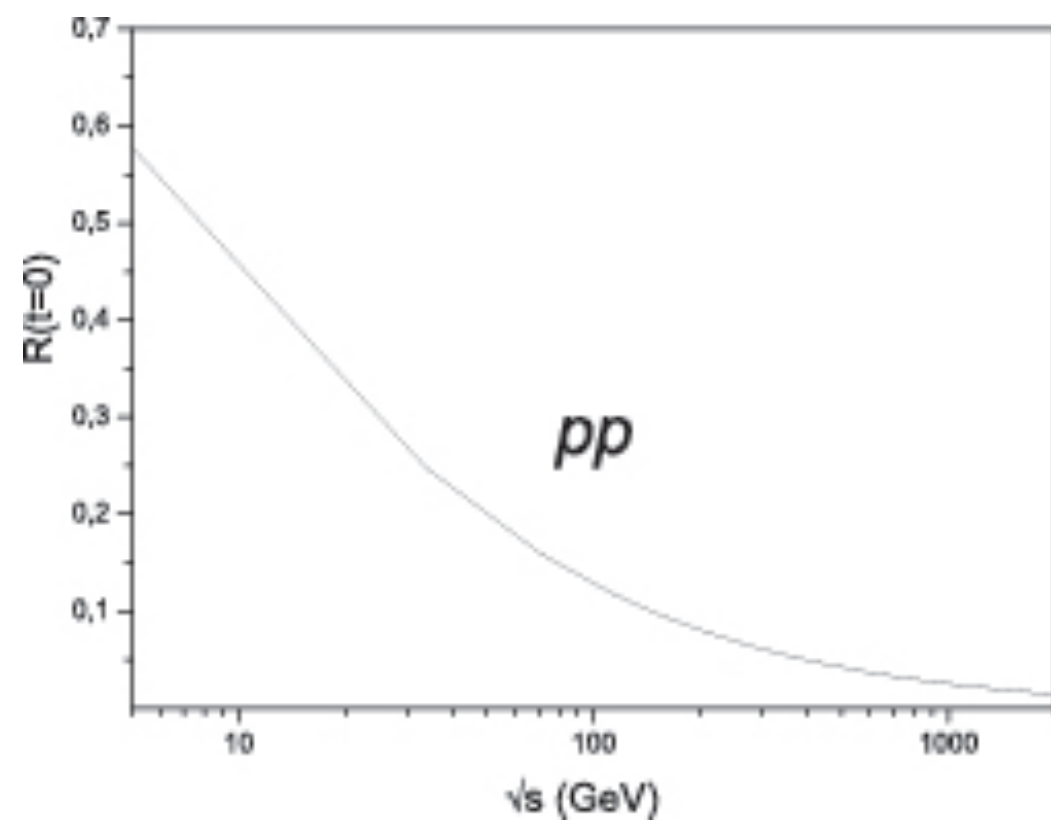
Energy variation of the relative importance of the Pomeron with respect to contributions from the secondary trajectories and the Odderon:

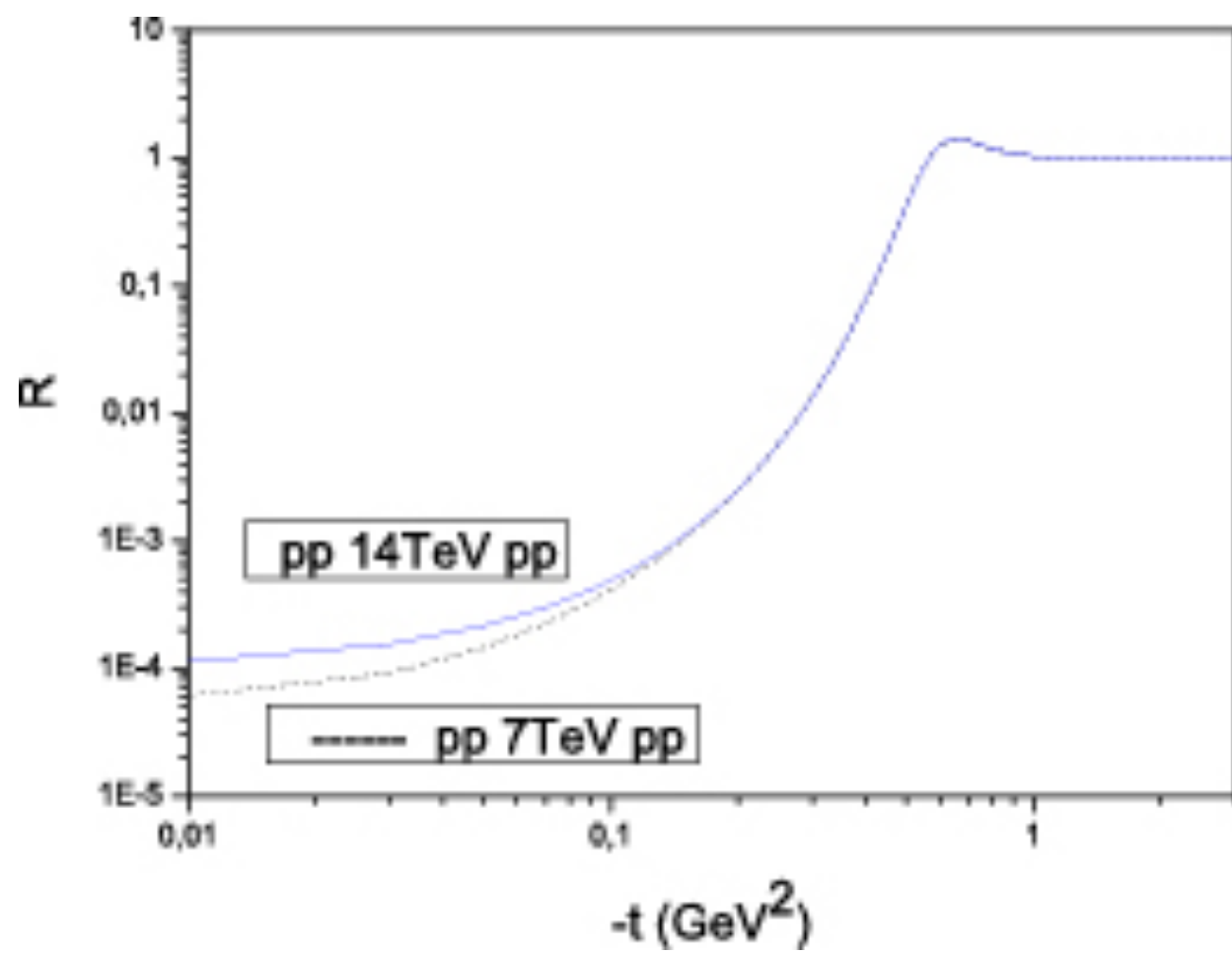
$$R(s, t = 0) = \frac{\Im m(A(s, t) - A_P(s, t))}{\Im A(s, t)}, \quad (1)$$

where the total scattering amplitude A includes the Pomeron contribution A_P plus the contribution from the secondary Reggeons and the Odderon.

Starting from the Tevatron energy region, the relative contribution of the non-Pomeron terms to the total cross-section becomes smaller than the experimental uncertainty and hence at higher energies they may be completely neglected, irrespective of the model used.

$$R(s, t) = \frac{|(A(s, t) - A_P(s, t))|^2}{|A(s, t)|^2}. \quad (2)$$





Lessons:

1. Model predictions **for integral characteristics**, on the whole, are compatible with the data within about 10% (not too interesting!), diverging by orders of magnitudes (!) in the dip-bump region, that can be used to discriminate the existing (and future) models;
2. Any model should describe all observables in a wide kinematical range, with a unique set of adjustable parameters;
3. For any comparison and critical assessment, a ‘bank of models’ should be created, in which different models would be tested on a unique set of the data. Who could do this?
4. The Pomeron has (nearly) the same status as the Pomeron;
5. Matching D0’s (Ch. Royon) and TOTEM’s (M.Deile) elastic data as well as DD are important;
6. The Regge pole theory and QCD are progressing parallelly, with little or no interference. Spin?
7. QCD, the official ideology, has no predictive power (at least in this field);
5. TOTEM’s first results are worth more than those of the “superluminal” OPERA and “Higgs’ exclusion”, taken together.

Cám ơn !