

# DIFFRACTIVE PRODUCTION OF $c\bar{c}$

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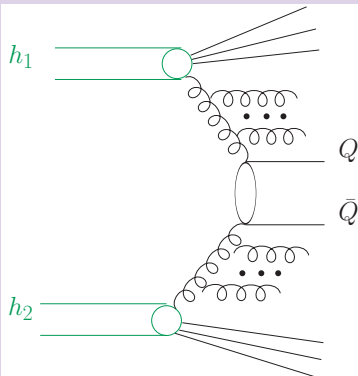
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# Plan of the talk

- Introduction
- Parton distributions
- Results
  - $k_t$ -factorization
  - gluon distributions at small- $x$  region
  - $\gamma g$  and  $g\gamma$  subprocesses
  - $\gamma\gamma$  subprocesses
  - single and central diffraction
  - production of two  $c\bar{c}$  pairs in double-parton scattering
- Conclusions

# Production of heavy quarks

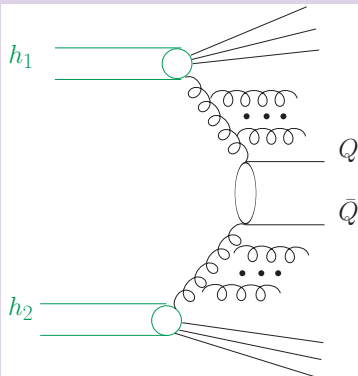
$$h_1 + h_2 \rightarrow Q + \bar{Q} + X:$$



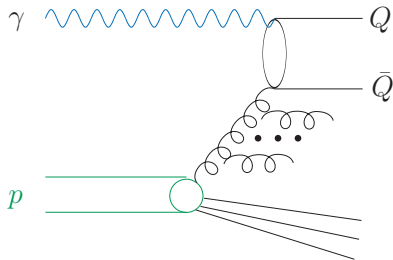
$$\gamma + p \rightarrow Q + \bar{Q} + X:$$

# Production of heavy quarks

$$h_1 + h_2 \rightarrow Q + \bar{Q} + X:$$

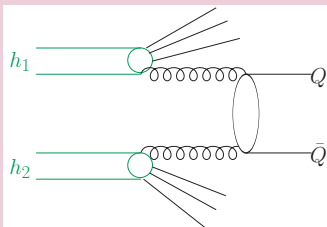


$$\gamma + p \rightarrow Q + \bar{Q} + X:$$

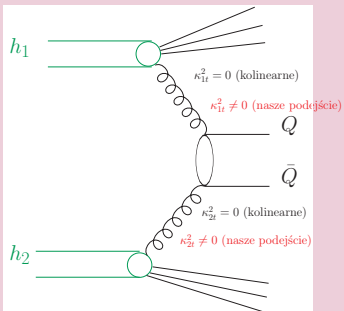


# Dominant mechanism

## LO collinear approach



## $k_t$ -factorization



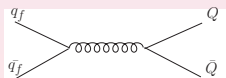
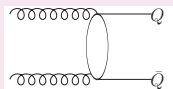
## Formalism of collinear - factorization

$$\frac{d\sigma}{dy_1 dy_2 d^2 p_t} = \frac{1}{16\pi^2 \hat{s}^2} \sum_{i,j} x_1 p_i(x_1, \mu^2) x_2 p_j(x_2, \mu^2) \overline{|\mathcal{M}_{ij}|^2}$$

$$p_{1t} = p_{2t} = p_t$$

$$x_1 = \frac{m_t}{\sqrt{s}} (\exp(y_1) + \exp(y_2)),$$

$$x_2 = \frac{m_t}{\sqrt{s}} (\exp(-y_1) + \exp(-y_2))$$



# Formalism of $k_t$ -factorization

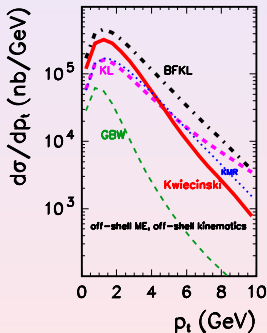
$$\frac{d\sigma}{dy_1 dy_2 d^2 p_{1,t} d^2 p_{2,t}} = \sum_{i,j} \int \frac{d^2 \kappa_{1,t}}{\pi} \frac{d^2 \kappa_{2,t}}{\pi} \frac{1}{16\pi^2 (x_1 x_2 s)^2} |\overline{\mathcal{M}}_{ij}|^2$$

$$\delta^2(\vec{\kappa}_{1,t} + \vec{\kappa}_{2,t} - \vec{p}_{1,t} - \vec{p}_{2,t}) f_i(x_1, \kappa_{1,t}^2) f_j(x_2, \kappa_{2,t}^2)$$

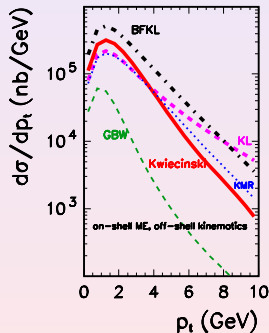
$$m_t = \sqrt{p_{t,t}^2 + m^2}$$

$$x_1 = \frac{m_{1,t}}{\sqrt{s}} \exp(y_1) + \frac{m_{2,t}}{\sqrt{s}} \exp(y_2),$$

$$x_2 = \frac{m_{1,t}}{\sqrt{s}} \exp(-y_1) + \frac{m_{2,t}}{\sqrt{s}} \exp(-y_2).$$

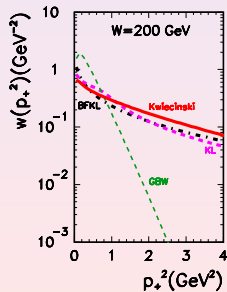
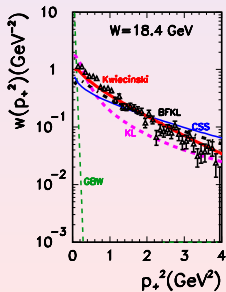
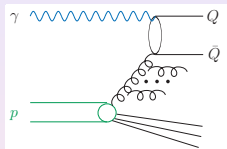
$gg \rightarrow c\bar{c}$  ( $k_t$ -factorization)

off-shell

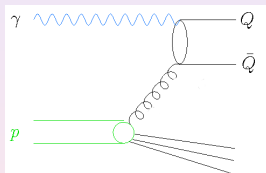


on-shell



$\gamma p \rightarrow c\bar{c}$  ( $k_t$ -factorization)

How important are photon initiated processes in hadronic collisions?



Then photon is a parton of proton.

Martin-Roberts-Stirling-Thorne 2004 include photons.

# MRSTQ parton distributions

The factorization of the QED-induced collinear divergences leads to QED-corrected evolution equations for the parton distributions of the proton.

$$\begin{aligned} \frac{\partial q_i(x, \mu^2)}{\partial \log \mu^2} &= \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{qq}(y) q_i\left(\frac{x}{y}, \mu^2\right) + P_{qg}(y) g\left(\frac{x}{y}, \mu^2\right) \right\} \\ &+ \frac{\alpha}{2\pi} \int_x^1 \frac{dy}{y} \left\{ \tilde{P}_{qq}(y) e_i^2 q_i\left(\frac{x}{y}, \mu^2\right) + P_{q\gamma}(y) e_i^2 \gamma\left(\frac{x}{y}, \mu^2\right) \right\} \\ \frac{\partial g(x, \mu^2)}{\partial \log \mu^2} &= \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{gq}(y) \sum_j q_j\left(\frac{x}{y}, \mu^2\right) + P_{gg}(y) g\left(\frac{x}{y}, \mu^2\right) \right\} \\ \frac{\partial \gamma(x, \mu^2)}{\partial \log \mu^2} &= \frac{\alpha}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{\gamma q}(y) \sum_j e_j^2 q_j\left(\frac{x}{y}, \mu^2\right) + P_{\gamma\gamma}(y) \gamma\left(\frac{x}{y}, \mu^2\right) \right\} \end{aligned}$$

# MRSTQ parton distributions

In addition to usual  $P_{qq}$ ,  $P_{gq}$ ,  $P_{qg}$ ,  $P_{gg}$  splitting functions new splitting functions appear.

$$\tilde{P}_{qq} = C_F^{-1} P_{qq},$$

$$P_{\gamma q} = C_F^{-1} P_{gq},$$

$$P_{q\gamma} = T_R^{-1} P_{qg},$$

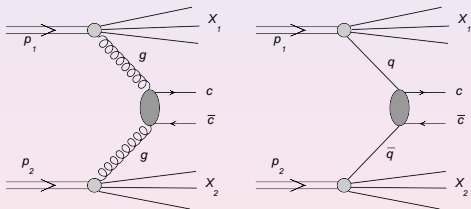
$$P_{\gamma\gamma} = -\frac{2}{3} \sum_i e_i^2 \delta(1-y)$$

momentum is conserved:

$$\int_0^1 dx x \left\{ \sum_i q_i(x, \mu^2) + g(x, \mu^2) + \gamma(x, \mu^2) \right\} = 1$$

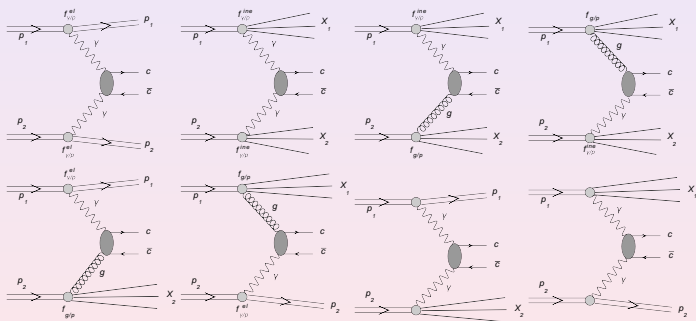
# Standard diagrams

- Standard diagrams

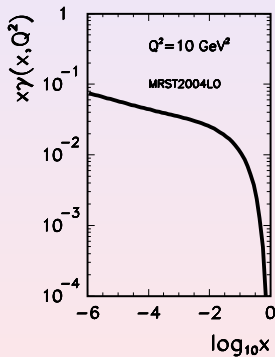
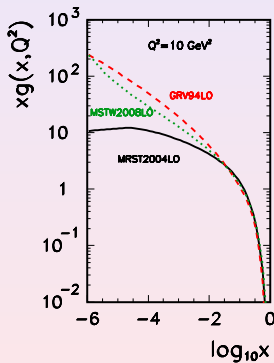


# Photon included diagrams

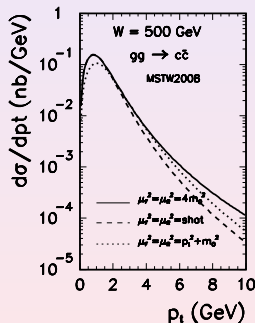
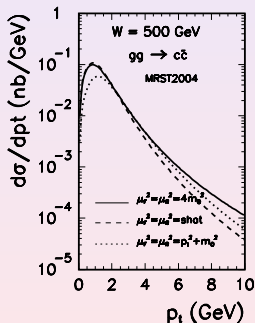
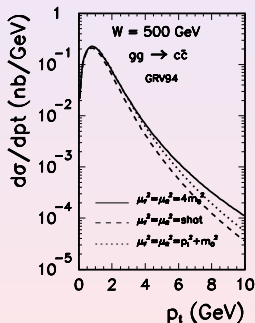
- Photon included diagrams



# Collinear LO gluon and photon distributions

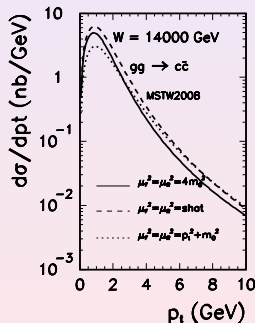
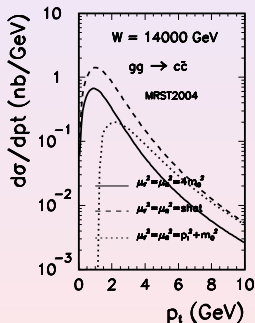
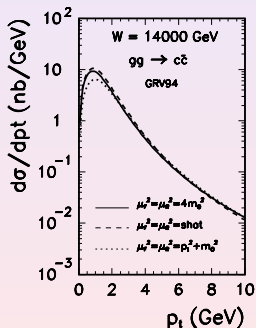


# Distribution in quark/antiquark transverse momentum at $\sqrt{s} = 500$ GeV

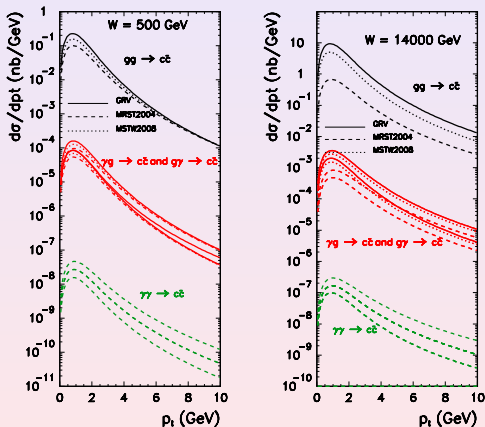




# Distribution in quark/antiquark transverse momentum at $\sqrt{s} = 14 \text{ TeV}$

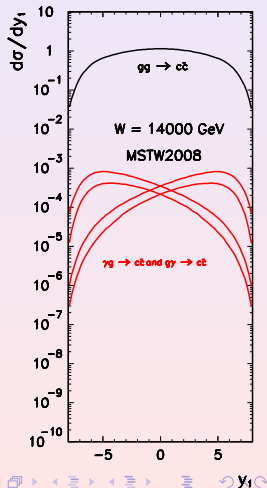
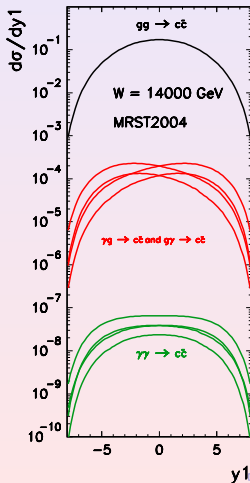
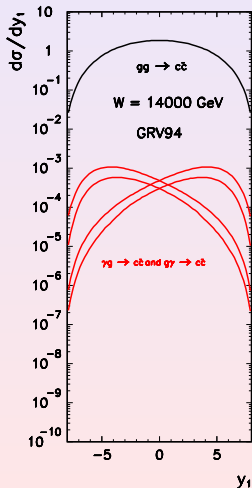


# Distribution in the transverse momentum

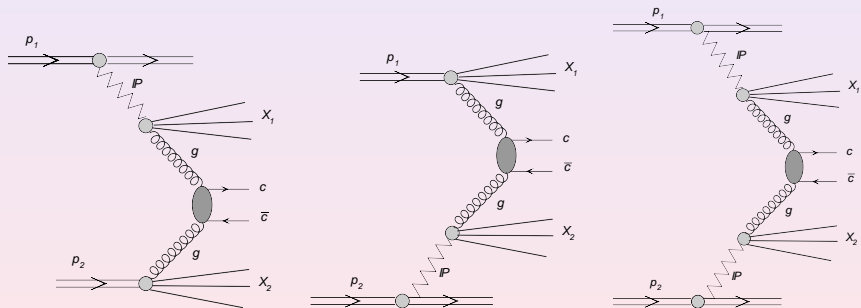


Luszczak, Maciula, Szczurek, Phys. Rev. **D84** (2011) 4018

# Distribution in the rapidity



# Single and central diffraction



Luszczak, Maciula, Szczurek, Phys. Rev. **D84** (2011) 4018

# Formalism

In this approach one assumes that the Pomeron has a well defined partonic structure, and that the hard process takes place in a Pomeron–proton or proton–Pomeron (**single diffraction**) or Pomeron–Pomeron (**central diffraction**) processes.

$$\frac{d\sigma_{SD}}{dy_1 dy_2 dp_t^2} = K \frac{|M|^2}{16\pi^2 \hat{s}^2} \left[ \left( x_1 q_f^D(x_1, \mu^2) x_2 \bar{q}_f(x_2, \mu^2) \right) + \left( x_1 \bar{q}_f^D(x_1, \mu^2) x_2 q_f(x_2, \mu^2) \right) \right],$$

$$\frac{d\sigma_{CD}}{dy_1 dy_2 dp_t^2} = K \frac{|M|^2}{16\pi^2 \hat{s}^2} \left[ \left( x_1 q_f^D(x_1, \mu^2) x_2 \bar{q}_f^D(x_2, \mu^2) \right) + \left( x_1 \bar{q}_f^D(x_1, \mu^2) x_2 q_f^D(x_2, \mu^2) \right) \right]$$

# Formalism

The 'diffractive' quark distribution of flavour  $f$  can be obtained by a convolution of the **flux of Pomerons**  $f_{\mathbf{P}}(x_{\mathbf{P}})$  and the **parton distribution in the Pomeron**  $q_{f/\mathbf{P}}(\beta, \mu^2)$ :

$$q_f^D(x, \mu^2) = \int dx_{\mathbf{P}} d\beta \delta(x - x_{\mathbf{P}}\beta) q_{f/\mathbf{P}}(\beta, \mu^2) f_{\mathbf{P}}(x_{\mathbf{P}}) = \int_x^1 \frac{dx_{\mathbf{P}}}{x_{\mathbf{P}}} f_{\mathbf{P}}(x_{\mathbf{P}}) q_{f/\mathbf{P}}\left(\frac{x}{x_{\mathbf{P}}}, \mu^2\right).$$

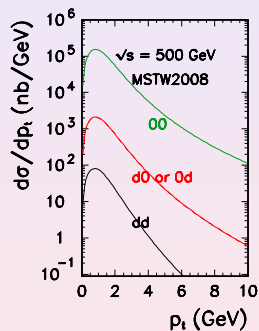
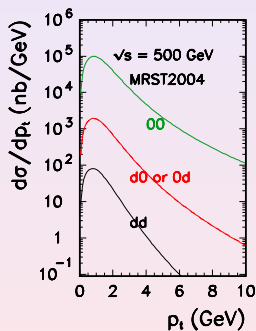
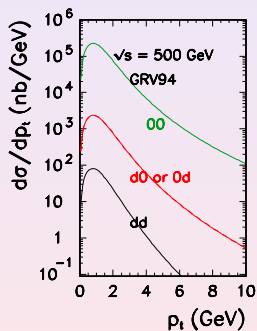
The flux of Pomerons  $f_{\mathbf{P}}(x_{\mathbf{P}})$ :

$$f_{\mathbf{P}}(x_{\mathbf{P}}) = \int_{t_{\min}}^{t_{\max}} dt f(x_{\mathbf{P}}, t),$$

with  $t_{\min}$ ,  $t_{\max}$  being kinematic boundaries.

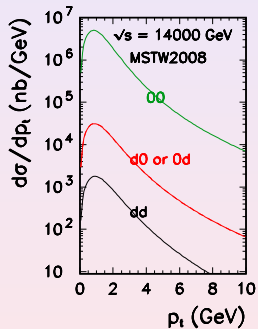
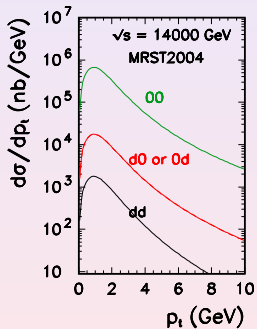
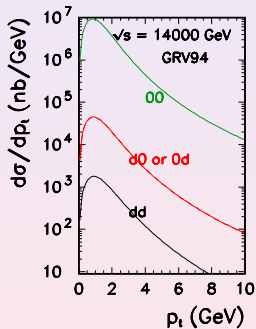
Both pomeron flux factors  $f_{\mathbf{P}}(x_{\mathbf{P}}, t)$  as well as quark/antiquark distributions in the pomeron were taken from the H1 collaboration analysis of diffractive structure function at HERA.

## Results



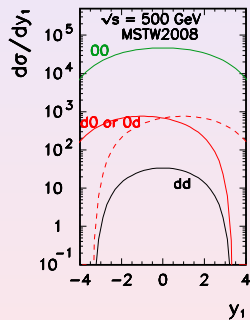
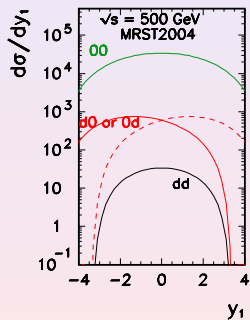
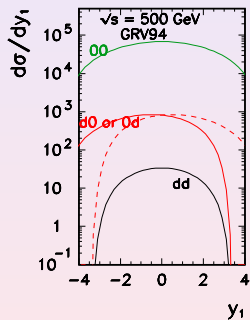
Absorption has been included

## Results

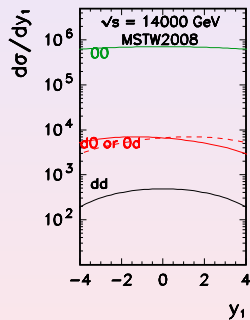
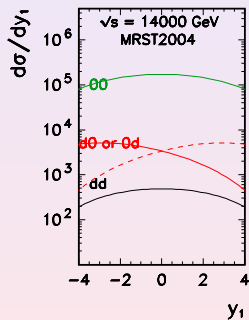
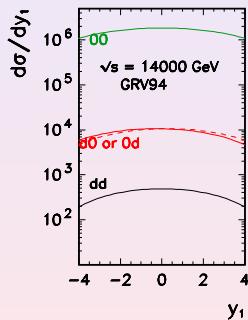




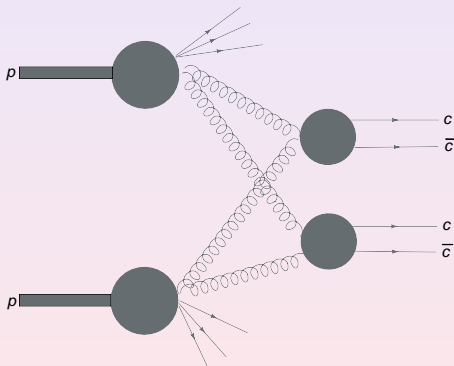
# Results



## Results



# Production of two $c\bar{c}$ pairs in double-parton scattering



Luszczak, Maciula, Szczurek, arXiv:1111.3255

# Formalism

$$\sigma^{DPS}(pp \rightarrow c\bar{c}c\bar{c}X) = \frac{1}{2\sigma_{\text{eff}}}\sigma^{SPS}(pp \rightarrow c\bar{c}X_1) \cdot \sigma^{SPS}(pp \rightarrow c\bar{c}X_2).$$

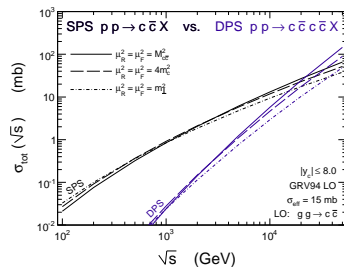
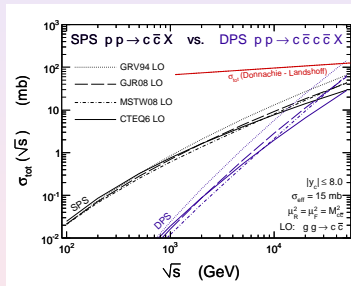
The simple formula can be generalized to include differential distributions

$$\frac{d\sigma}{dy_1 dy_2 d^2 p_{1t} dy_3 dy_4 d^2 p_{2t}} = \frac{1}{2\sigma_{\text{eff}}} \cdot \frac{d\sigma}{dy_1 dy_2 d^2 p_{1t}} \cdot \frac{d\sigma}{dy_3 dy_4 d^2 p_{2t}}.$$

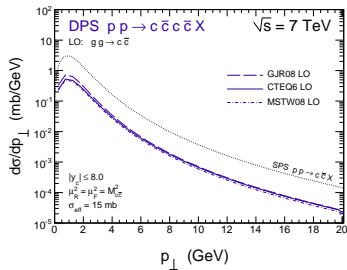
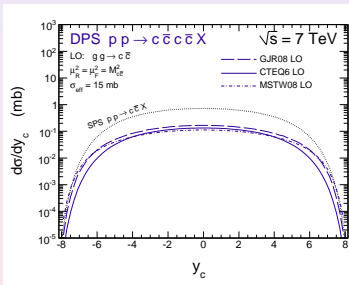
$$d\sigma^{DPS} = \frac{1}{2\sigma_{\text{eff}}} F_{gg}(x_1, x_2, \mu_1^2, \mu_2^2) F_{gg}(x'_1, x'_2, \mu_1^2, \mu_2^2)$$

$$d\sigma_{gg \rightarrow c\bar{c}}(x_1, x'_1, \mu_1^2) d\sigma_{gg \rightarrow c\bar{c}}(x_2, x'_2, \mu_2^2) dx_1 dx_2 dx'_1 dx'_2$$

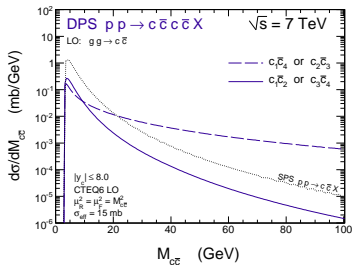
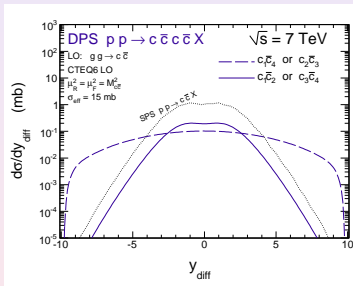
## Results



# Results



# Results



# Conclusions

- Huge sensitivity to gluon distribution and scales for  $W=14000$  GeV.
- We have calculated cross section for many new photon included processes. They are small but there are many of them.
- The cross sections for single and central diffraction have been calculated. The  $SD_{c\bar{c}}$  smaller by 2 orders of magnitude than the dominant  $gg$  term.
- We predict large cross section for two  $c\bar{c}$  pair production in double-parton scattering.